

HAIR: History of Animals using Isotope Records

(You are what you eat . . . plus a few ‰)

- Thure Cerling
University of Utah



Thanks

- Linda Ayliffe, Gabe Bowen, Claire Cerling, Dylan Cerling, Lesley Chesson, Edna Ehleringer, Jim Ehleringer, Iain Douglas-Hamilton, Jackson King'oo, Passey, Dave Podlesak, Chris Remien, Jerry Schuster, Matt Sponheimer, Kevin Uno, George Wittemyer
- *IsoForensics, Kenya Wildlife Service, National Science Foundation, Packard Foundation, Save-The-Elephants, Sheldrick Wildlife Trust*

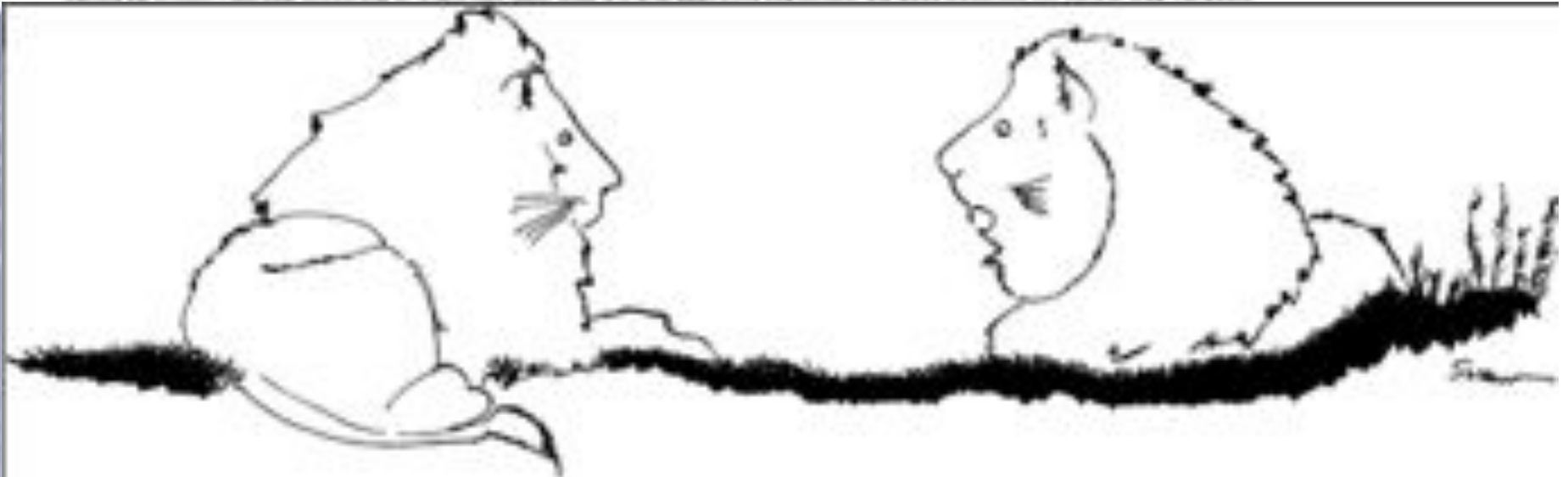
PNAS 10 Nov 2009

Cooperation and individuality among man-eating lions

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Jonathan W. Moore⁶, Paul L. Koch⁷, and Nathaniel J. Dominy^{1,8,9}

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Edited by Simon Hawkes, University of Utah, Salt Lake City, UT, and approved September 25, 2009 (received for review May 12, 2009)



"I'm trying to eat more vegetarians."

The New Yorker, 14 Dec 2009

Elements are defined by the number of protons in the nucleus:

1=H, 2=He, 3 = Li, 4 = Be, 5 = B, 6 = C, 7 = N, 8 = O, and so on . . .

PERIODIC TABLE OF THE ELEMENTS

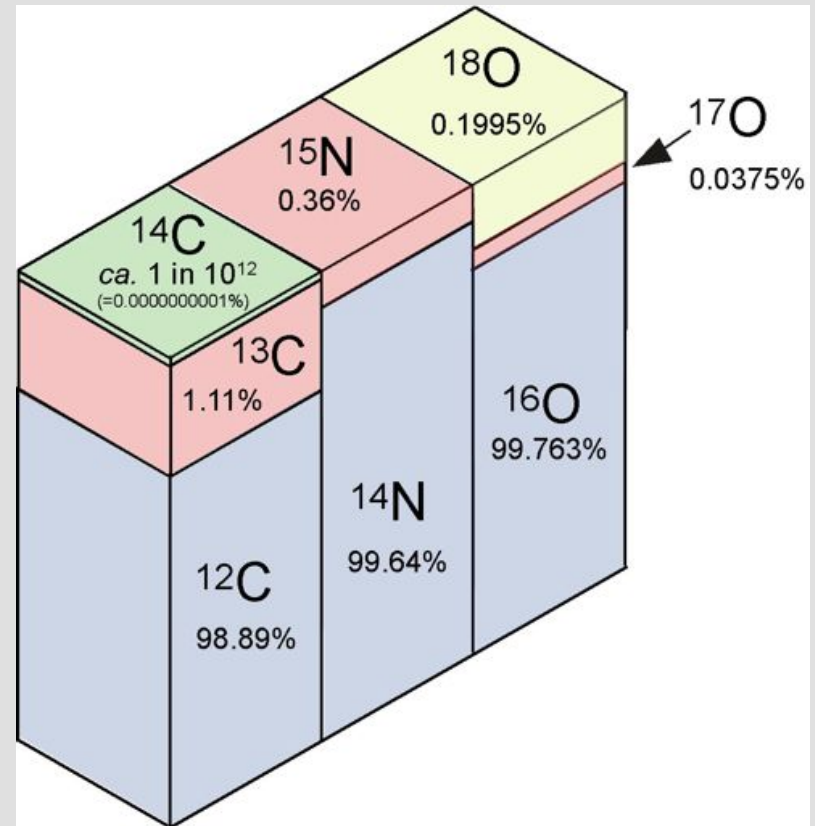
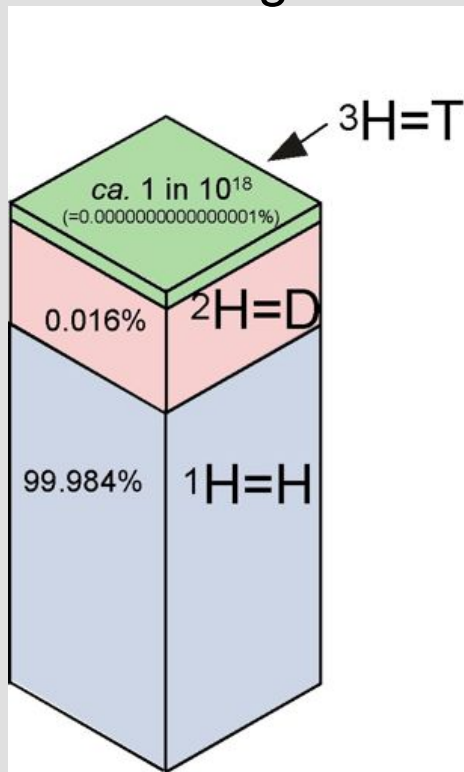
1 IA	PERIODIC TABLE OF THE ELEMENTS																18 VIIIA	
1 H Hydrogen 1.0079	2 IIA												13 IIIA	14 IVA	15 VA	16 VIA	17 VIIA	18 He Helium 4.0026
2 Li Lithium 6.941	Be Beryllium 9.0122											B Boron 10.811	C Carbon 12.011	N Nitrogen 14.007	O Oxygen 15.999	F Fluorine 18.998	Ne Neon 20.179	
3 Na Sodium 22.990	Mg Magnesium 24.305											Al Aluminum 26.982	Si Silicon 28.086	P Phosphorus 30.974	S Sulfur 32.065	Cl Chlorine 35.453	Ar Argon 39.948	
4 K Potassium 39.098	Ca Calcium 40.078	Sc Scandium 44.956	Ti Titanium 47.887	V Vanadium 50.942	Cr Chromium 51.996	Mn Manganese 54.938	Fe Iron 55.845	Co Cobalt 58.933	Ni Nickel 58.693	Cu Copper 63.546	Zn Zinc 65.38	Ga Gallium 69.723	Ge Germanium 72.64	As Arsenic 74.922	Se Selenium 78.94	Br Bromine 79.904	Kr Krypton 83.80	
5 Rb Rubidium 85.468	Sr Strontium 87.62	Y Yttrium 88.906	Zr Zirconium 91.224	Nb Niobium 92.906	Mo Molybdenum 95.94	Tc Technetium (98)	Ru Ruthenium 101.07	Rh Rhodium 101.07	Pd Palladium 106.42	Ag Silver 107.87	Cd Cadmium 112.41	In Indium 114.82	Sn Tin 118.71	Sb Antimony 121.75	Te Tellurium 127.6	I Iodine 126.90	Xe Xenon 131.29	
6 Cs Cesium 132.91	Ba Barium 137.33	La Lanthanide	Hf Hafnium 178.49	Ta Tantalum 180.95	W Tungsten 183.84	Re Rhenium 186.21	Os Osmium 190.23	Ir Iridium 192.22	Pt Platinum 195.08	Au Gold 196.97	Hg Mercury 200.59	Tl Thallium 204.38	Pb Lead 207.2	Bi Bismuth 208.98	Po Polonium (209)	At Astatine (210)	Rn Radon (222)	
7 Fr Francium (223)	Ra Radium (226)	Ac Actinide	Rf Rutherfordium (261)	Db Dubnium (262)	Sg Seaborgium (266)	Bh Bohrium (264)	Hs Hassium (277)	Mt Meitnerium (268)	Uun Ununium (271)	Uuu Ununium (272)	Uub Ununium (274)	Uut Ununium (284)	Uuq Ununium (286)	Uup Ununium (288)	Uuh Ununium (290)	Uus Ununium (294)	Uuo Ununium (294)	

1	K	2	2	2	2	2
2	L	8	2	6		
3	M	18	2	6	10	
4	N	32	2	6	10	14
5	O	32	2	6	10	14
6	P	18	2	6	10	
7	Q	8	2	6		
8	R	2	2			

57 La Lanthanum 138.91	58 Ce Cerium 140.12	59 Pr Praseodymium 140.91	60 Nd Neodymium 144.24	61 Pm Promethium (145)	62 Sm Samarium 150.36	63 Eu Europium 151.96	64 Gd Gadolinium 157.25	65 Tb Terbium 158.93	66 Dy Dysprosium 162.50	67 Ho Holmium 164.93	68 Er Erbium 167.26	69 Tm Thulium 168.93	70 Yb Ytterbium 173.05	71 Lu Lutetium 174.97
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89 Ac Actinium 227	90 Th Thorium 232.04	91 Pa Protactinium 231.04	92 U Uranium 238.03	93 Np Neptunium 237.05	94 Pu Plutonium 244.06	95 Am Americium 243.06	96 Cm Curium 247.07	97 Bk Berkelium 247.07	98 Cf Californium 251.08	99 Es Einsteinium 252.08	100 Fm Fermium 257.10	101 Md Mendelevium 258.10	102 No Nobelium 259.10	103 Lr Lawrencium 262.10
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Isotopes are the different numbers of neutrons for a given proton configuration



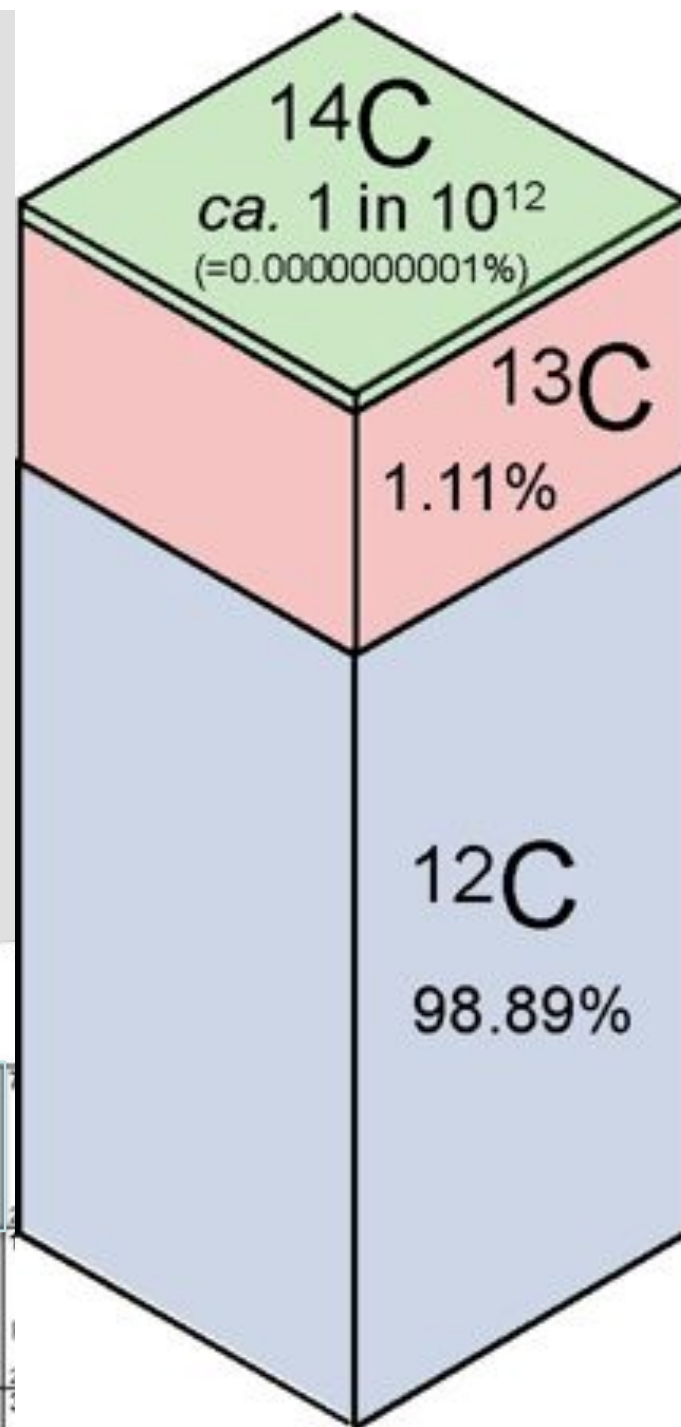
1	IA
1	H
	Hydrogen
	1.0079
1	2
3	4
	IA

	14	15	16	
IIIA	IVA	VA	VIA	VIIA
5	6	7	8	9
B	C	N	O	F
Boron	Carbon	Nitrogen	Oxygen	Fluorine
10.811	12.011	14.007	15.999	18.998
2-3	2-4	2-5	2-6	2-7
13	14	15	16	17
Al	Si	P	S	Cl
Aluminium	Silicon	Phosphorus	Sulphur	Chlorine
26.982	28.086	30.974	32.065	35.453
2-8-3	2-8-4	2-8-5	2-8-6	2-8-7
31	32	33	34	35
Ge	As	Se	P	
Germanium	Arsenic	Selenium	Phosphorus	
72.64	74.922	78.972	78.972	
2-8-3-2	2-8-4-3	2-8-5-3	2-8-6-4	

Isotopes are the different numbers of neutrons for a given proton configuration

Isotope	protons	neutrons
^{12}C	6	6
^{13}C	6	7
^{14}C	6	8

5 B Boron 10.811	6 C Carbon 12.011
13 Al Aluminium 26.982	14 Si Silicon 28.086
31 Ga Gallium	32 Ge Germanium



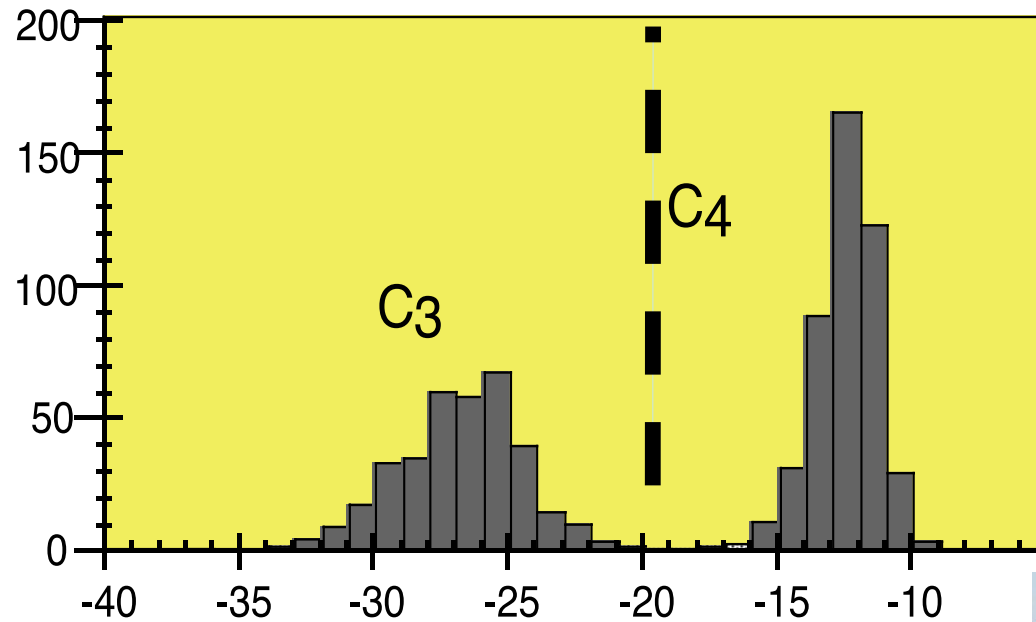
Isotope terminology

- $R_{\text{phase}} = {}^{13}\text{C}/{}^{12}\text{C}$ ratio in “phase”
- $\delta^{13}\text{C} (\text{‰}) = (R_{\text{phase}} / R_{\text{standard}} - 1) * 1000$
- On Earth, ${}^{13}\text{C}$ ranges from 1.04‰ to about 1.14‰ (*ca.* $\delta^{13}\text{C}$ range from -65‰ to +25‰)

Stable isotopes and animal behavior on different time scales

- A Traveler's Tale
- You are what you eat. Plus a few ‰.
- Reaction progress variable
- Modern elephant isotope ecology
- NCIS - forensics

$\delta^{13}\text{C}$ distinction between C_3 and C_4 plants



$\delta^{13}\text{C}$

← Almost everything else

→ tropical grasses

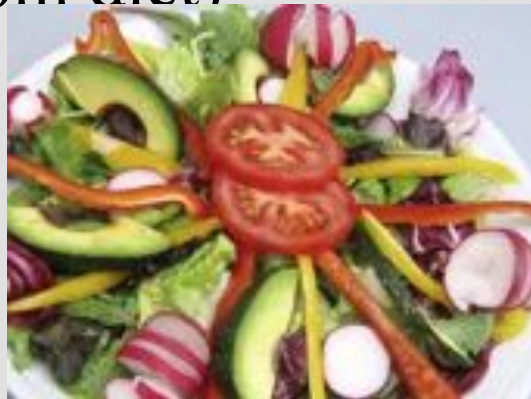


C_3 and C_4 photosynthesis



- C_3 plants
- most dicots
- cool-season grasses
- Foods: vegetables, fruits, beans, wheat, barley, rye, meat (from diet)

- C_4 plants
- rare in dicots
- tropical grasses and sedges
- Foods: maize, sorghum, sugar cane, millet, tef, fonio, and meat (from diet)



You are what you eat . . .

. . . plus a few permil (‰)

Ginger Nut



Ingredients:

Flour, Cornflour, Sugar, Hydrogenated Vegetable Oil, Ginger Powder, Salt, Invert Syrup, Lecithin, Chemicals, Synthetic Flavours & Permissible Food Colours.

Net Weight when packed 200 gms.

المكونات
دقيق، دقيق الذرة، سكر، زيت نباتي، مستحوق زنجبيل، ملح، عصير، لیسٹین، کیمائیات رواحج، اللون غذائیه -
الوزن: ۲۰۰ غرام

جسٹراء
گندم کا آٹا، ذائقہ، گندمی، بنا سیتی، ایڑک کا پائڈر، نمک، ایڑرٹ سیرپ، لیسٹین، کیمیکلز، مستحوقی، لیسٹین اور منظر شدہ ٹوٹو کٹر۔
وزن: ۲۰۰ گرام

English Biscuit Manufacturers (Private) Limited
Karachi - Pakistan.

Max. Retail Price

MAX. RETAIL RS 7.75



New

Ginger Nut

Biscuits



You are . . .

. . . what you eat.

Ingredients:

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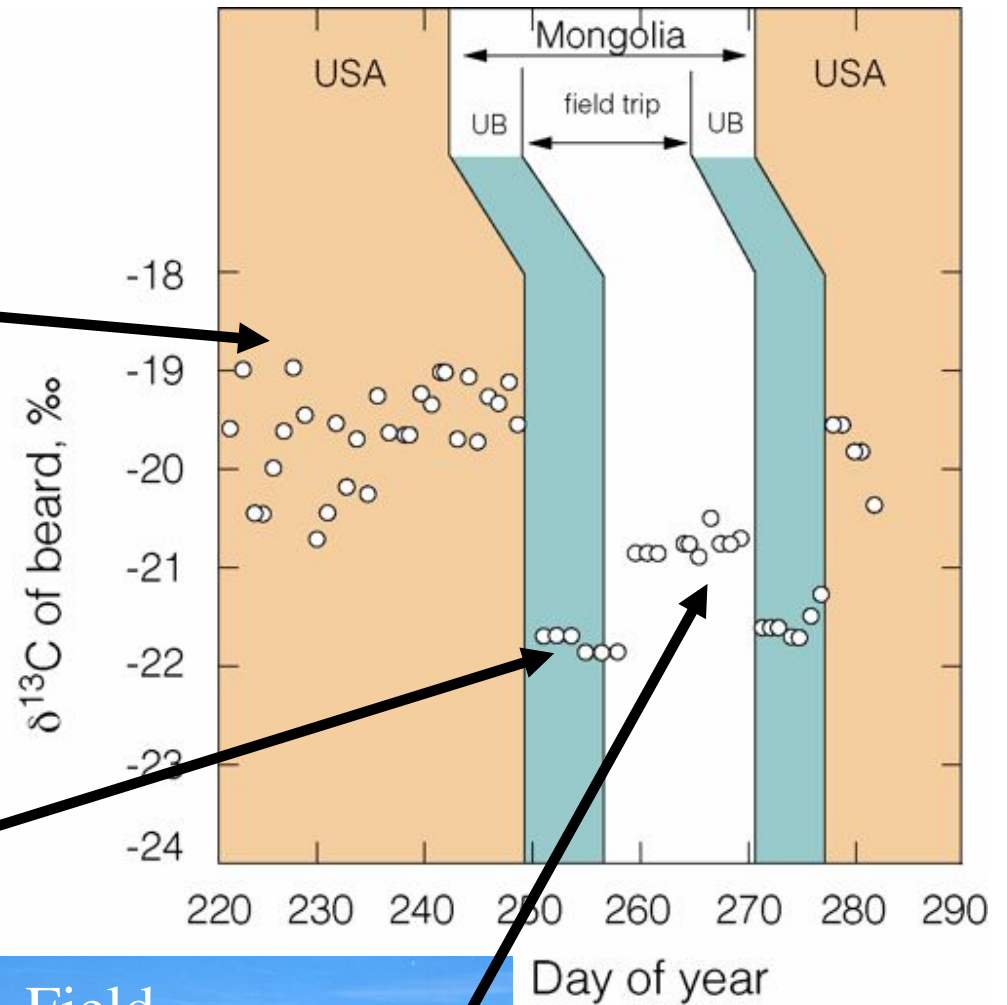
What the traveler ate . . .



Got milk?



Movements between Mongolia and USA are recorded in beard hair



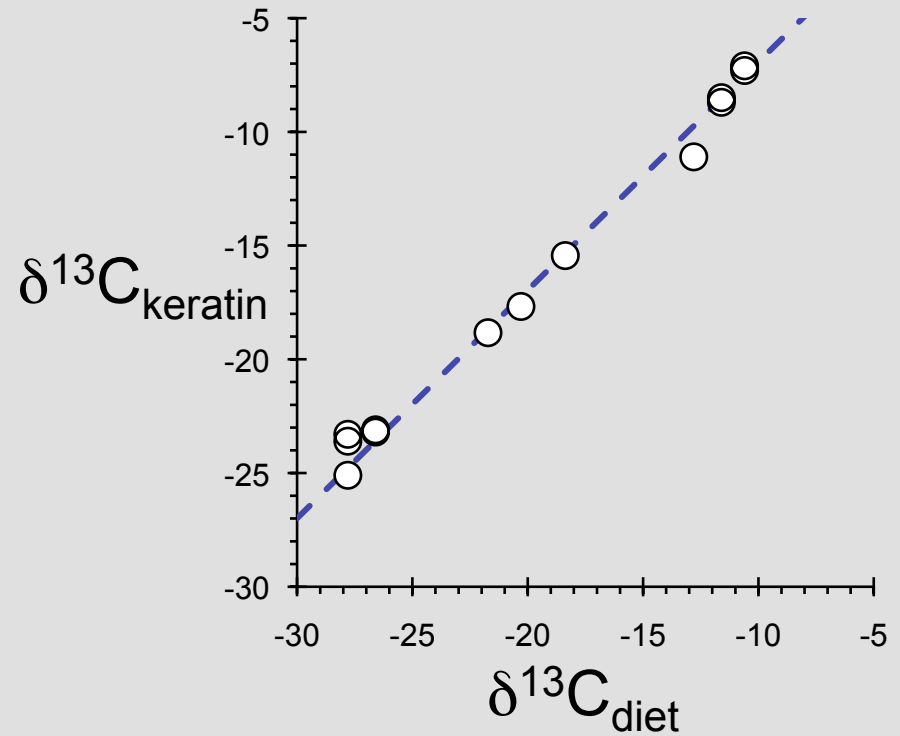


Univ Utah-BYU : controlled diets

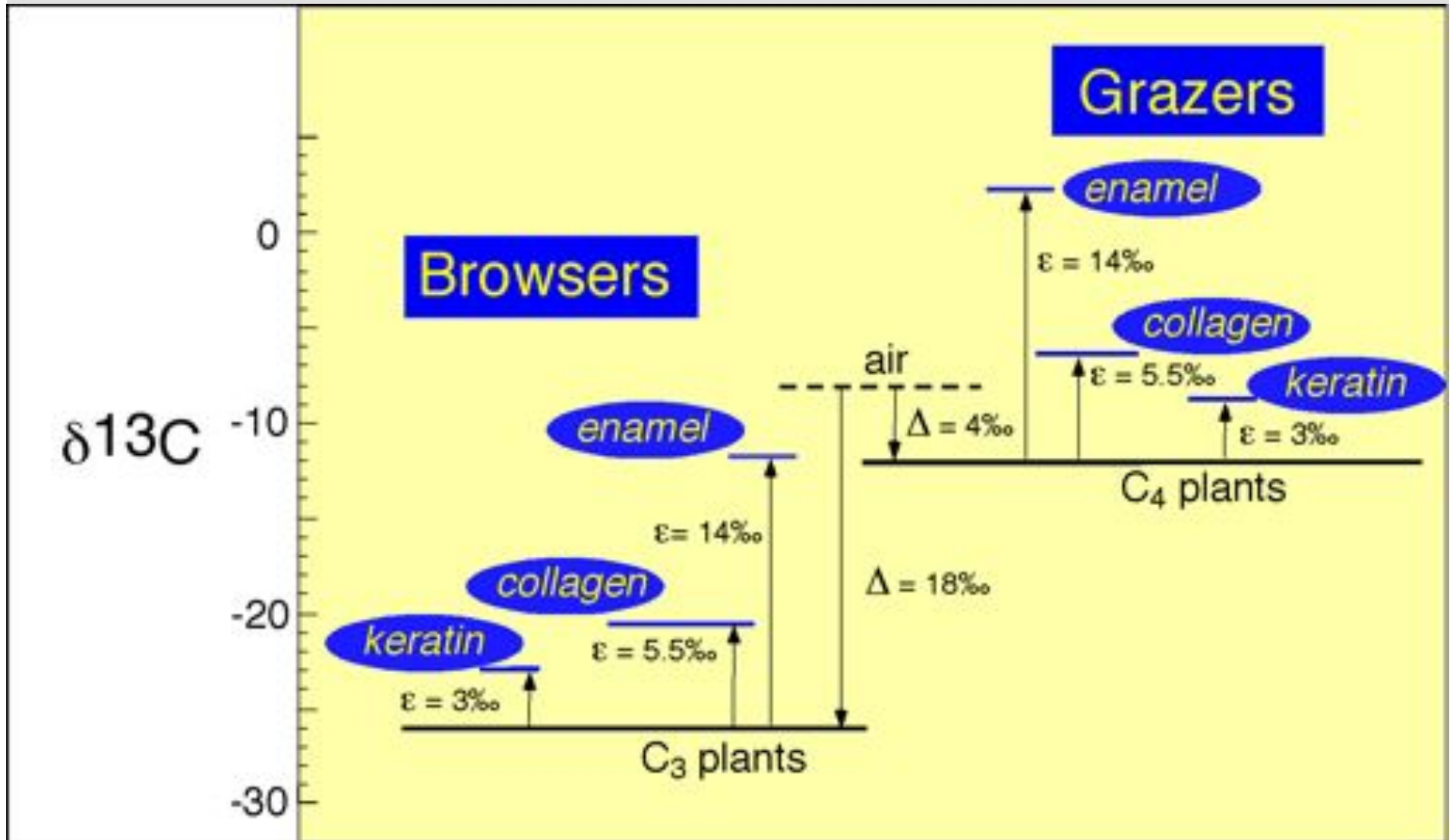




Isotope enrichment $\epsilon^*_{\text{hair-diet}} = 3.1\text{‰}$



Isotope discrimination (air to plant) and enrichment (diet to animal tissue)



Controlled diet change UU – BYU

diet change of horses: C_3 to C_4 . Back to C_3 after 150 days. Ends with 7 day spike of C_4

- horse tail hair sectioned to 1 mm (ca. 1 day)

Team Utah-BYU

Dandy with Linda Ayliffe

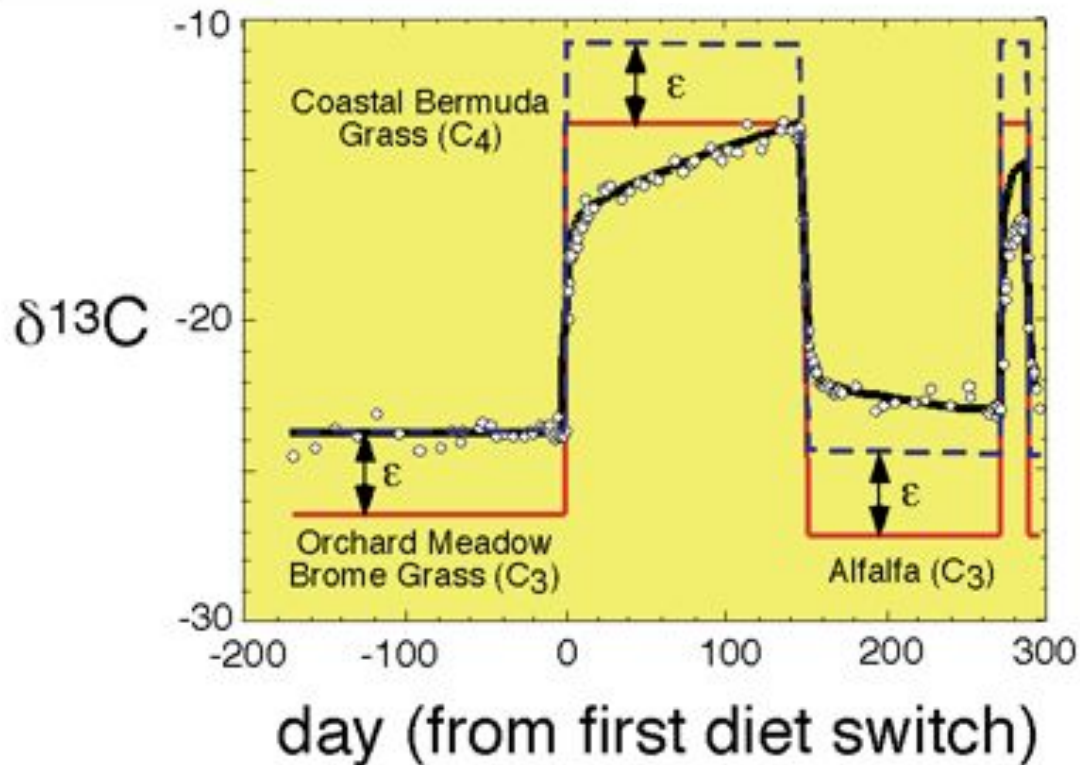
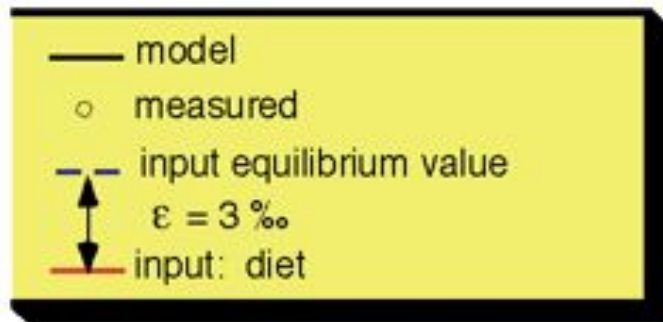


Controlled diet change UU - BYU

- diet change: C_3 to C_4 . Back to C_3 after 150 days. Ends with 7 day spike of C_4
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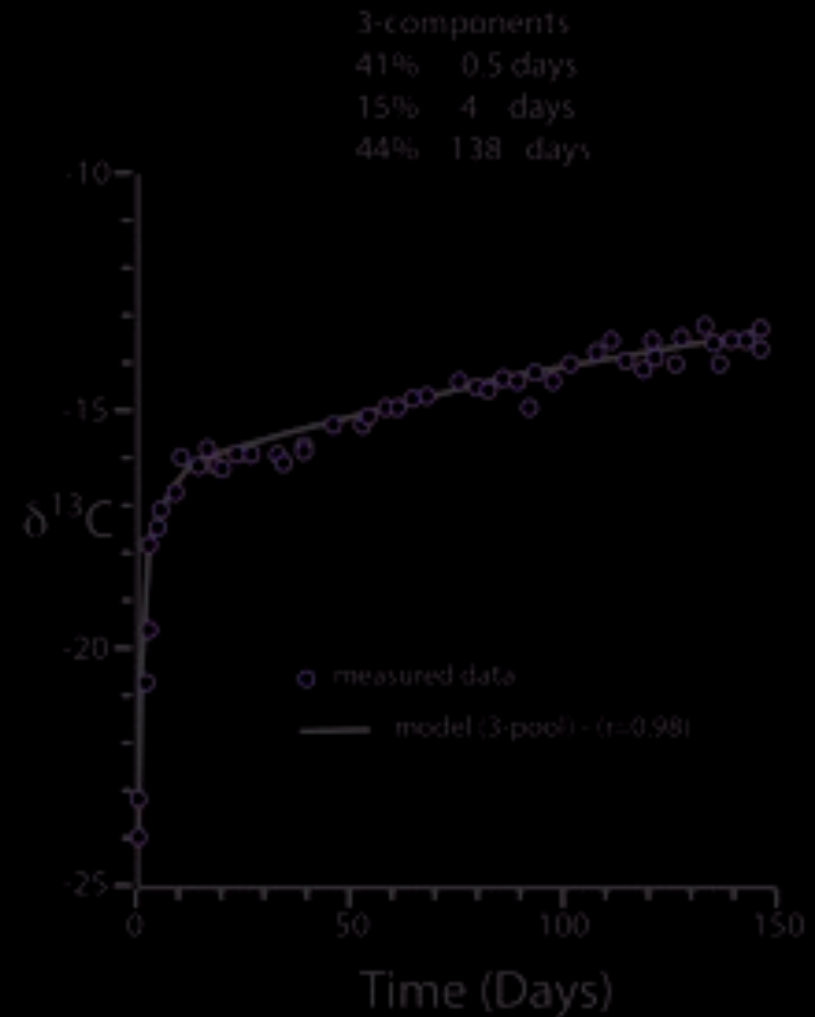
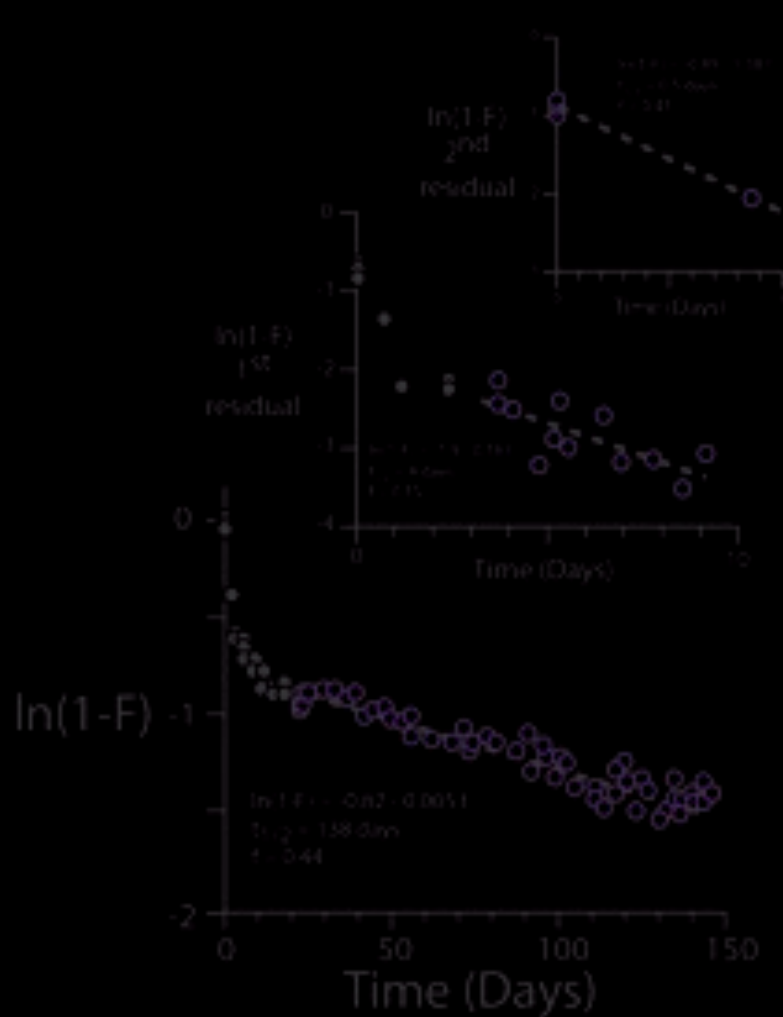
Hair treated as $dN_i/dt = -\lambda_i N_i$

Isotope composition of hair predicted from known



-Ayliffe et al.
2004

Treat as “reaction progress”: isotope values normalized from 0 to 1 (Ayliffe et al., 2004; Cerling et al 2007)



Model to directly calculate diet from isotope measurements of hair

Each pool changes as:

$$\delta_{i,(t)} = \delta_{i,(t-1)} e^{-\lambda_i(\Delta t)} + \delta_{D(t)} (1 - e^{-\lambda_i(\Delta t)})$$

And thus diet is directly calculated as:

$$\delta_{D(t)} = \frac{\left(\frac{\delta_H + 1000}{\alpha_{HD}} - 1000 \right) - \left(\sum_{i=1}^n f_i \delta_{i,t-1} e^{-\lambda_i \Delta t} \right)}{\left(\sum_{i=1}^n f_i (1 - e^{-\lambda_i \Delta t}) \right)}$$

(Although need to guess values at $t = 0$)

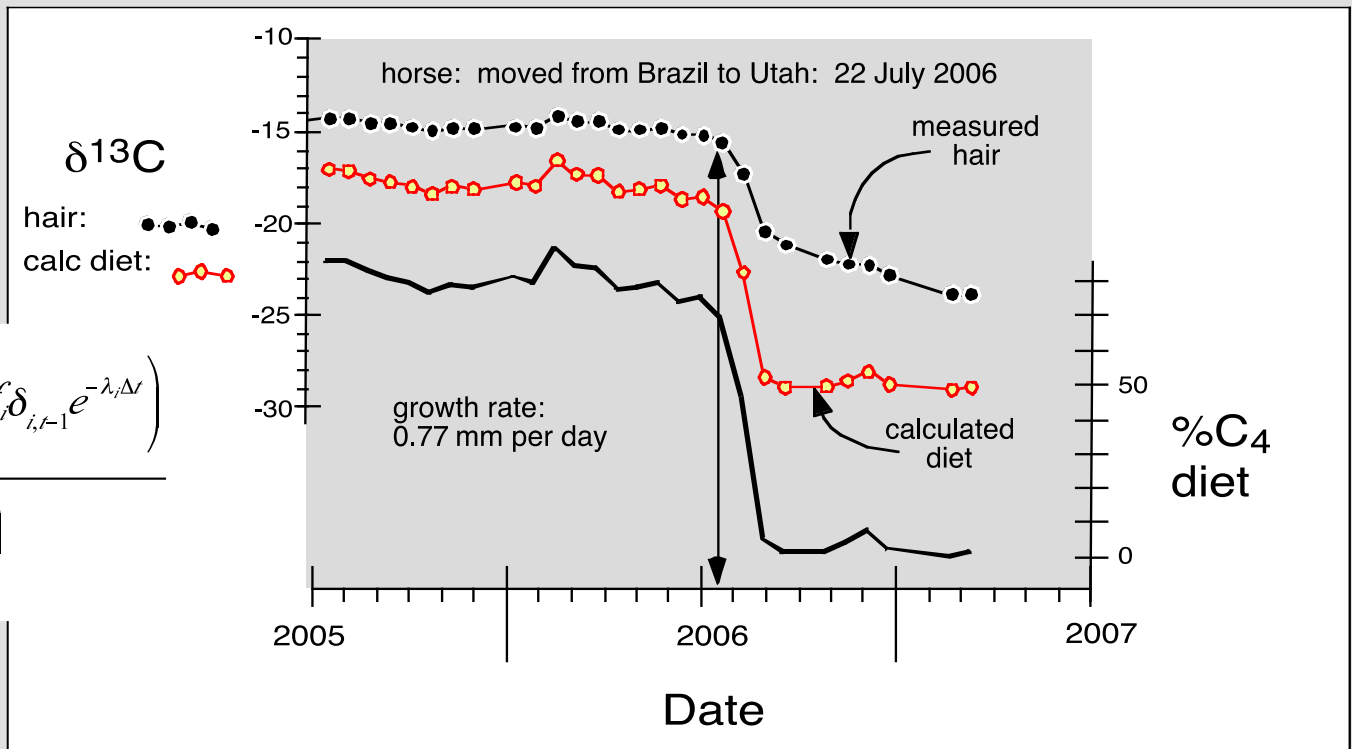
-Cerling et al., 2004

Direct calculation of diet from sequence

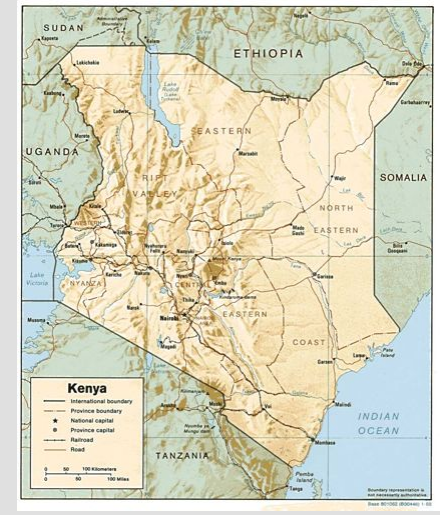
- Horse moved from Brazil to Utah: July 2006
- Sampled April 2007
- Assume growth rate of 0.77 mm per day to match known time of movement
- Model of Cerling et al. (2007)

-unpublished

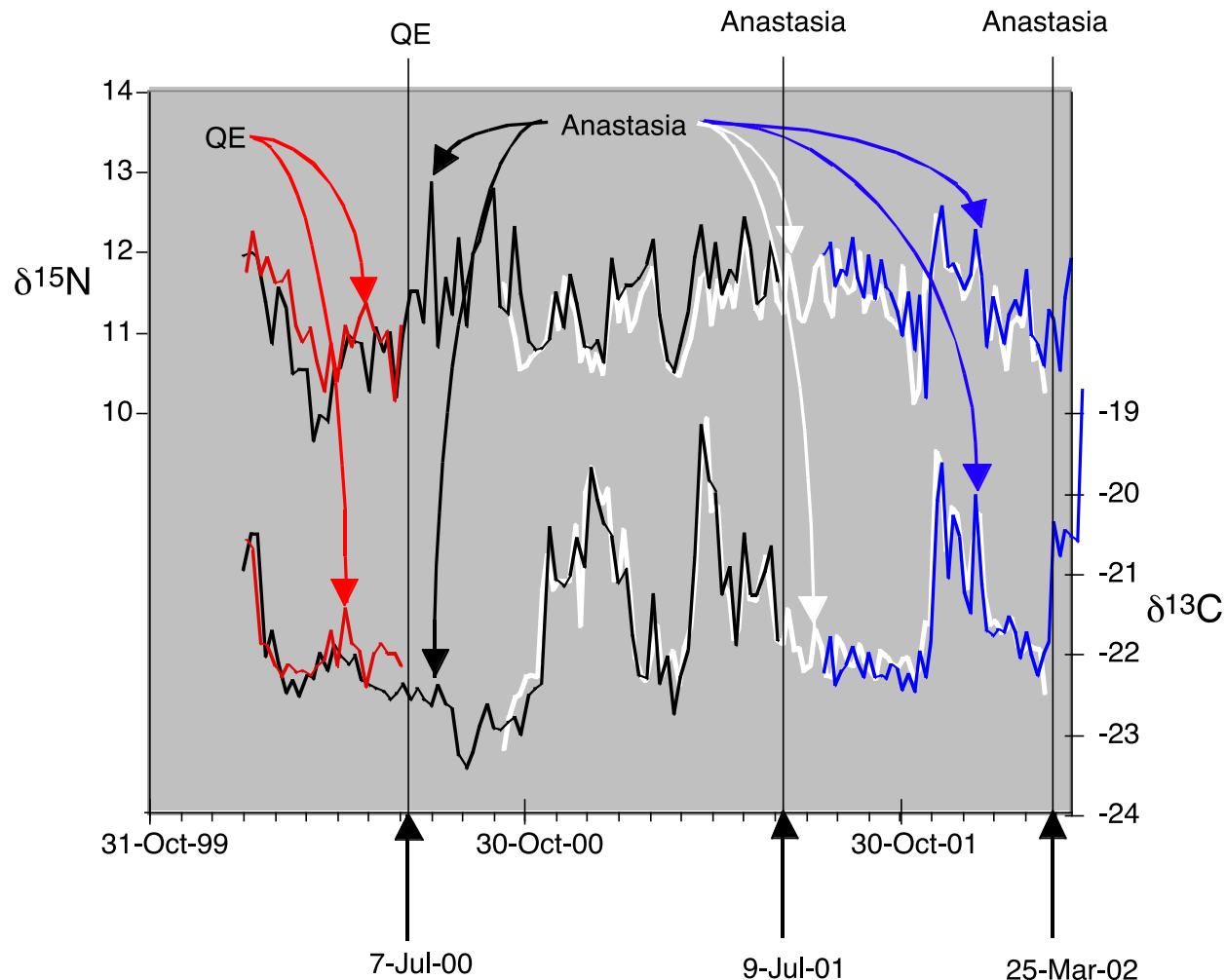
$$\delta_{D(t)} = \frac{\left(\frac{\delta_H + 1000}{\alpha_{HD}} - 1000 \right) - \left(\sum_{i=1}^3 f_i \delta_{i,t-1} e^{-\lambda_i \Delta t} \right)}{\left(\sum_{i=1}^3 f_i (1 - e^{-\lambda_i \Delta t}) \right)}$$



GPS collars and elephant hair



How do we get growth rates of hair?

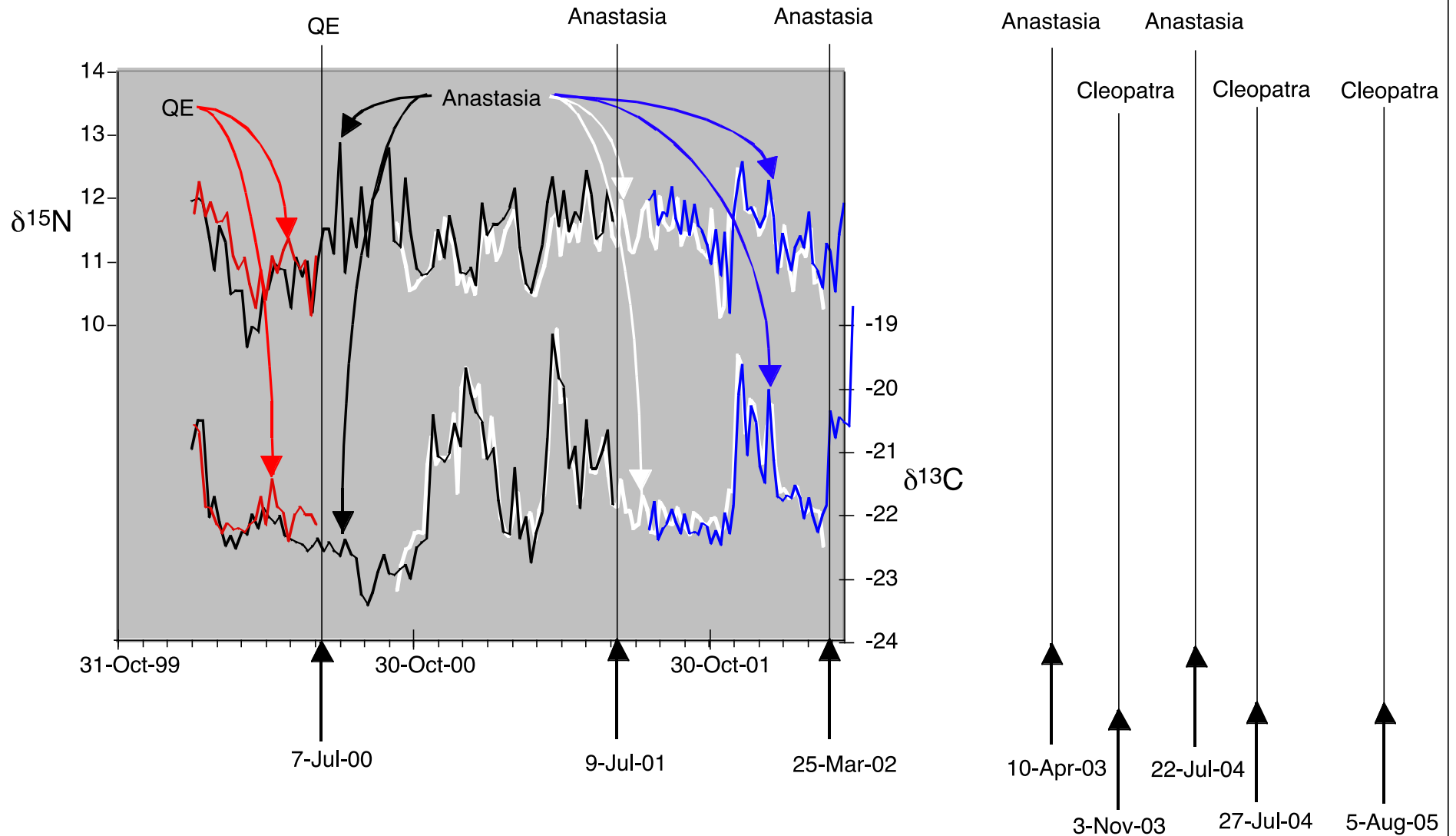


Collect hair
from same individual
several times.

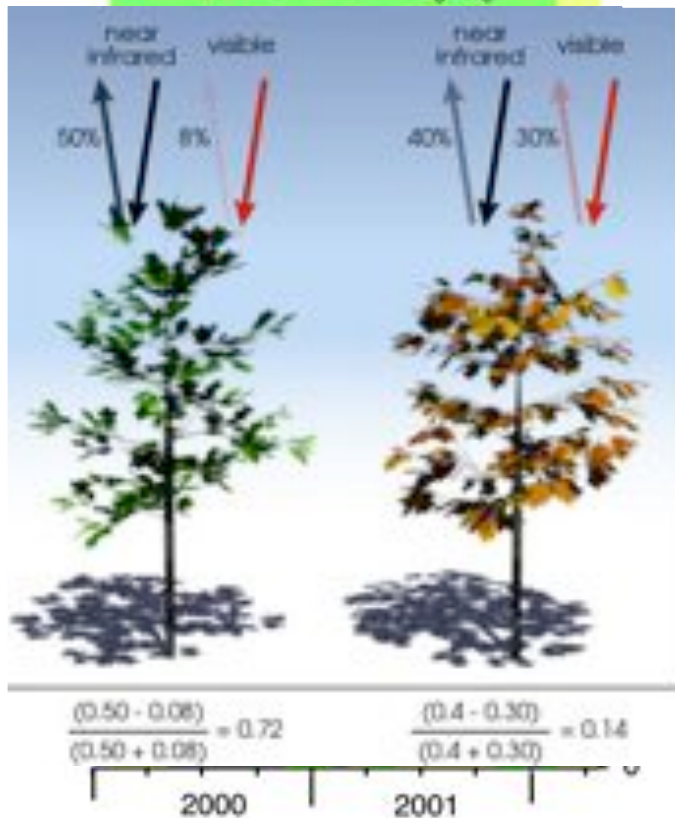
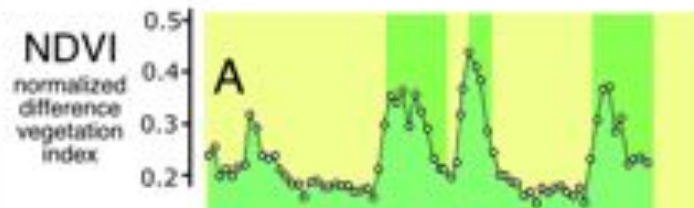
“Wiggle Match”

Can also correlate
to other individuals
QE is in same
family unit as
Anastasia (QE is
mother of Anastasia)

Baton is passed to Cleopatra (sister)



Quantify the importance of grass during rainy season

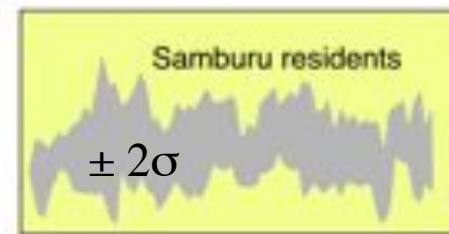
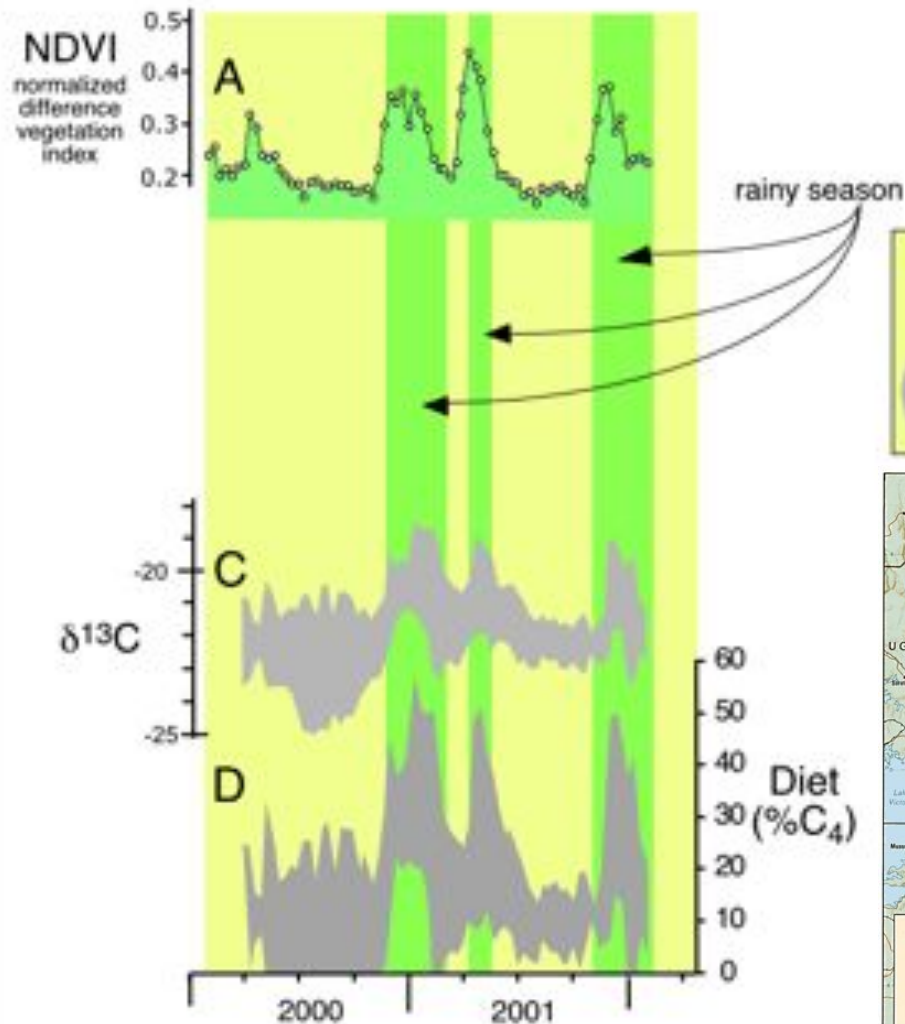


$$NDVI = \frac{(NRI - VIS)}{(NRI + VIS)}$$

Samburu



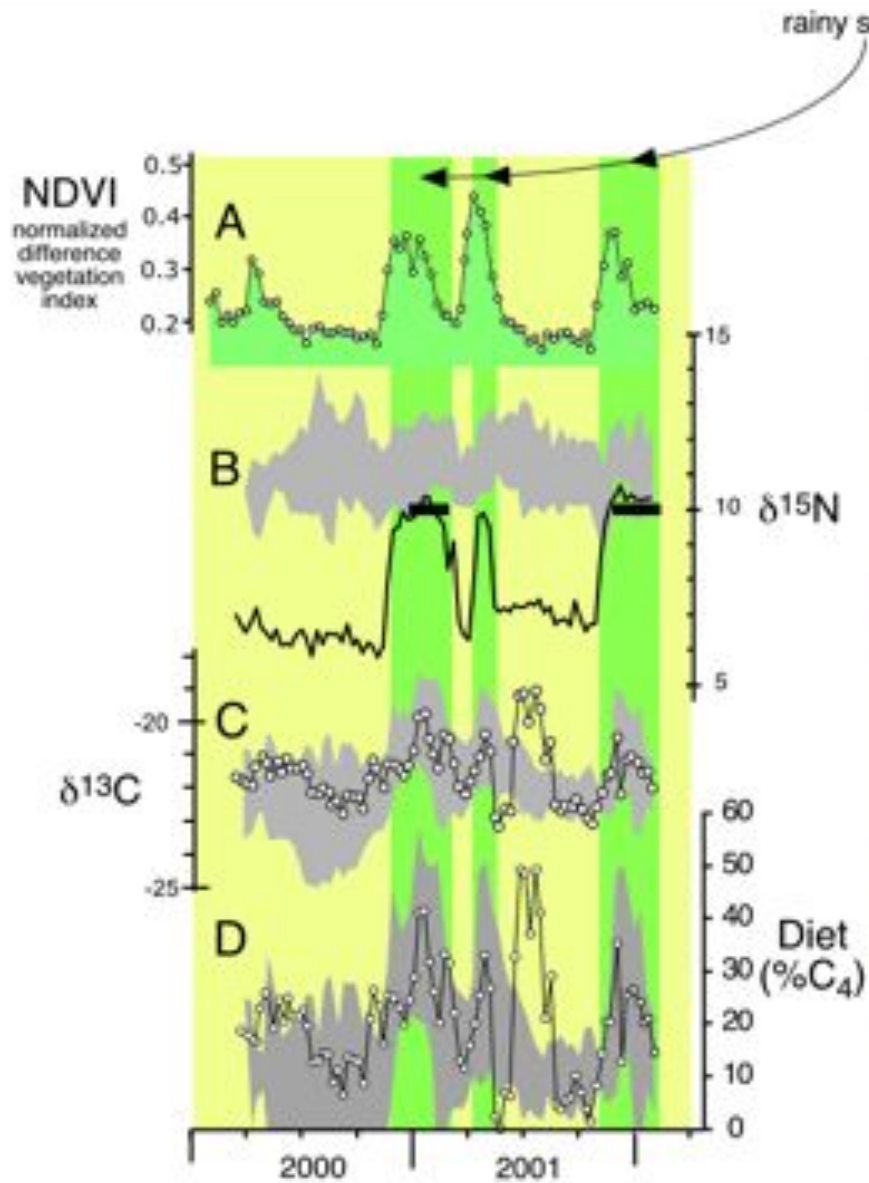
Quantify the importance of grass during rainy season



Samburu

Data is for average $\pm 2\sigma$ for 5 Samburu Reserve resident elephants

Lewis, the wandering elephant

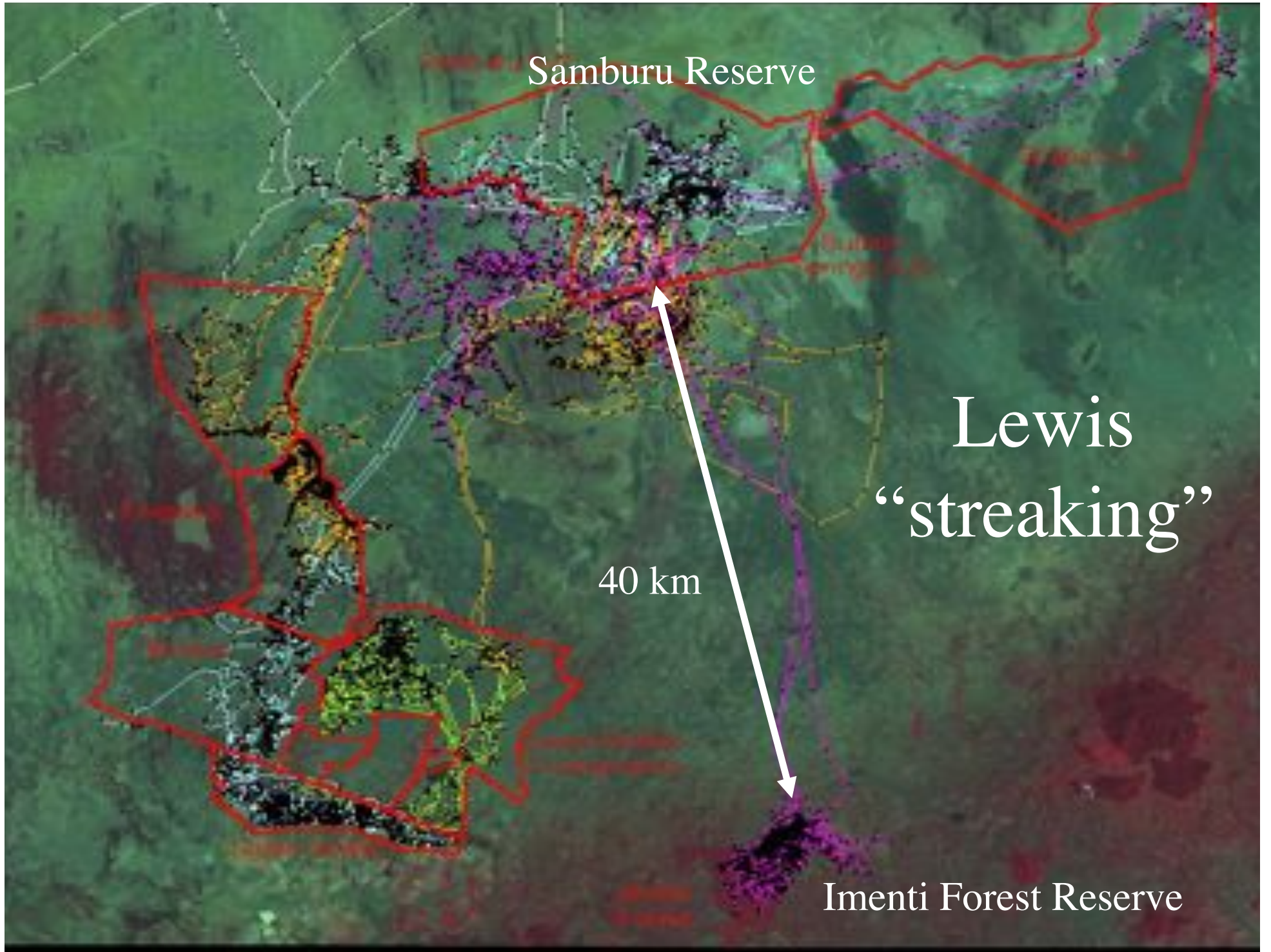


Samburu

Seasonal migration

Mt. Kenya



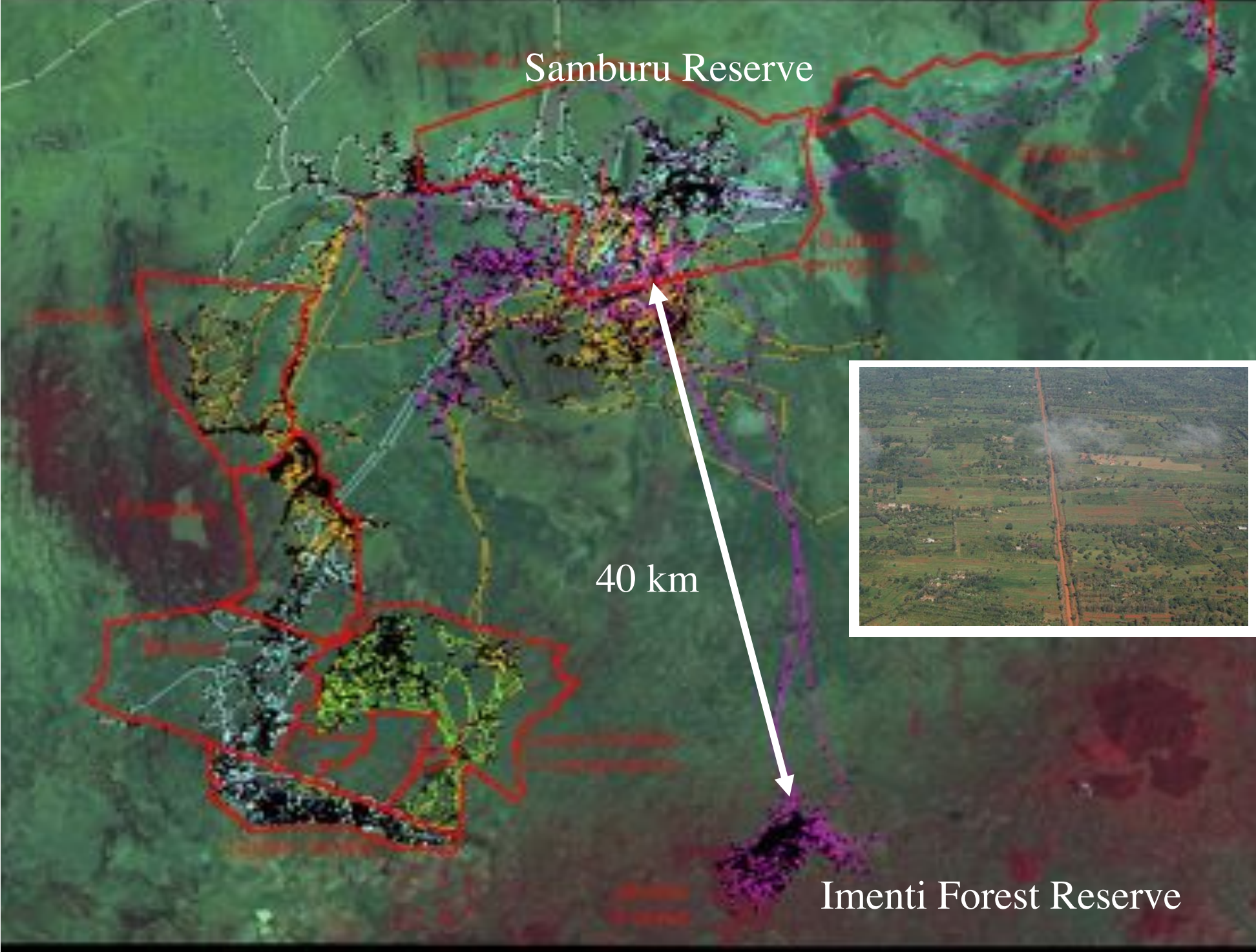


Samburu Reserve

Lewis
"streaking"

40 km

Imenti Forest Reserve

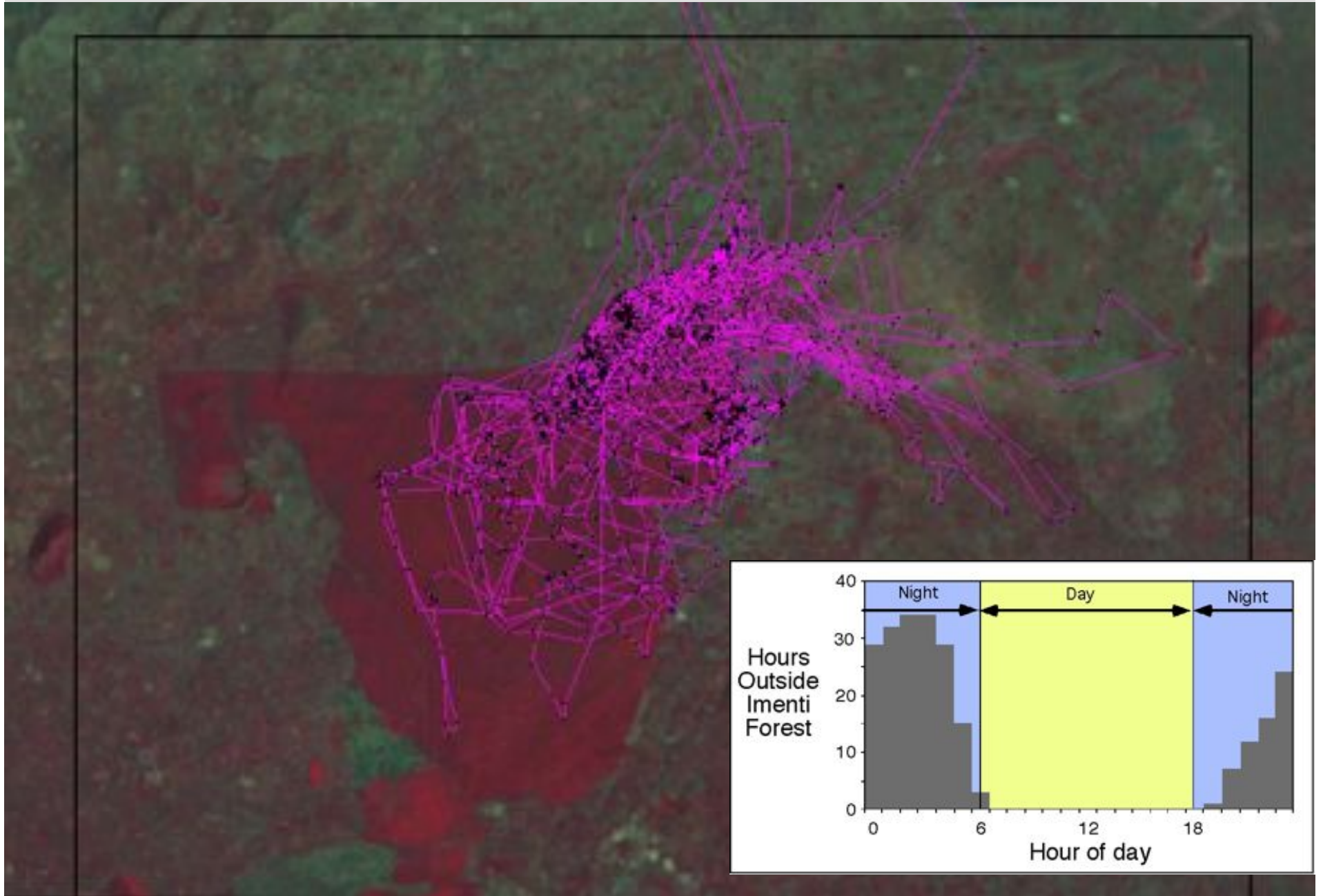


Samburu Reserve

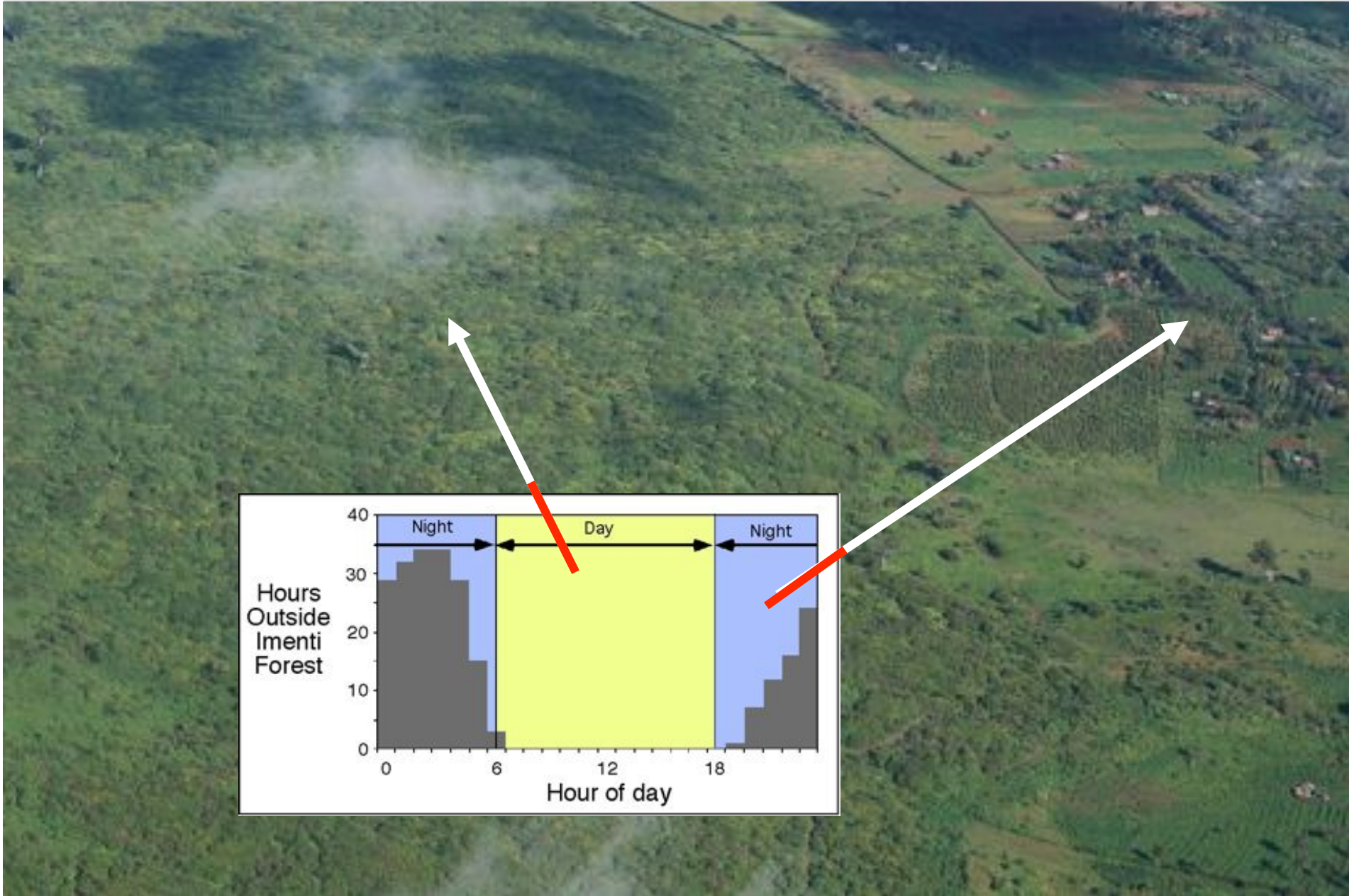
40 km

Imenti Forest Reserve

Crop raiding by Lewis occurs at night: outside the Imenti Forest

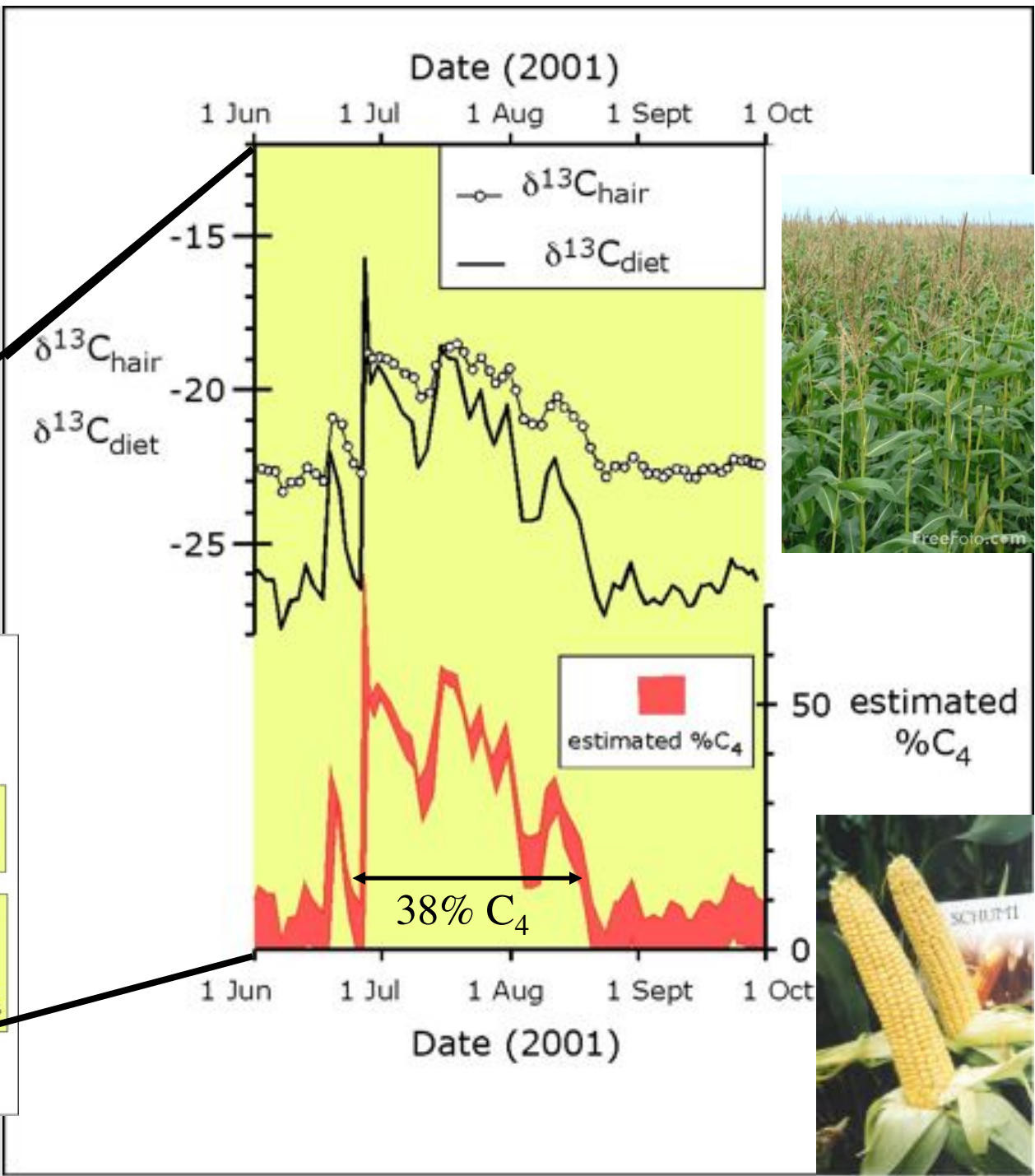
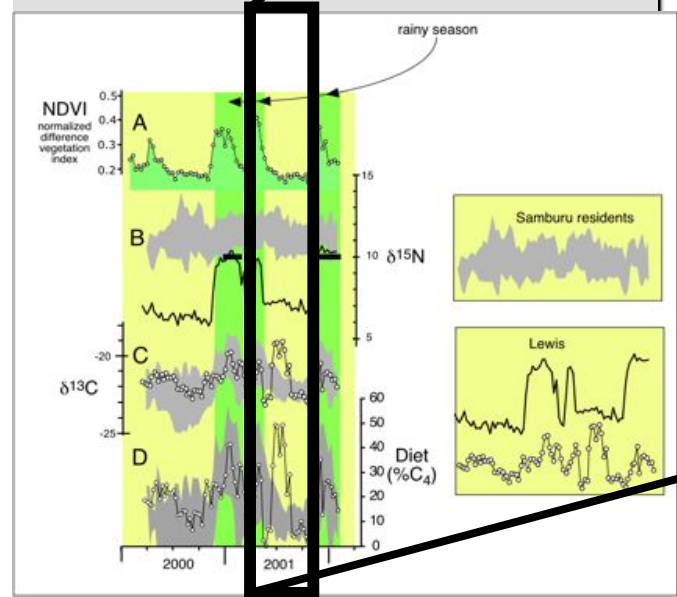


Crop raiding by Lewis occurs at night: outside the Imenti Forest

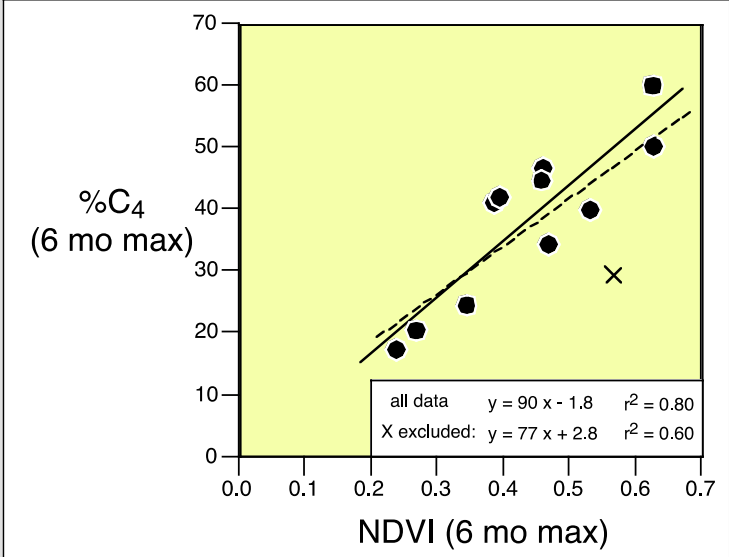
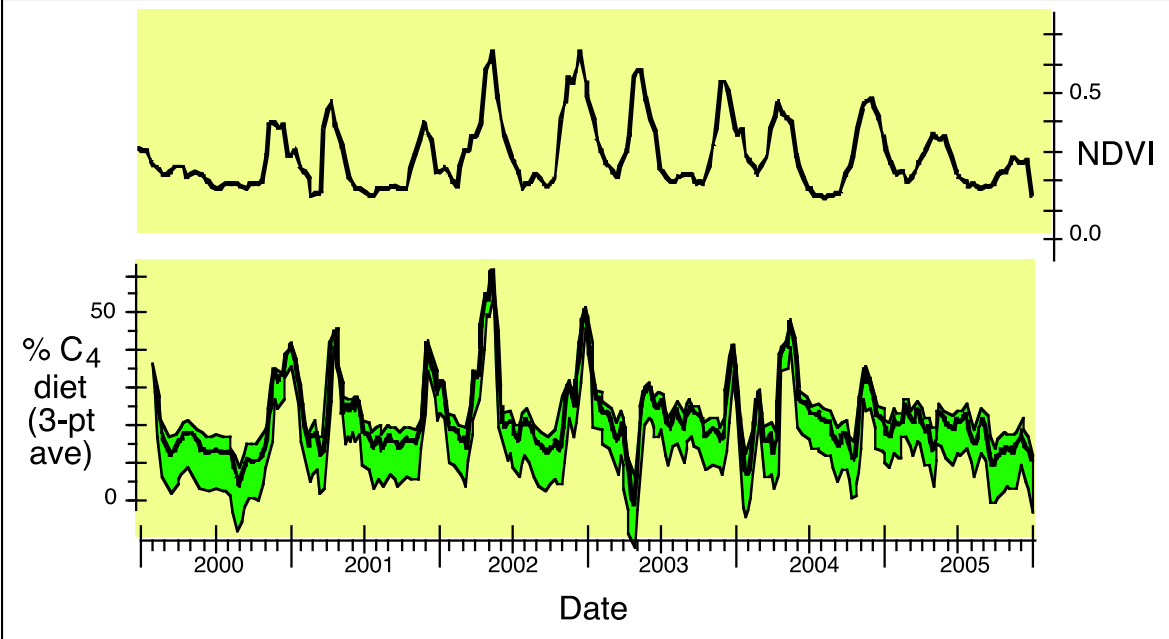


Detail of Lewis: June- Oct 2001

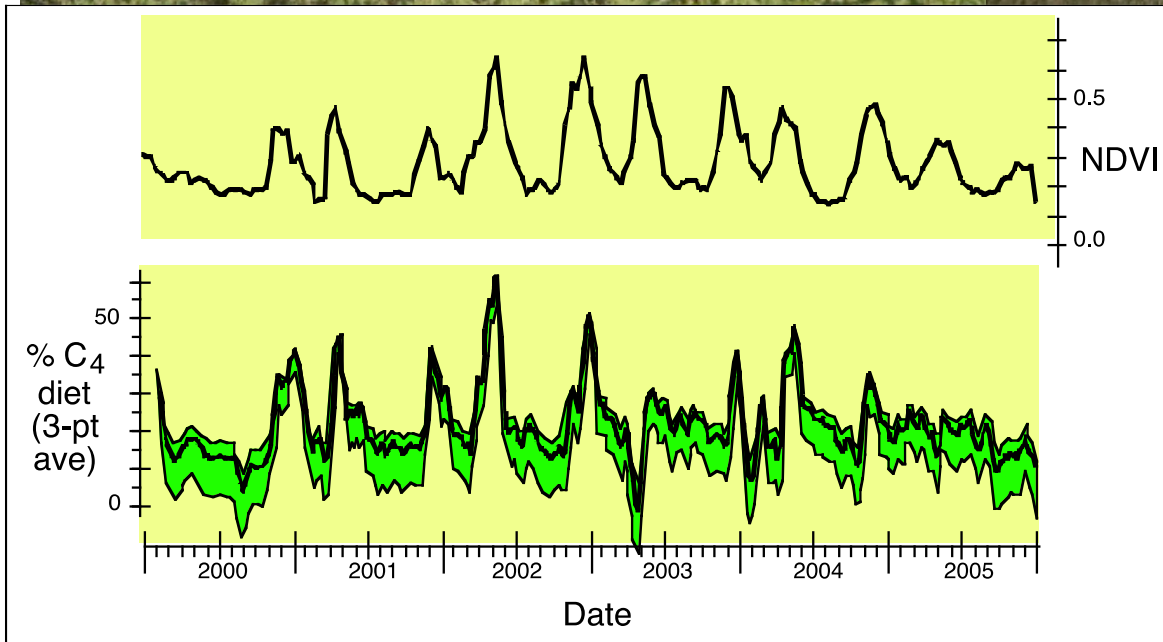
- Quantification of crop raiding



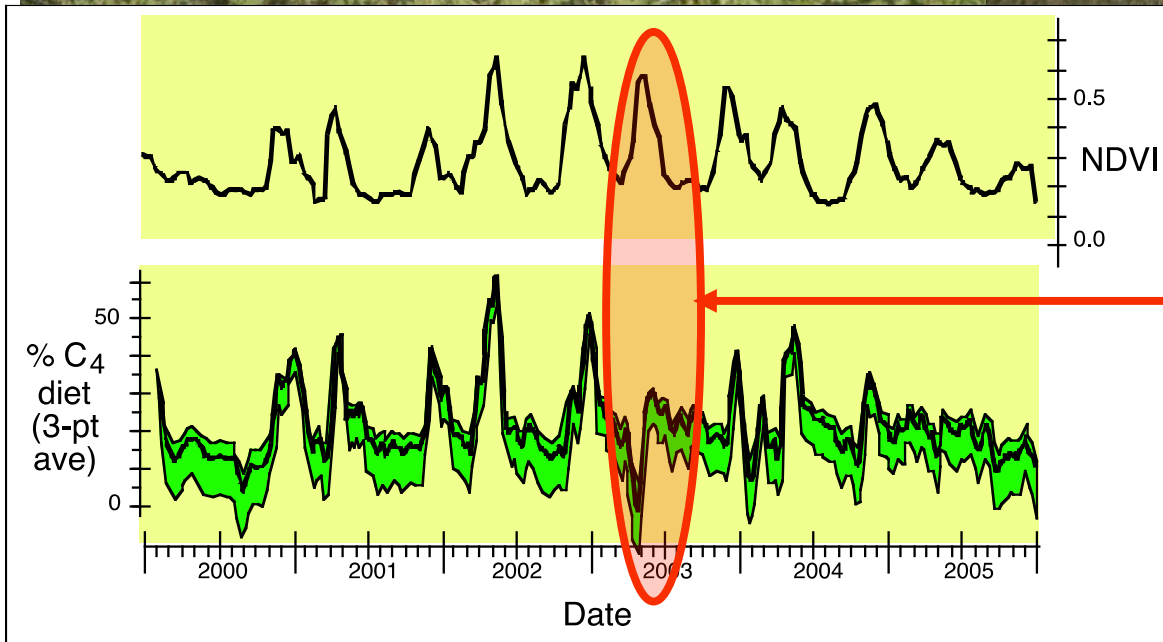
Diet, climate change, land-use change



Predicting behavior (diet)

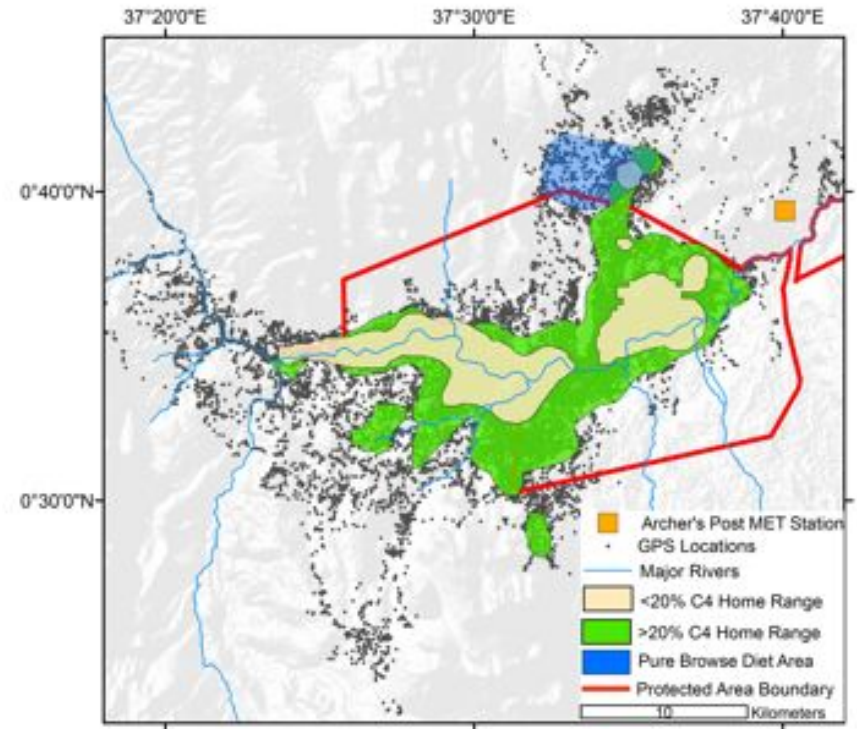


Diet, climate change, land-use change

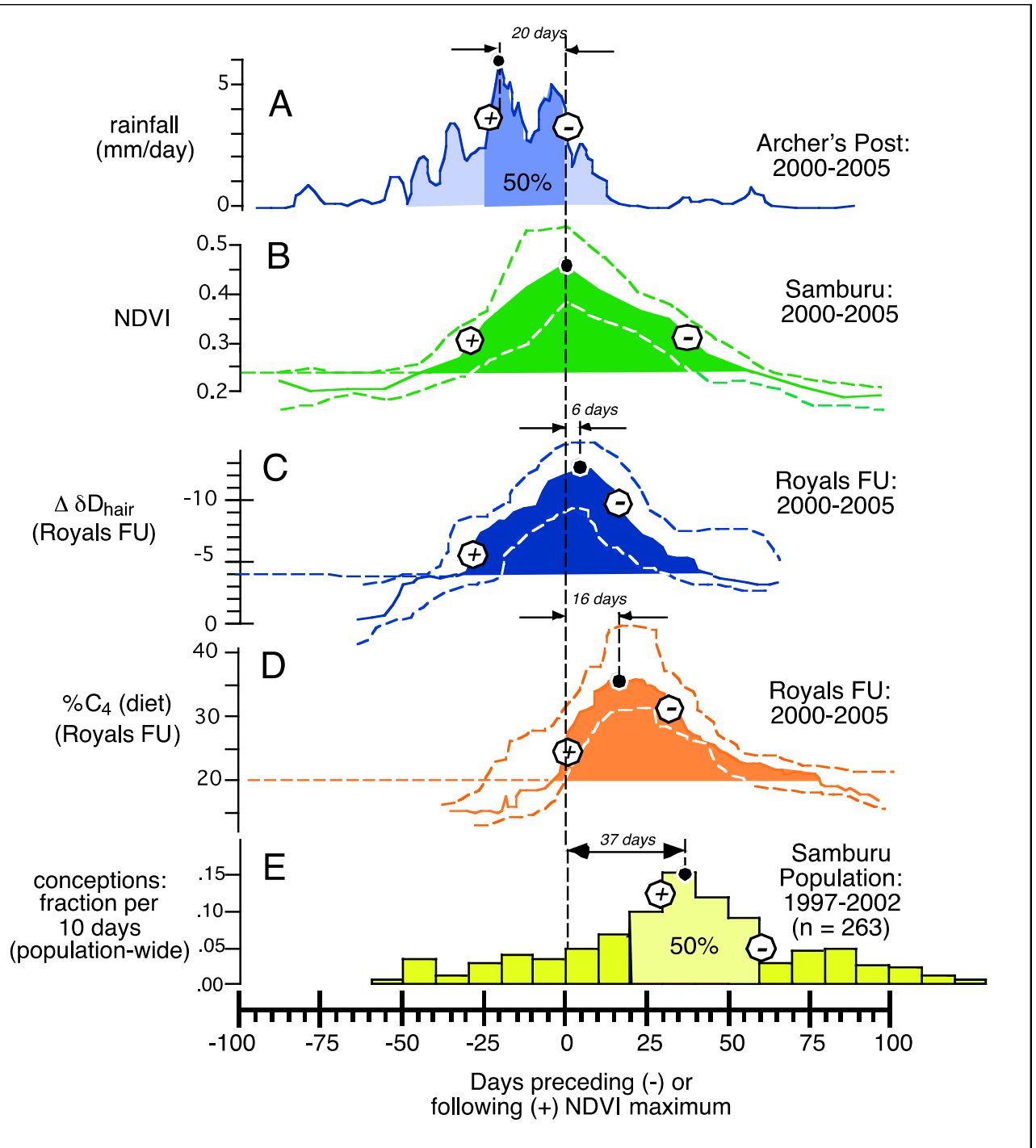


So what happened here?

GPS tracking shows they left the park and were in community lands where they cannot compete with cattle: the grass is too short!



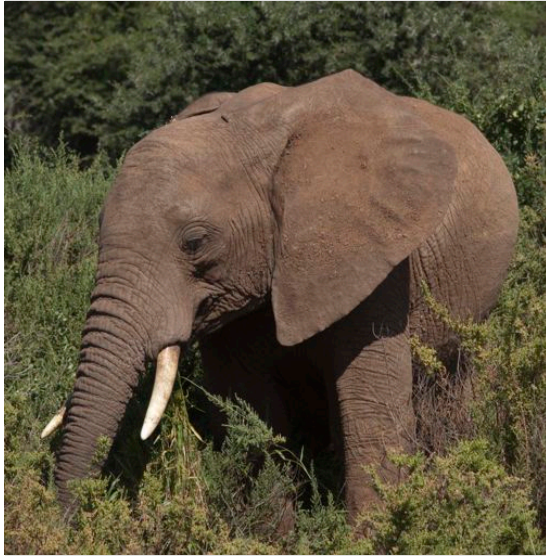
- Stable isotopes document the timing and progression of
- A. Rains
- B. Net Primary Productivity
- C. Water availability
- D. Diet
- E. Fertility responses



How do hair and ivory compare?



Other tissues? Compare hair and ivory.



- Amina: d. 27 Sept 2006
 - Tusk. 27 Sept 2006
 - Molar (M6). 27 Sept 2006
 - Hair. 27 Sept 2006; 16 June 2006; 1 Nov 2002; 4 Feb 2002; 25 Jan 2001
 - GPS. 25 Jan 2001 to 27 Sept 2006 (intermittent)

Kevin Uno, UU



Misha: d. 9 Sept 2008

- Tusk. 9 Sept 2008
- Molar. M5 and M6
- Hair. None
- Travel. Moved from Vallejo CA to Salt Lake City UT 22 April 2005



Elephant ivory:
longitudinal section

July 2004

milling striations

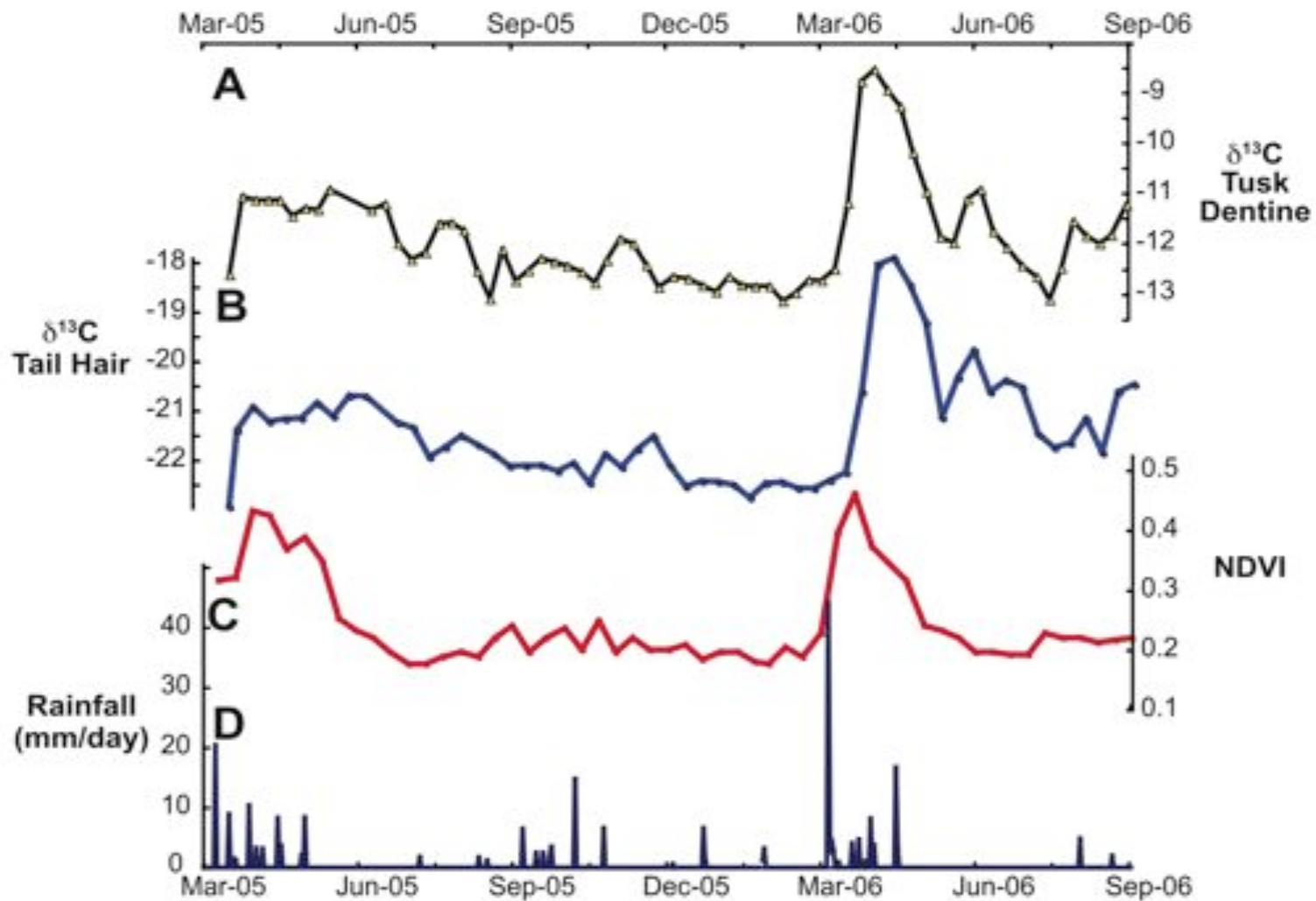
growth laminations

1000 microns

Jan 2005

Kevin Uno, UU

Amina:
d. 27 Sept 2006



Kevin Uno, UU

How do you
collect collect
elephant hair?



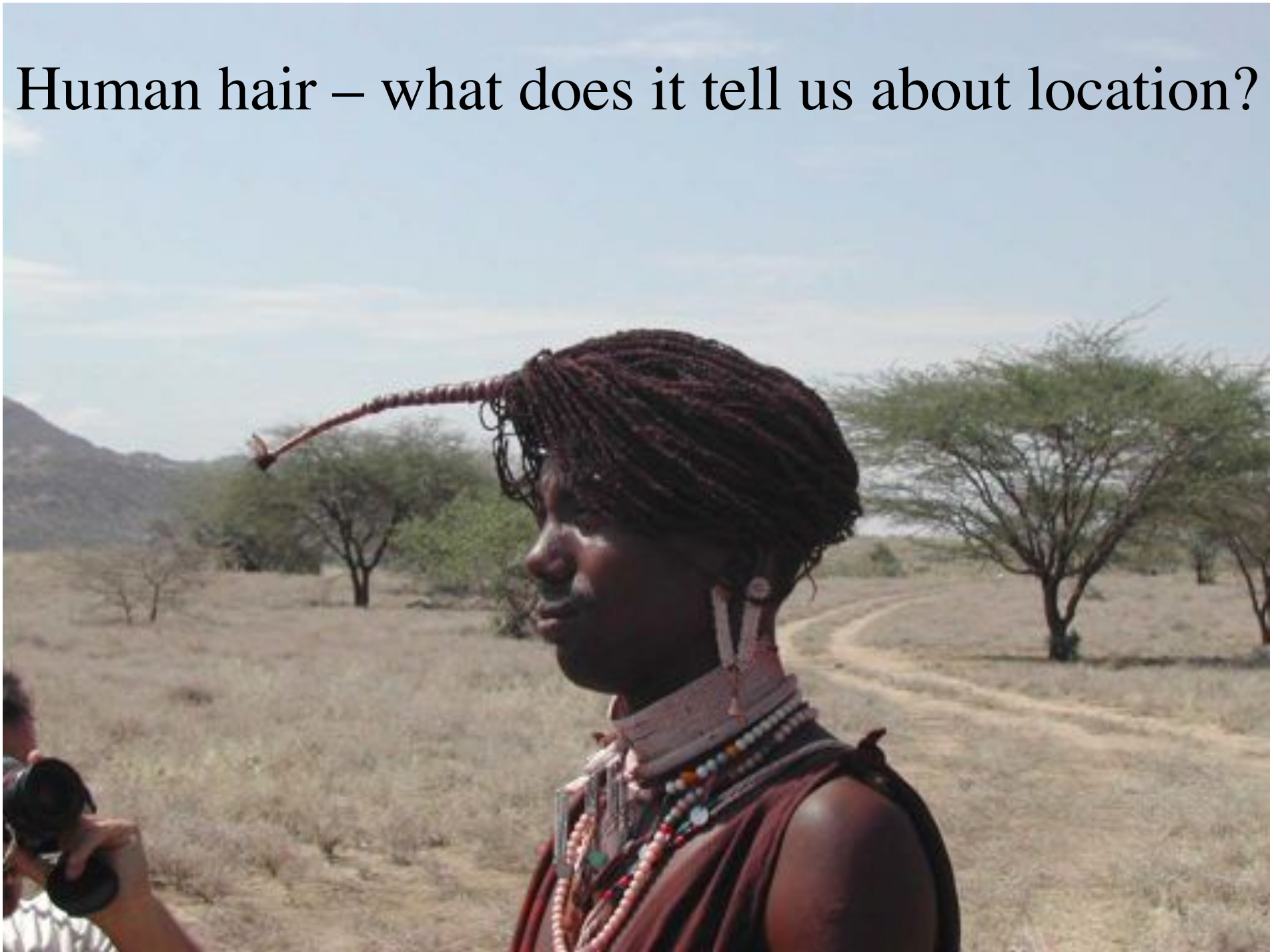
*5 tons vs. 1½ ton
("curb" weights)*

"Rommel"

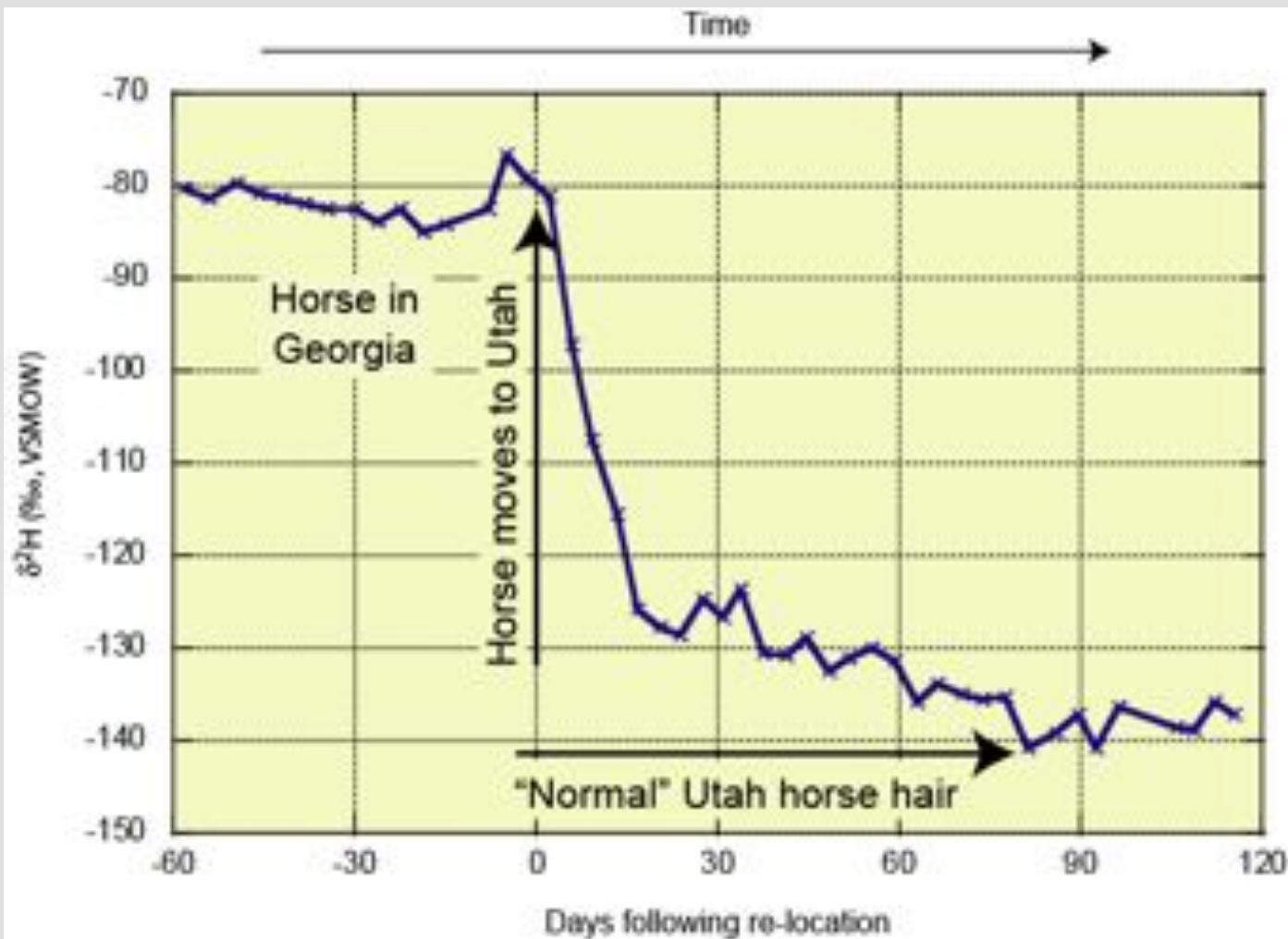


George Wittemyer's
truck

Human hair – what does it tell us about location?

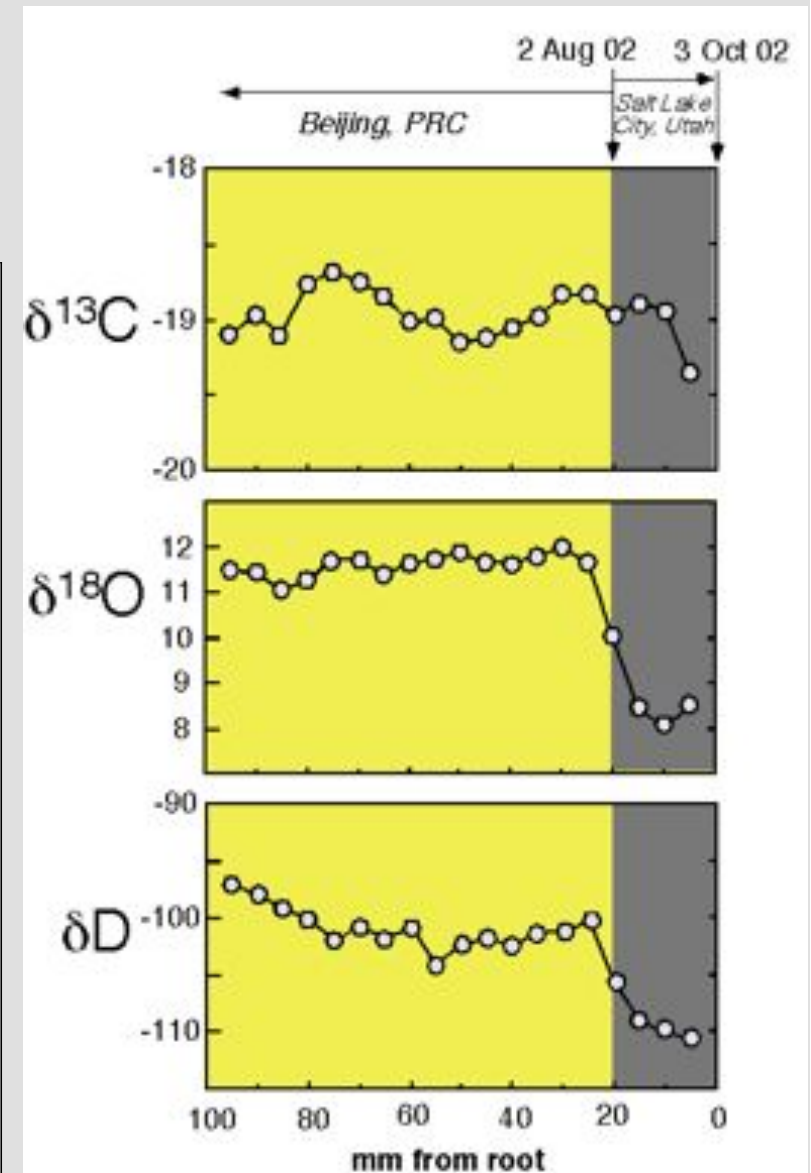
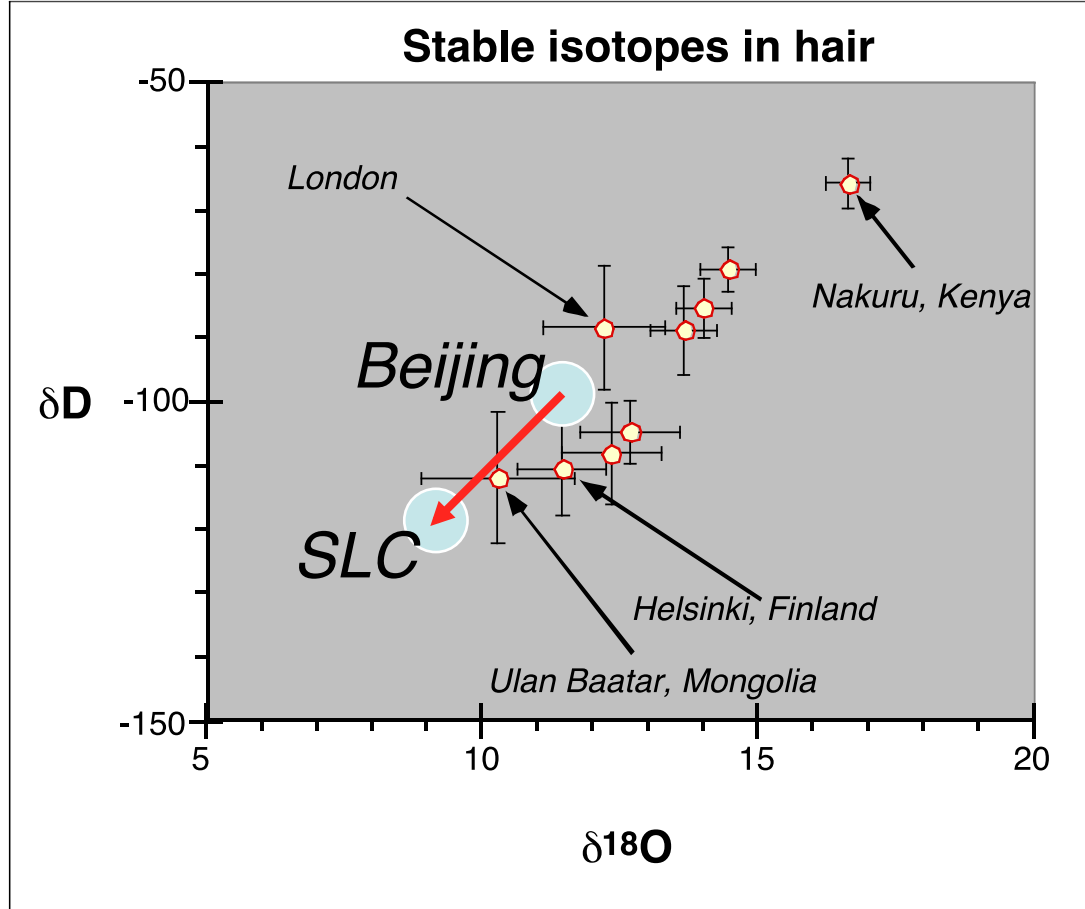


What is response to change in location?



Change in location recorded in a single hair. (Beijing to Salt Lake City).

- Residents of different cities have characteristic isotope ratios in their hair

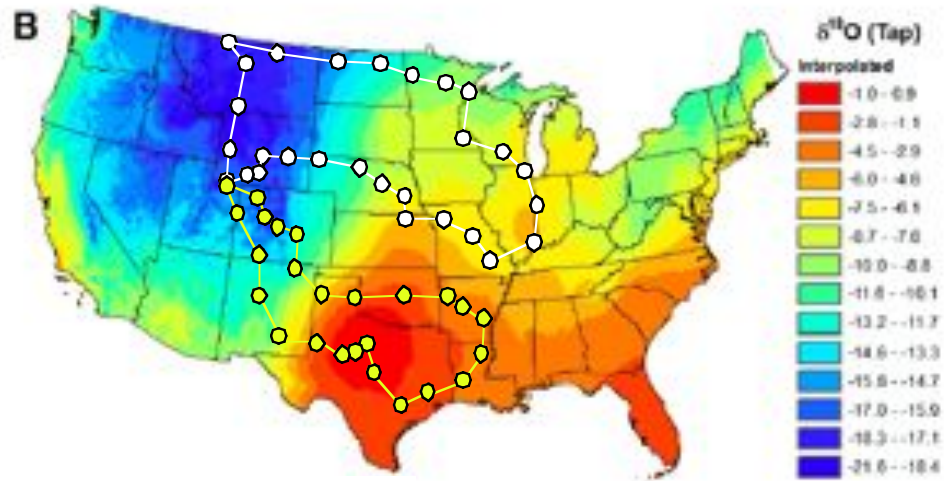


USA Tap Water Map $\delta^{18}\text{O}$, Bowen et al., 2007



Tap water “isoscape”
based on > 1000
municipal water
supplies

USA Tap Water Map $\delta^{18}\text{O}$, Bowen et al., 2007



Tap water “isoscape”
based on > 1000
municipal water
supplies

Differences in the
naturally occurring stable
isotopes of water are
“inherited” by local
people in their hair

Dylan Cerling



Claire Cerling



Edna Ehleringer

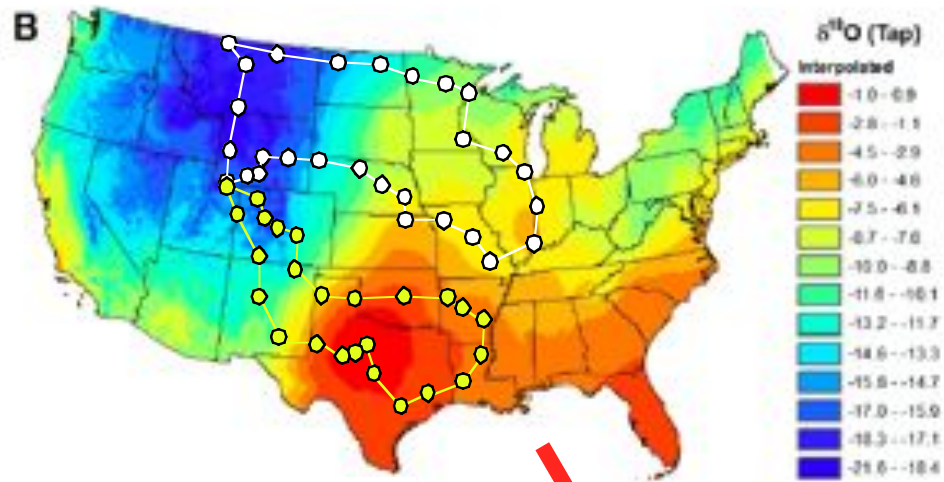




Photos by Claire Cerling

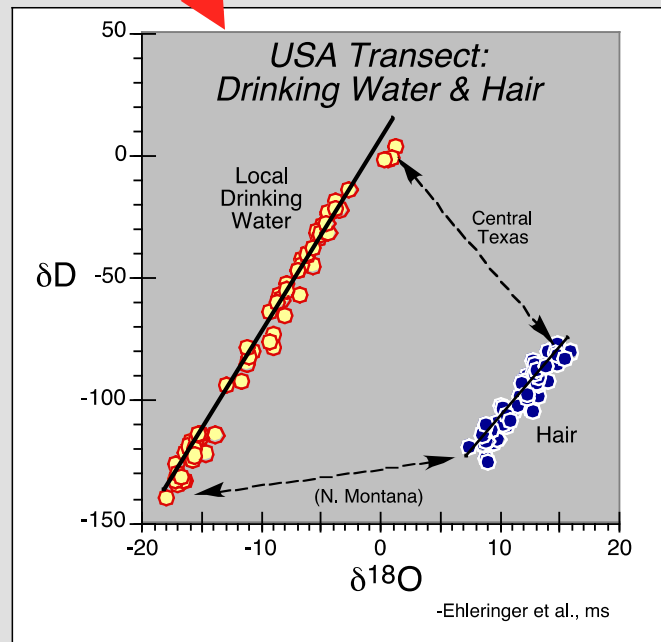


USA Tap Water Map $\delta^{18}\text{O}$, Bowen et al., 2007

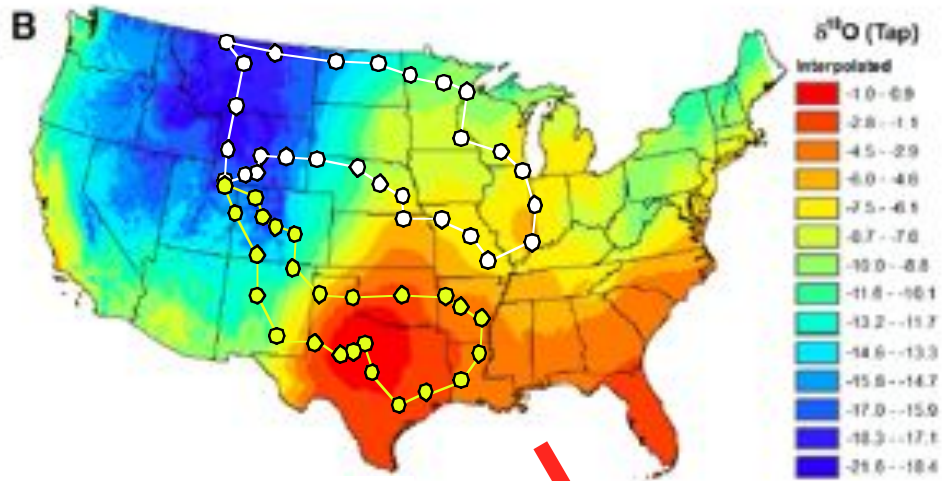


Differences in the naturally occurring stable isotopes of water are “inherited” by local people in their hair

Tap water “isoscape” based on > 1000 municipal water supplies

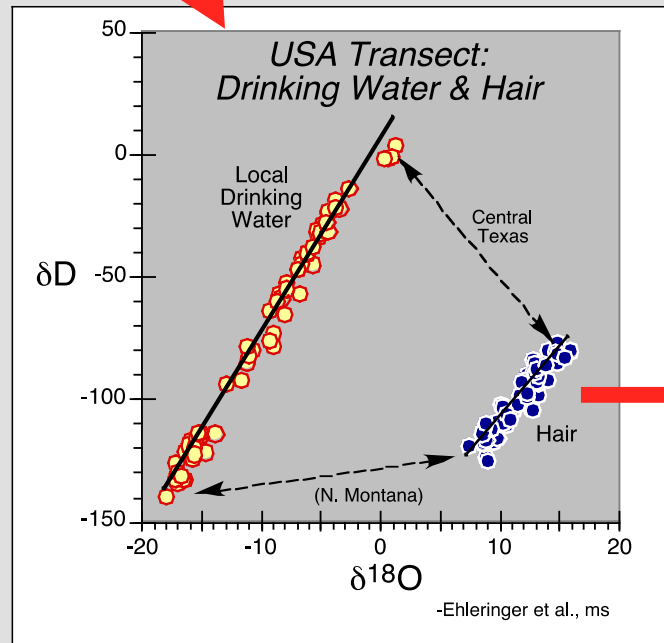


USA Tap Water Map $\delta^{18}\text{O}$, Bowen et al., 2007

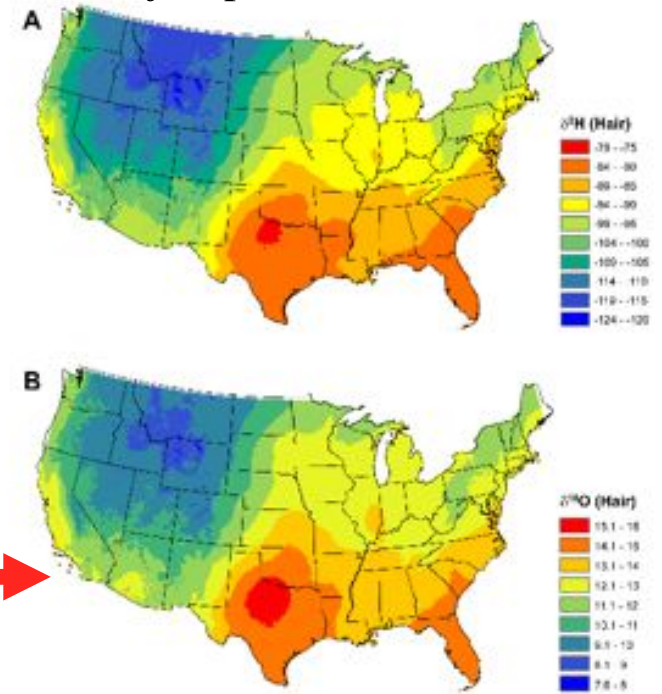


Differences in the naturally occurring stable isotopes of water are “inherited” by local people in their hair

Tap water “isoscape” based on > 1000 municipal water supplies



Human hair maps for provenance



-Ehleringer et al., 2008

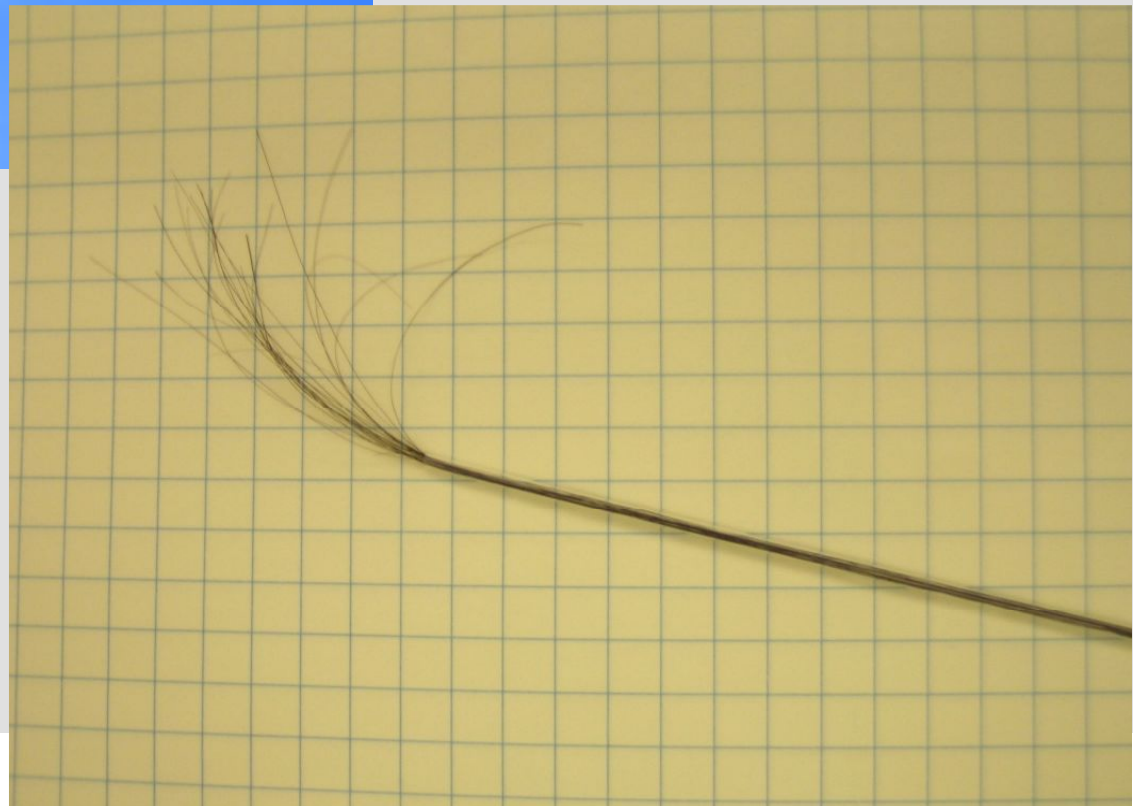


“Saltaire Sally”



A local “cold case”

*Hair, skull, some
bones were found
near Saltaire, Utah*



Bundling of hair: increases resolution by increasing sample amount

Decreasing resolution by “averaging” samples with different growth rates and in different stages of growth (anagen versus catagen-telogen).

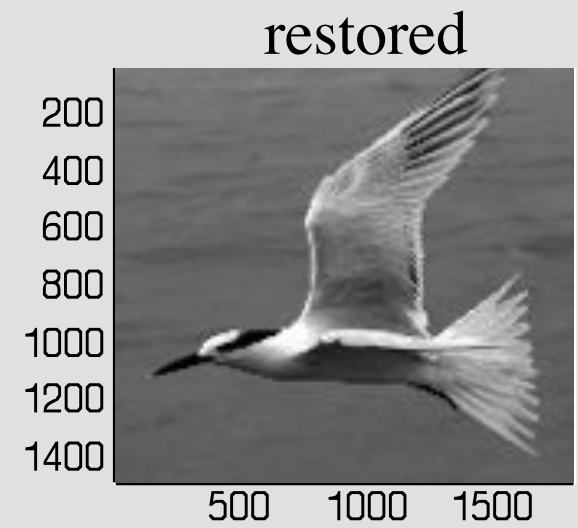
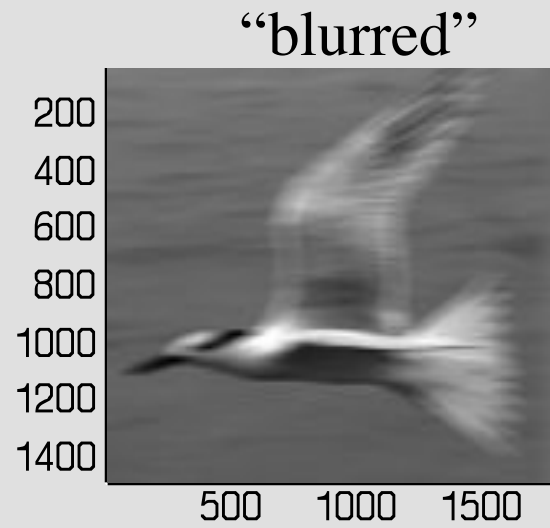
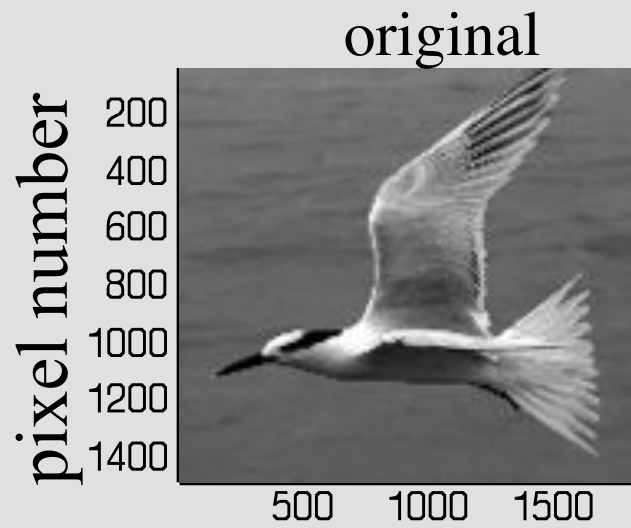
Growth rates (*ca.* 1 cm per month) in humans varies by *ca.* $\pm 10\%$

Approximately 10% of hairs are in “resting stage”.

Model that follows:

90% anagen stage 60 ± 6 months

10% catagen-telogen 6 ± 1 months



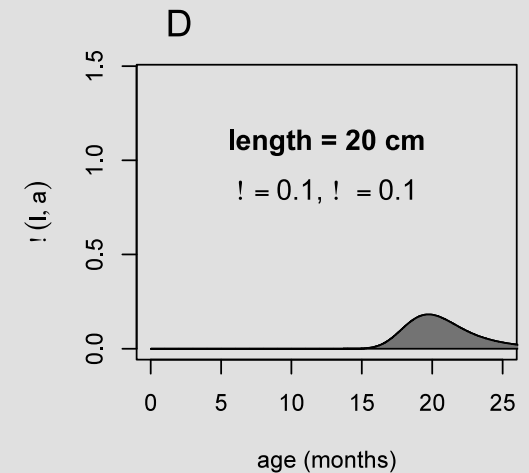
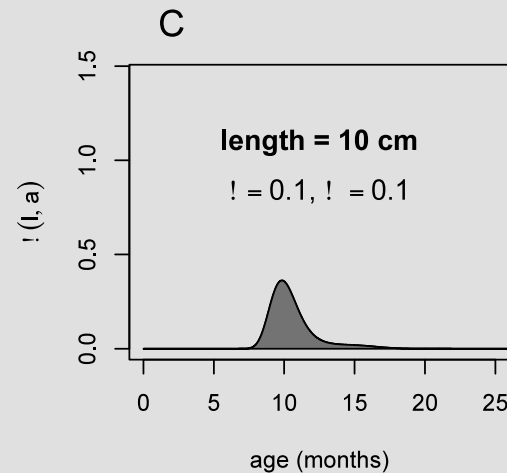
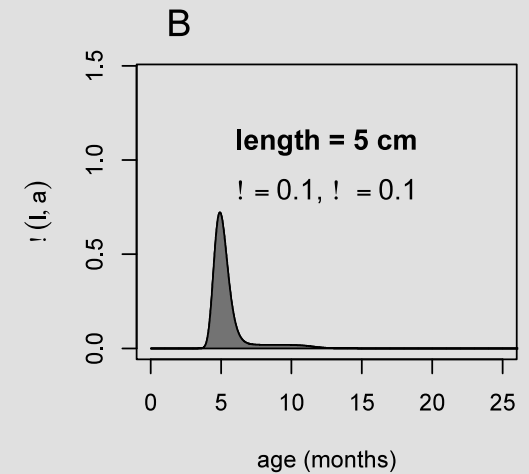
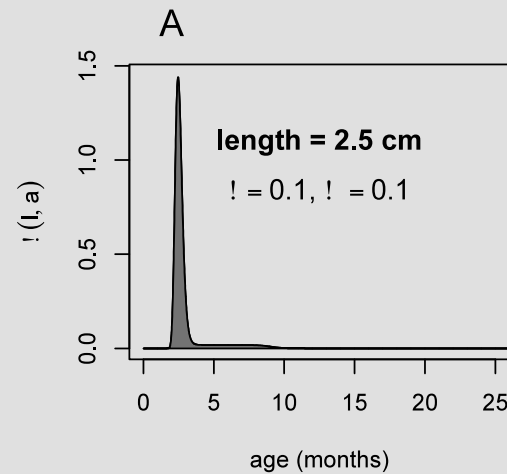
100-pt boxcar smoothing

-Menke, 2012



Hair Bundling (Remien thesis)

- Multiple hairs
- Gaussian distribution of growth rates and phases
- Signal increasingly “blurred” with increasing time

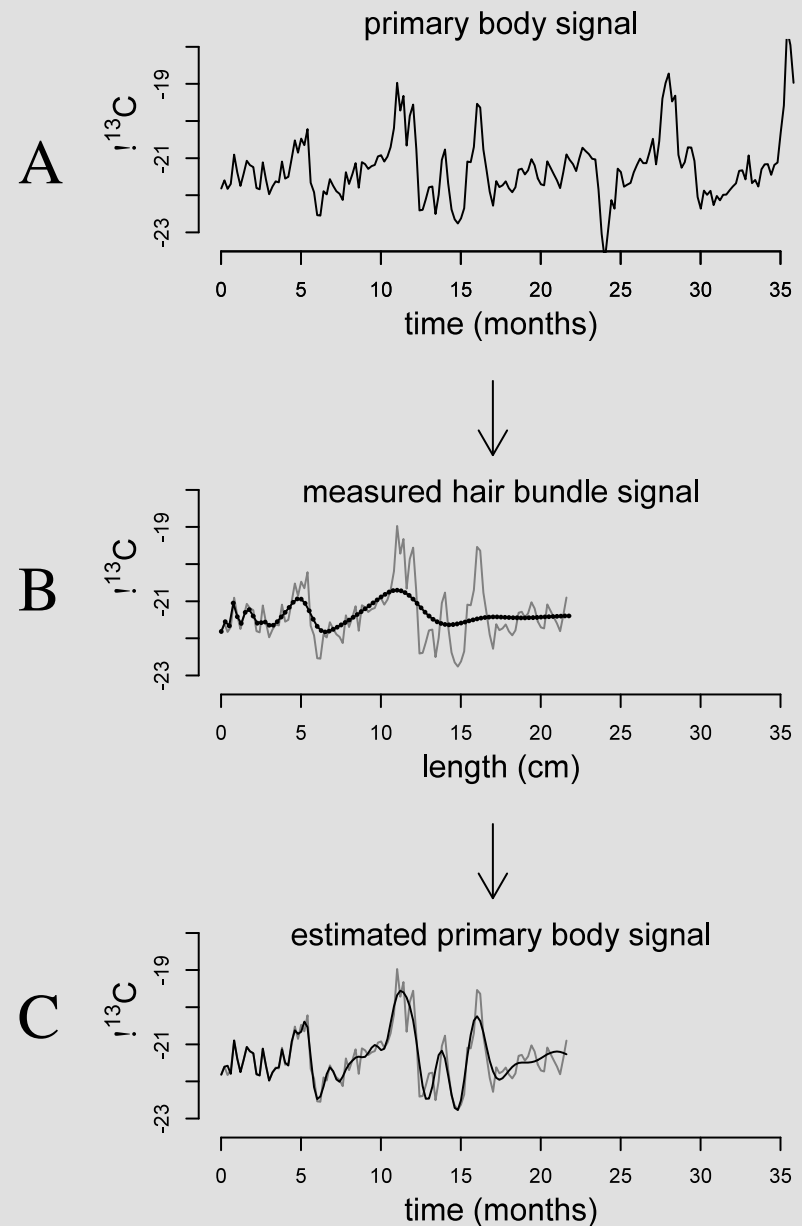


Signal recovered with inversion methods

but high frequency information can be lost

Example. high resolution record of elephant hair (ca. 3 years)

- A. Original
- B. Modeled: assume 10% growth rate variation
- C. Deconvolution using inverse methods



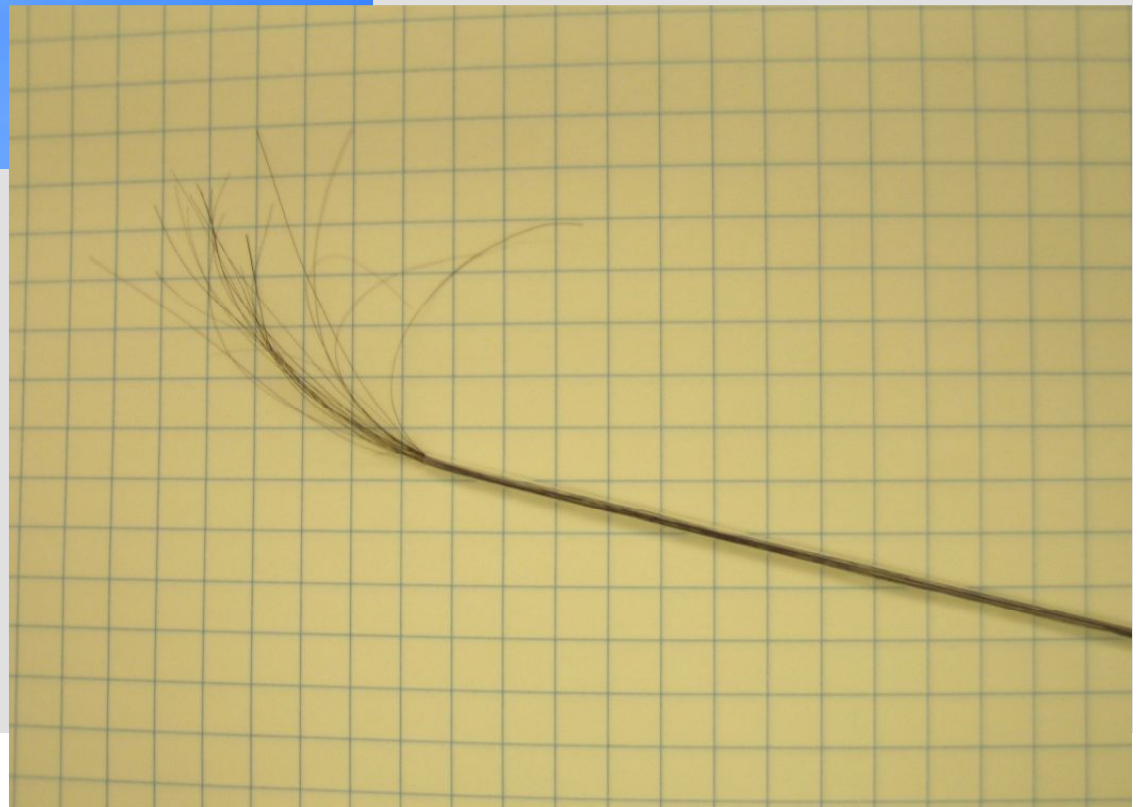


“Saltaire Sally”

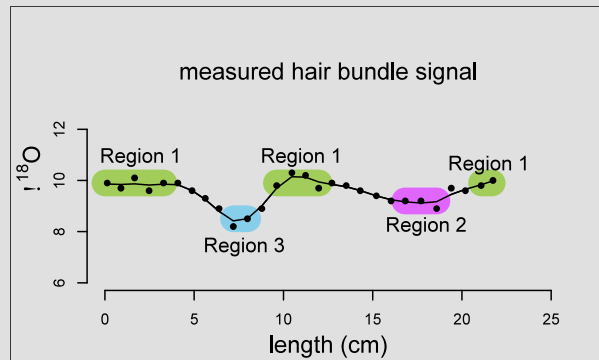


A local “cold case”

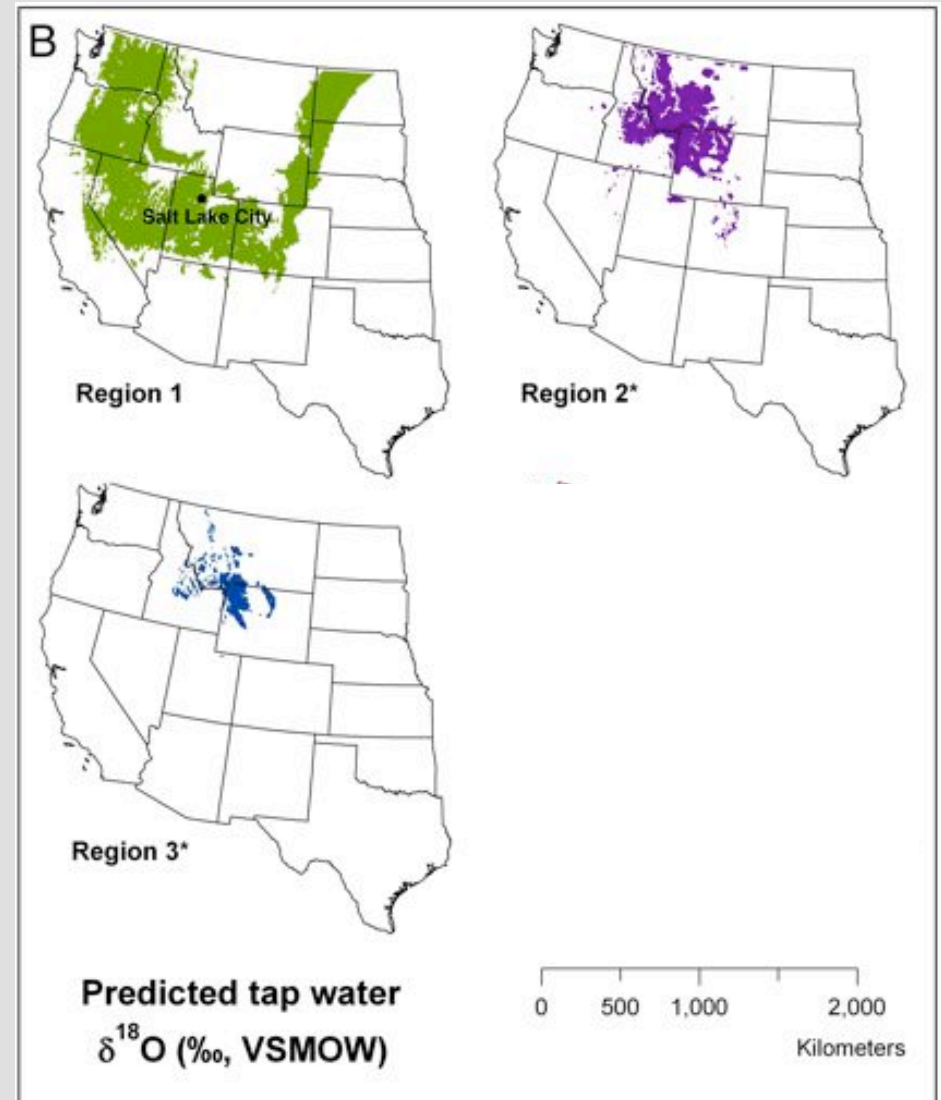
*Hair, skull, some
bones were found
near Saltaire, Utah*



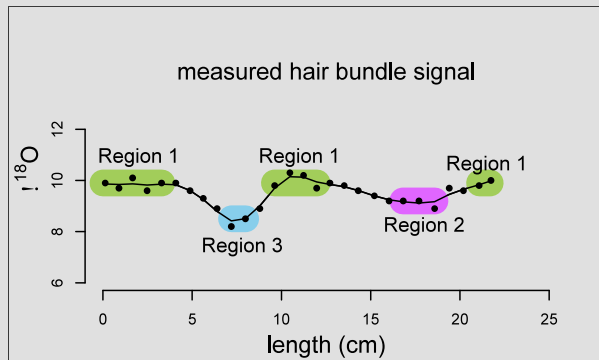
Inversion and non-steady state suggests new search region for murder victim



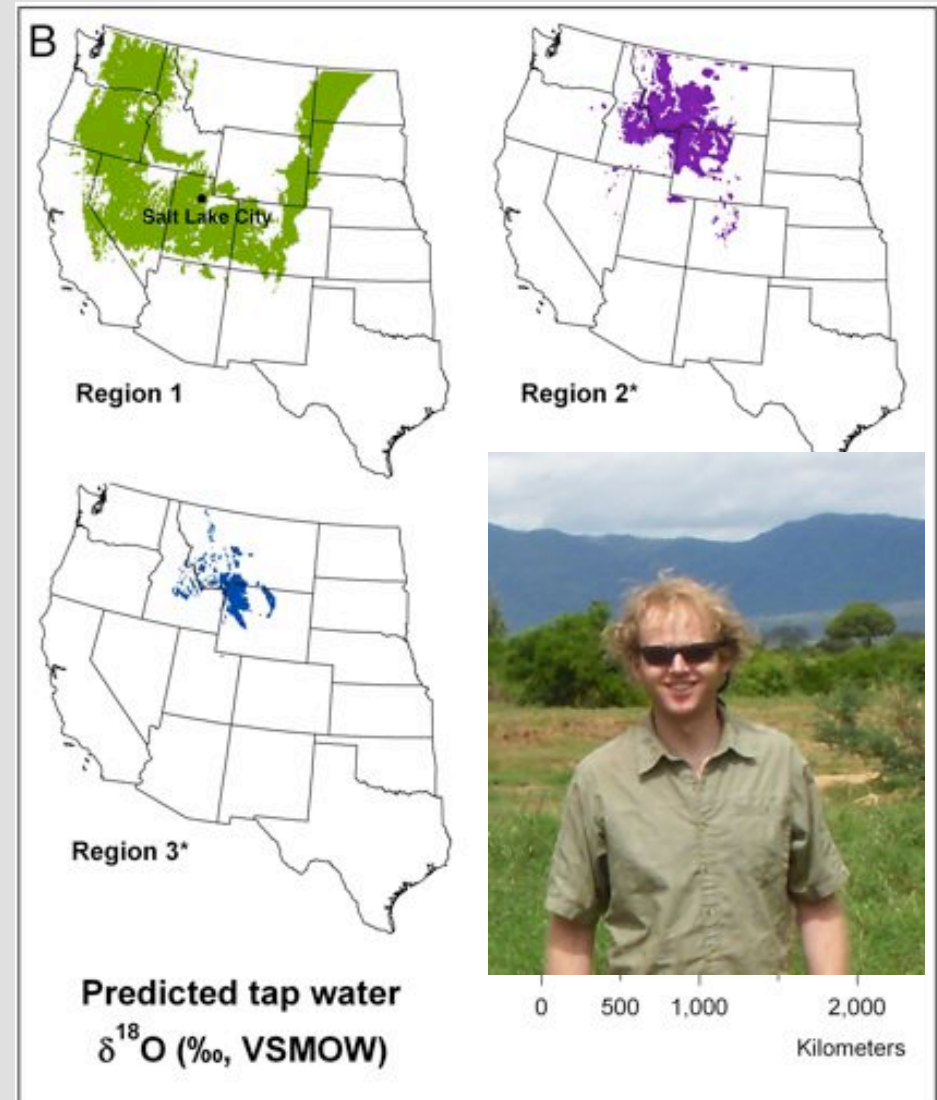
Original interpretation:
Travel in N-S direction,
about every 6 months



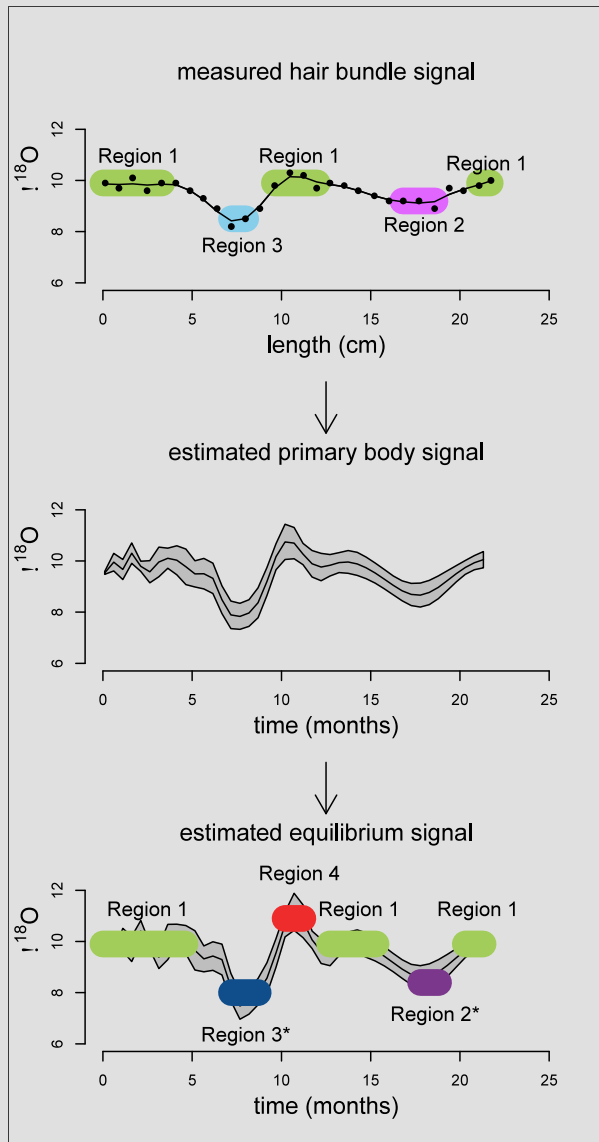
Inversion and non-steady state suggests new search region for murder victim



Original interpretation:
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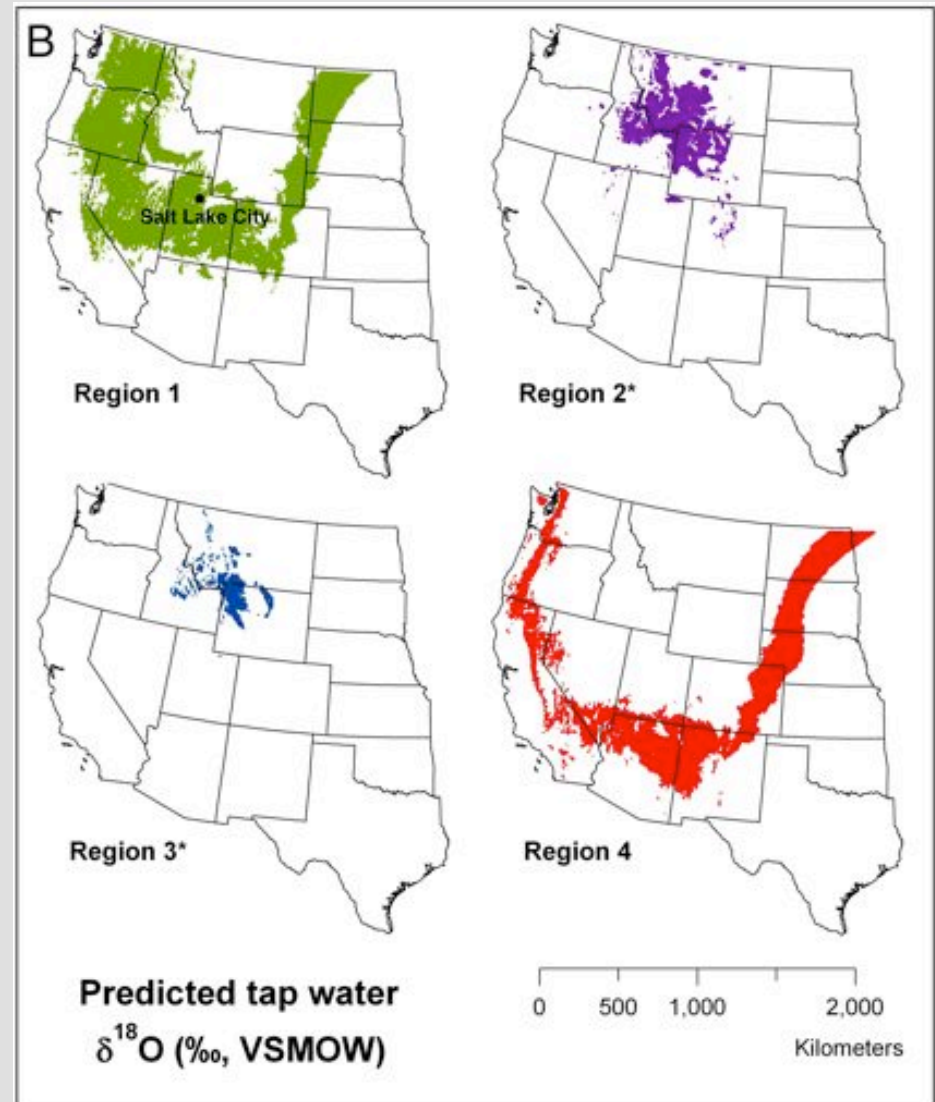


Inversion and non-steady state suggests new search region for murder victim



1. Inversion

2. Correct to "equilibrium"



Inversion and non-steady state suggests new search region for murder victim

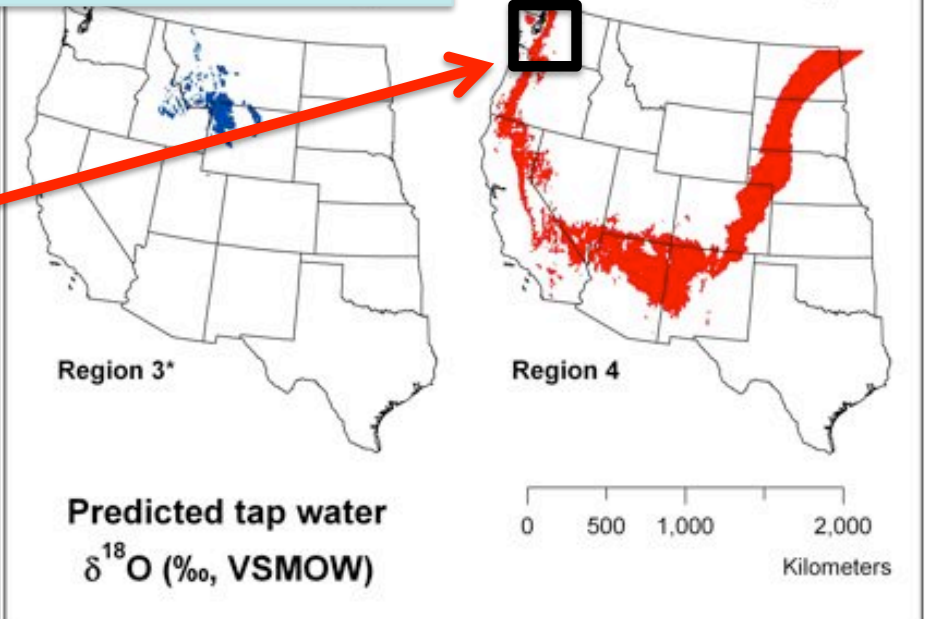
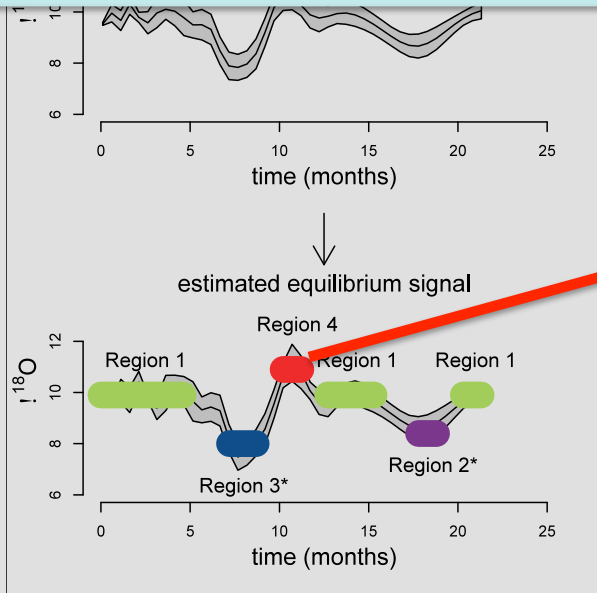
measured hair bundle signal

12-year-old mystery solved: 'Saltair Sally' ID'd

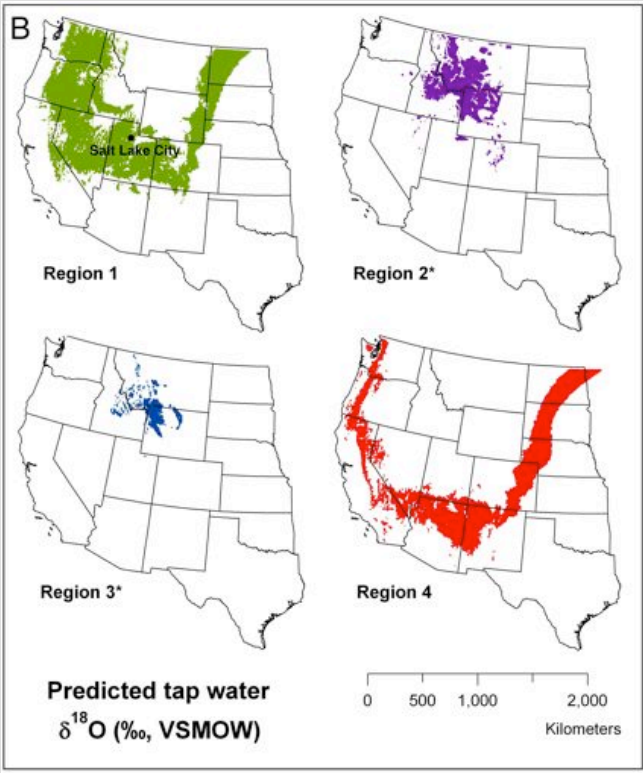
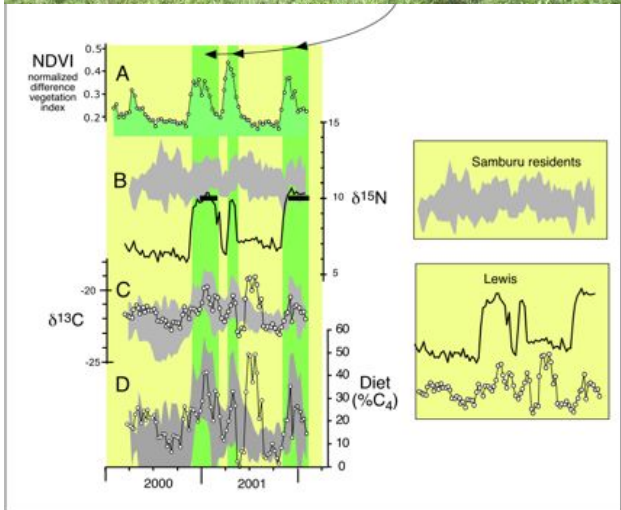
Police » DNA shows body found in '00 belonged to Nikole Bakoles; "We want to find out who" killed her, sheriff says.

By Aaron Falk And Jessica Miller | The Salt Lake Tribune
First Published Aug 07 2012 12:07 pm • Last Updated Aug 08 2012 09:32 am

South Salt Lake • They called her "Saltair Sally."

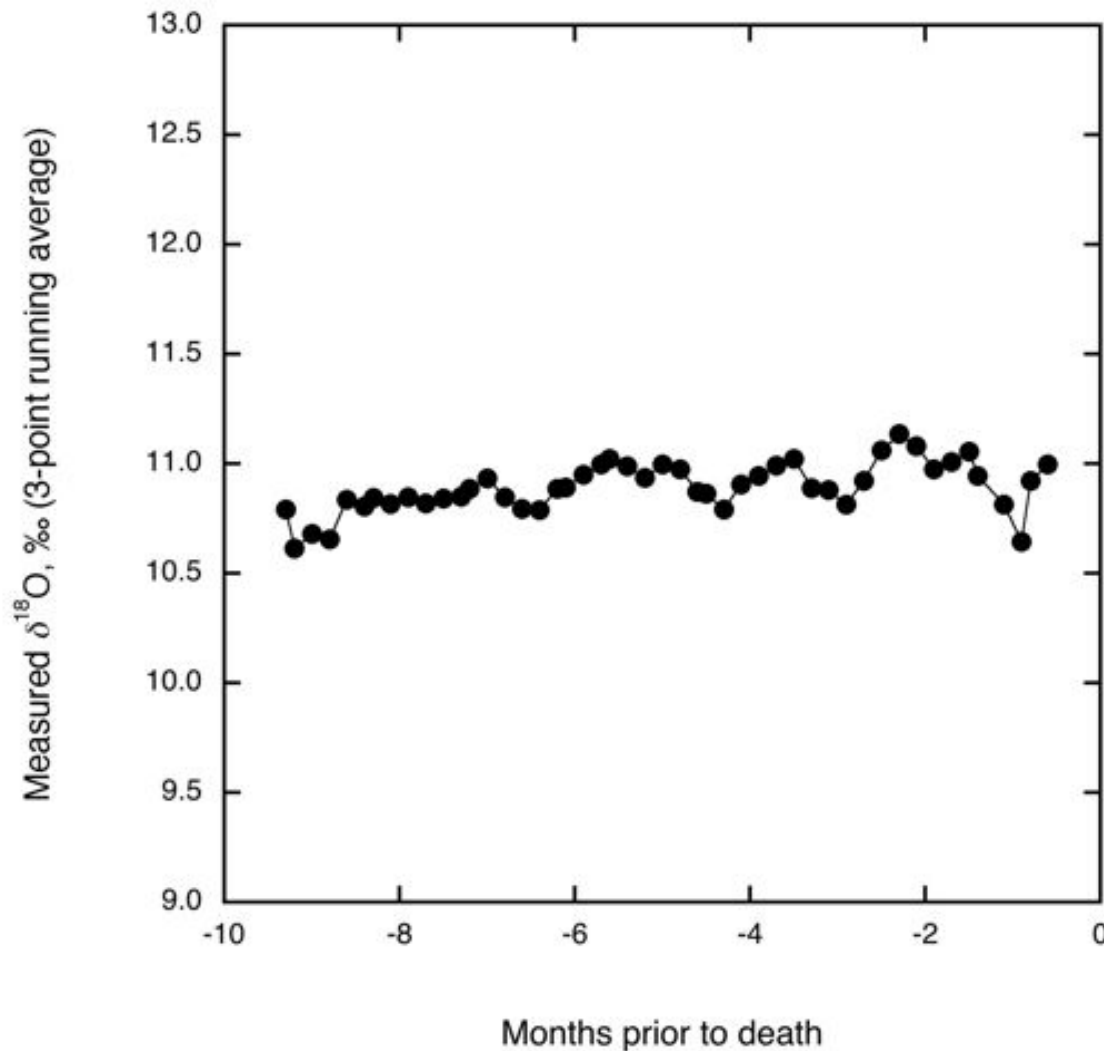


You are what you eat (+ a few ‰)



Backup

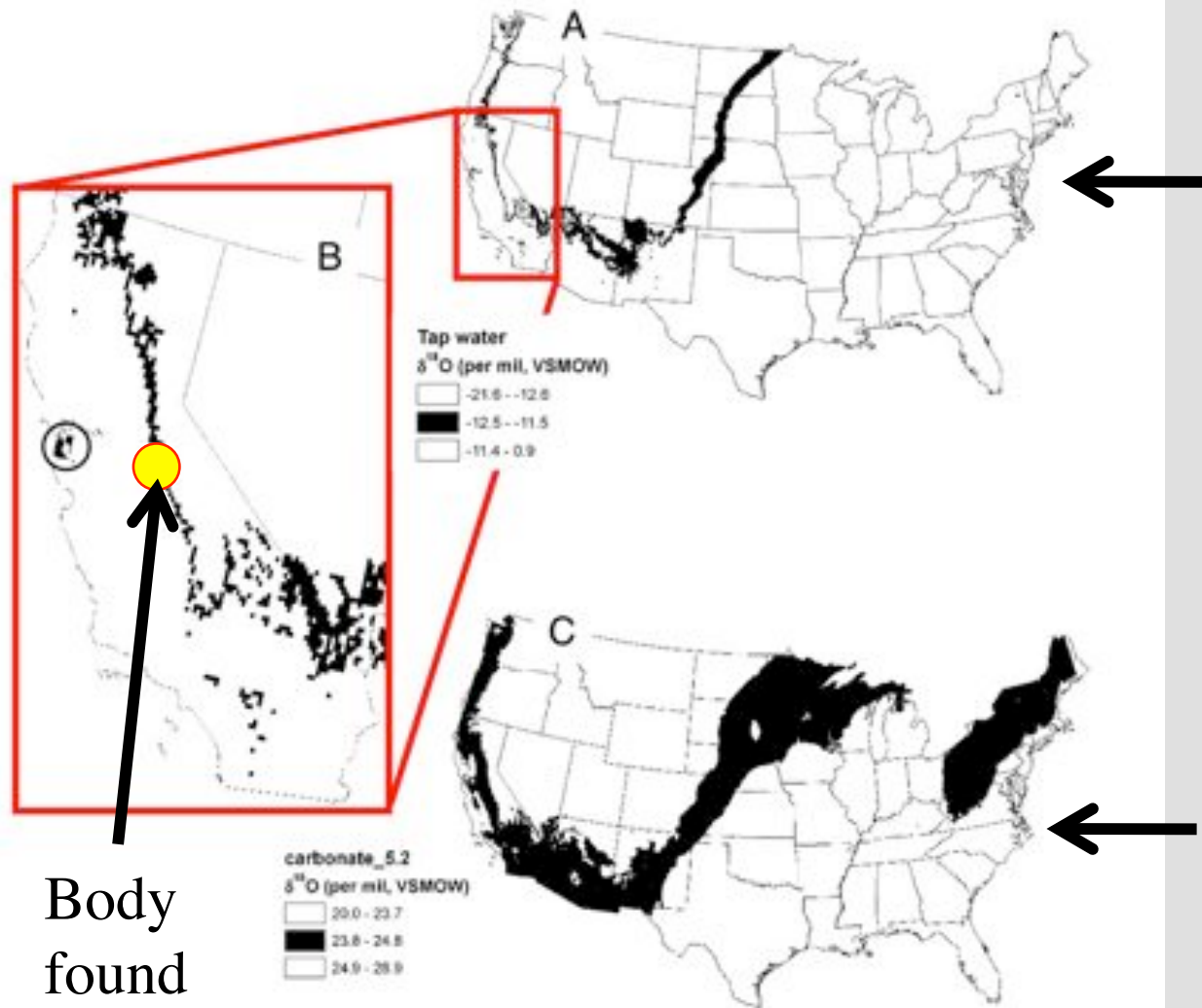
NCIS (A Cold case, re-opened in 2008)



Hair from “Jane Doe”, found in canal in Stanislaus County, CA on 11 September 1971 with 65 stab wounds.

Isotopes indicate limited travel in last year of life

Reconstructed travel history



From hair
- last year of life
- *i.e.*, 1971

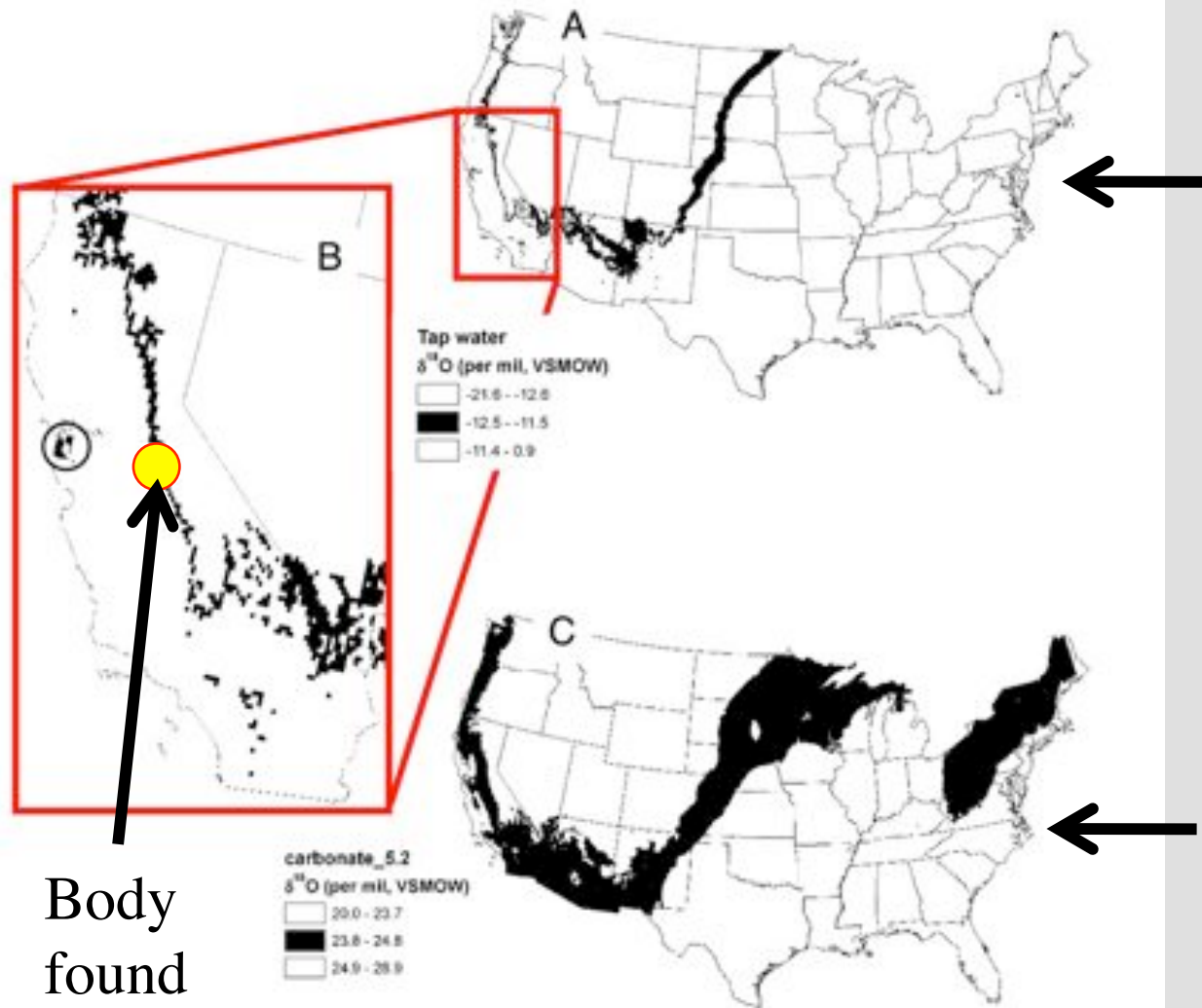
*Who was
this person?*

From teeth
- *ca.* 6 years old
- *i.e.*, 1950

Body
found

-Chesson, et al., in press

Reconstructed travel history



From hair
- last year of life
- *i.e.*, 1971

Conclusion: likely limited travel. Could be California resident

From teeth
- *ca.* 6 years old
- *i.e.*, 1950

-Chesson, et al., in press

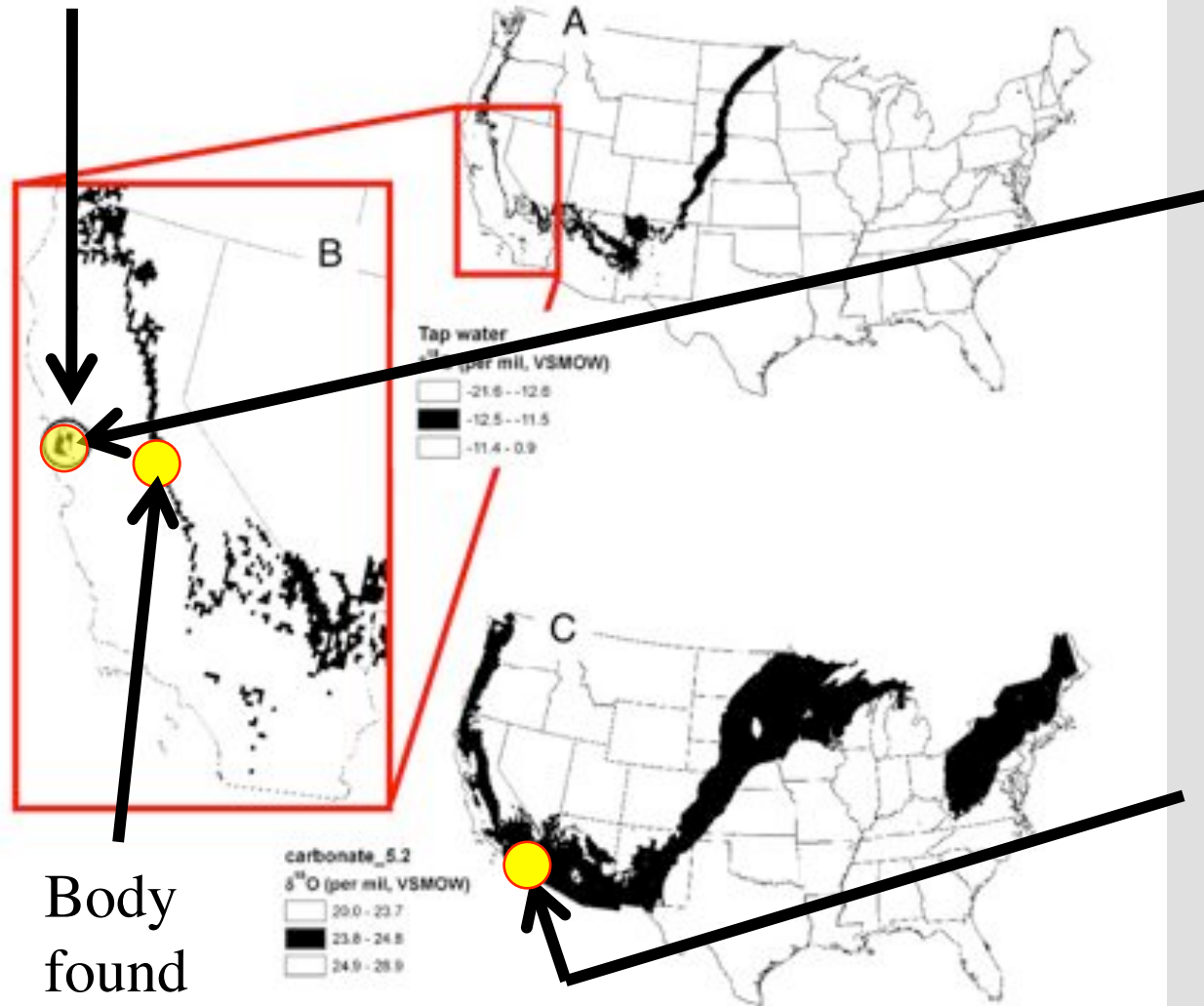
MARY ALICE WILLEY and the BLACK LIBERATION ARMY

- Mary Alice Willey was born in Anaheim, CA in 1949; she moved to San Francisco, CA in **September 1969** to attend college. She grew disillusioned with school, dropped out, and became involved in the Black Power movement. In high school she had been known as Carol.
- **21 August 1971**, she is thought to have smuggled a gun to George Jackson, a San Quentin prisoner, resulting in the killing of several prison guards and the death of Jackson during an escape attempt.
- **28 August 1971**, a woman fitting the description of Mary Alice (but who gave the name Carol George) entered a San Francisco police station to report a missing purse. After completing paperwork, she signaled to individuals outside the station, who entered and killed policemen in apparent retaliation for George Jackson's death.
- **11 September 1971**, the body of "Jane Doe" was discovered floating in a canal ditch in Stanislaus County.



Reconstructed travel history

*San Francisco
(Hetch-Hetchy
Reservoir)*



From hair
- last year of life
- *i.e.*, 1971

*Who was
this person?*

From teeth
- *ca.* 6 years old
- *i.e.*, 1950

Anaheim, CA

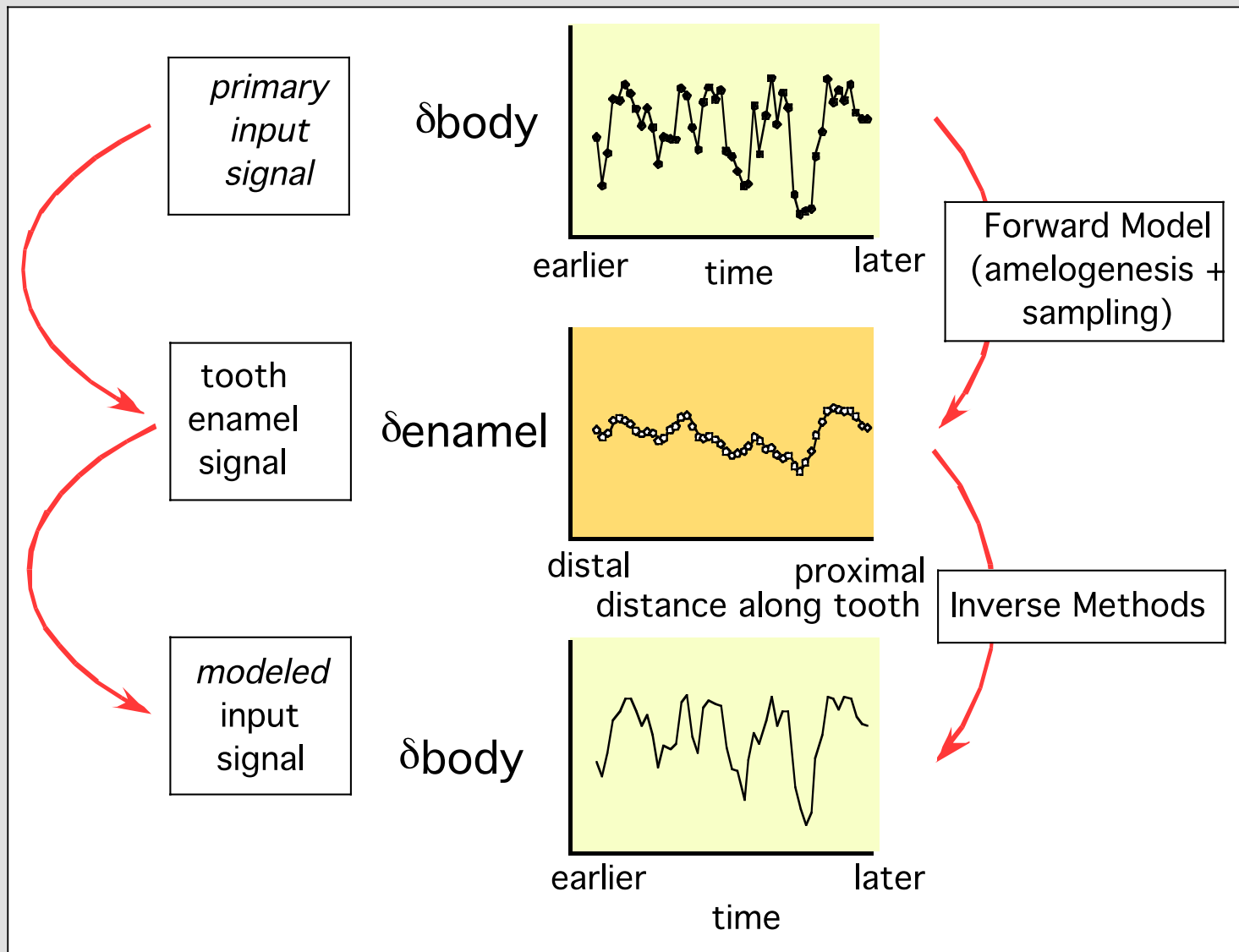
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- 11 September 1971, the body of "Jane Doe" was discovered in a canal ditch in Stanislaus County.
- *Stable isotopes used for confirmation of DNA studies.*
ID established in 2009.

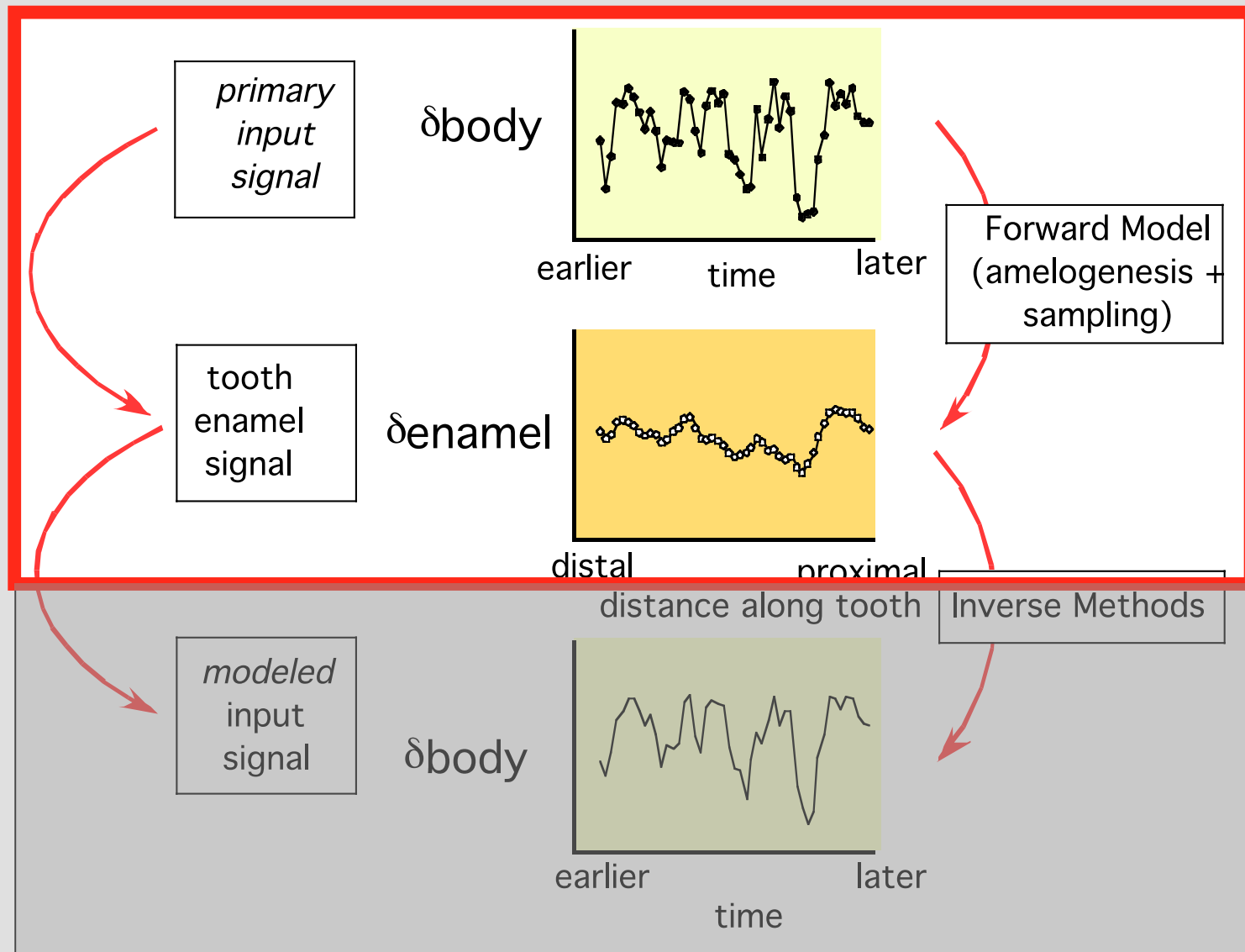


Prospects for reconstruction of diets using tooth enamel

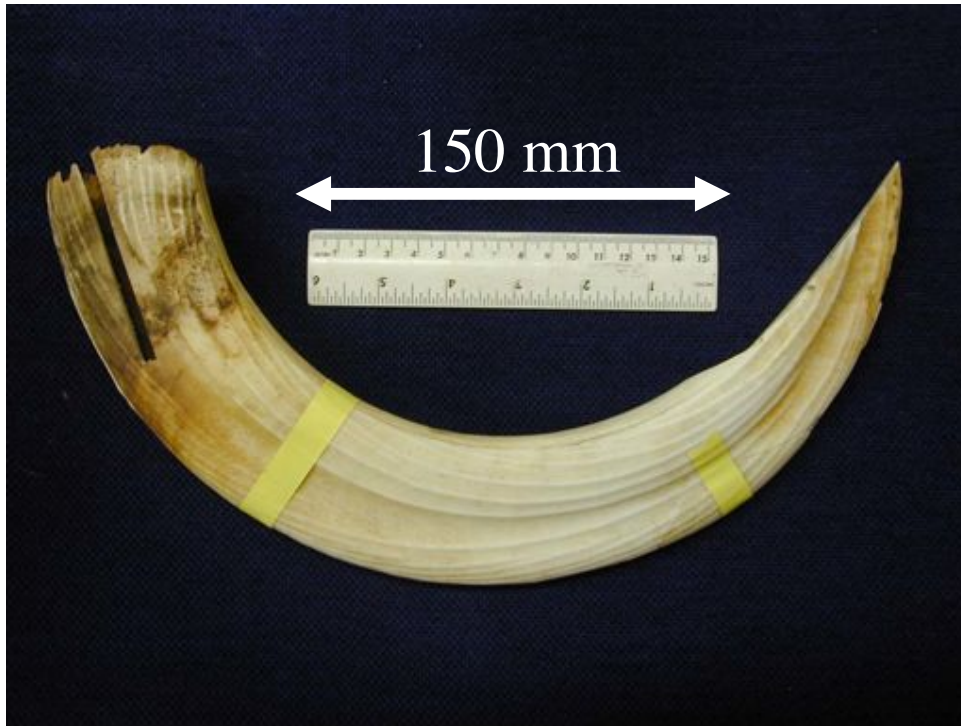
Real input vs. modeled output



Real input vs. modeled output



Enamel does not form all at once

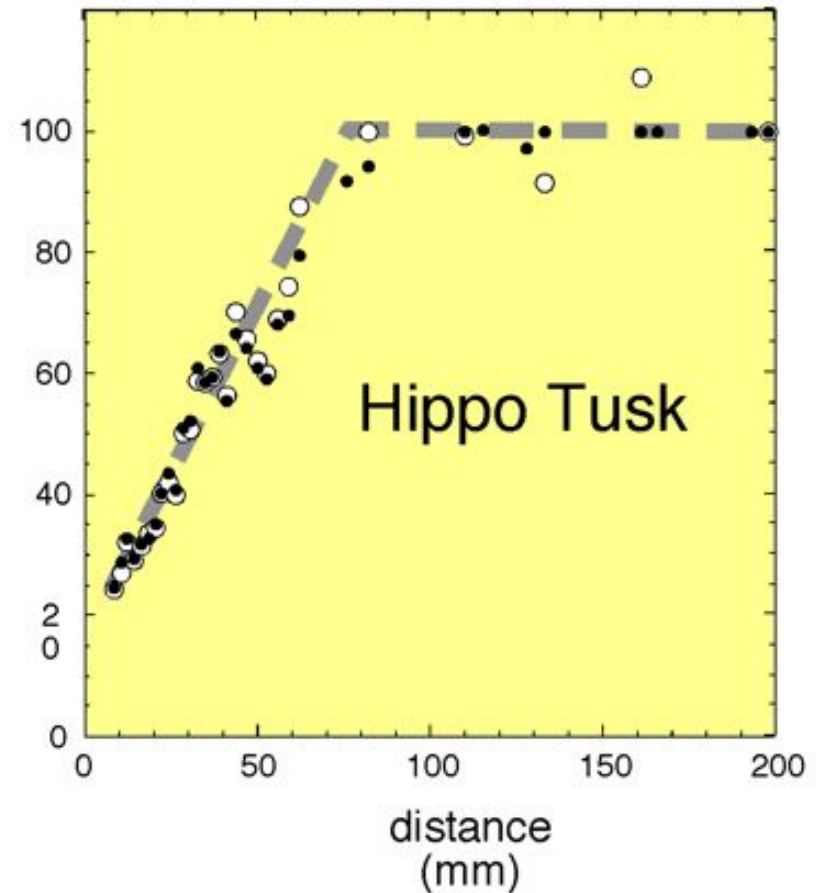


unit volume of enamel forms
over time interval

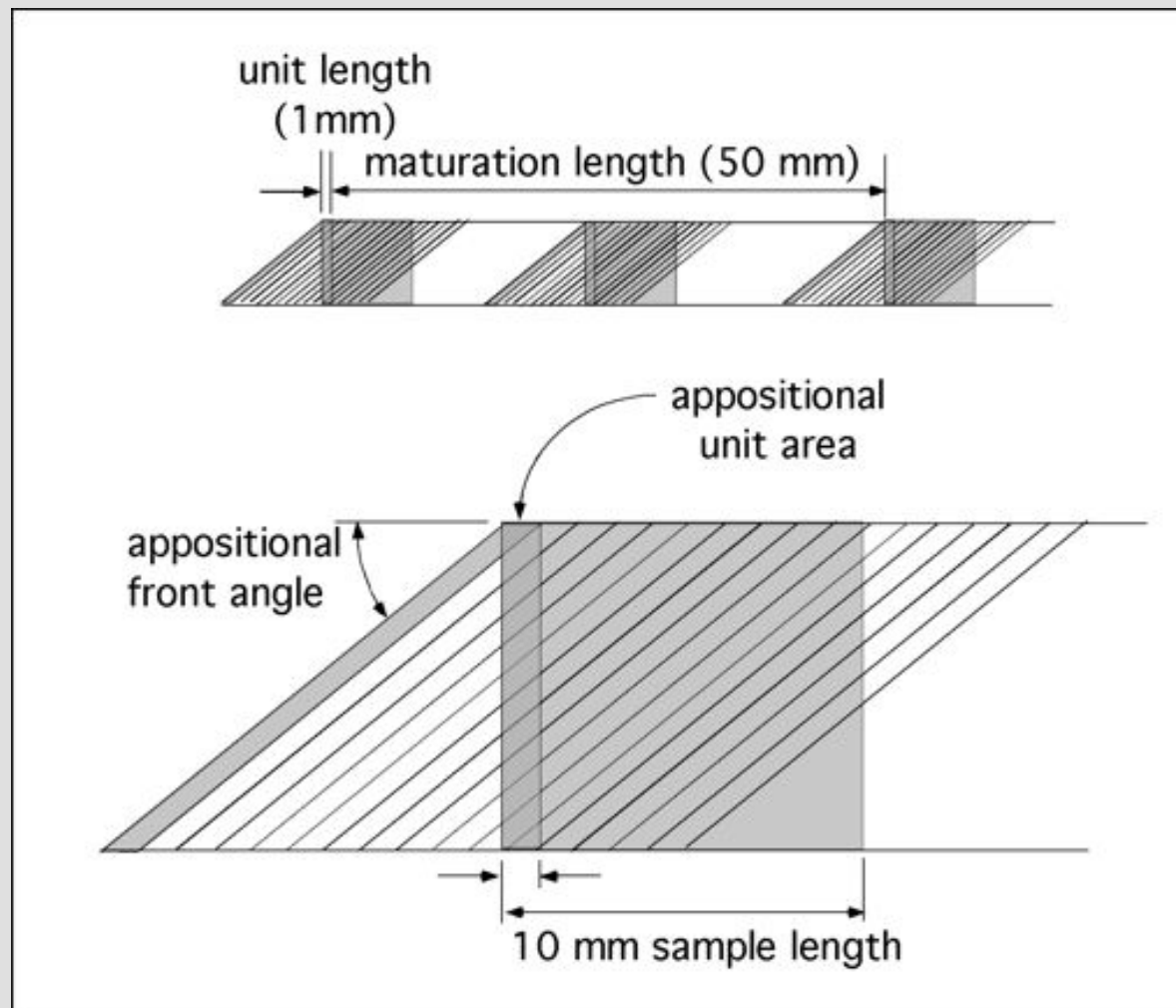
Limit to sample resolution: can
never get pure signal no
matter what the sampling
strategy

-Passey and Cerling, 2002

percent
final PO_4
(○)
percent
final density
(●)



model for enamel maturation and sampling

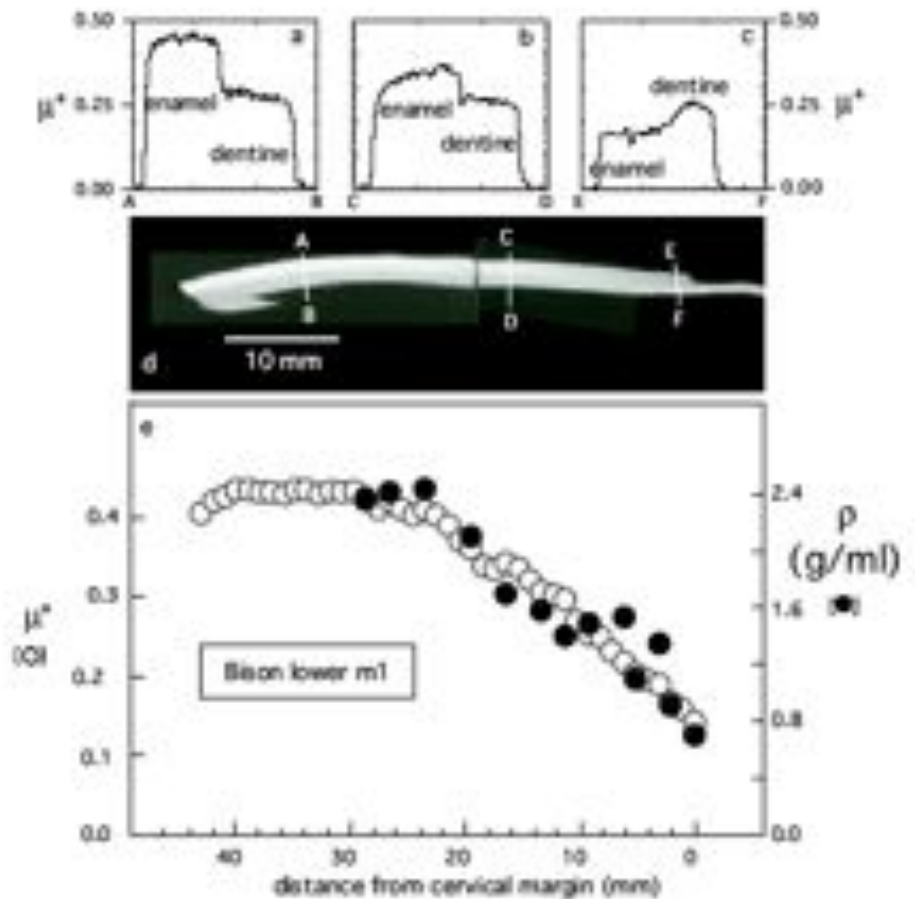


Maturation parameters: Micro-Computerized Tomography

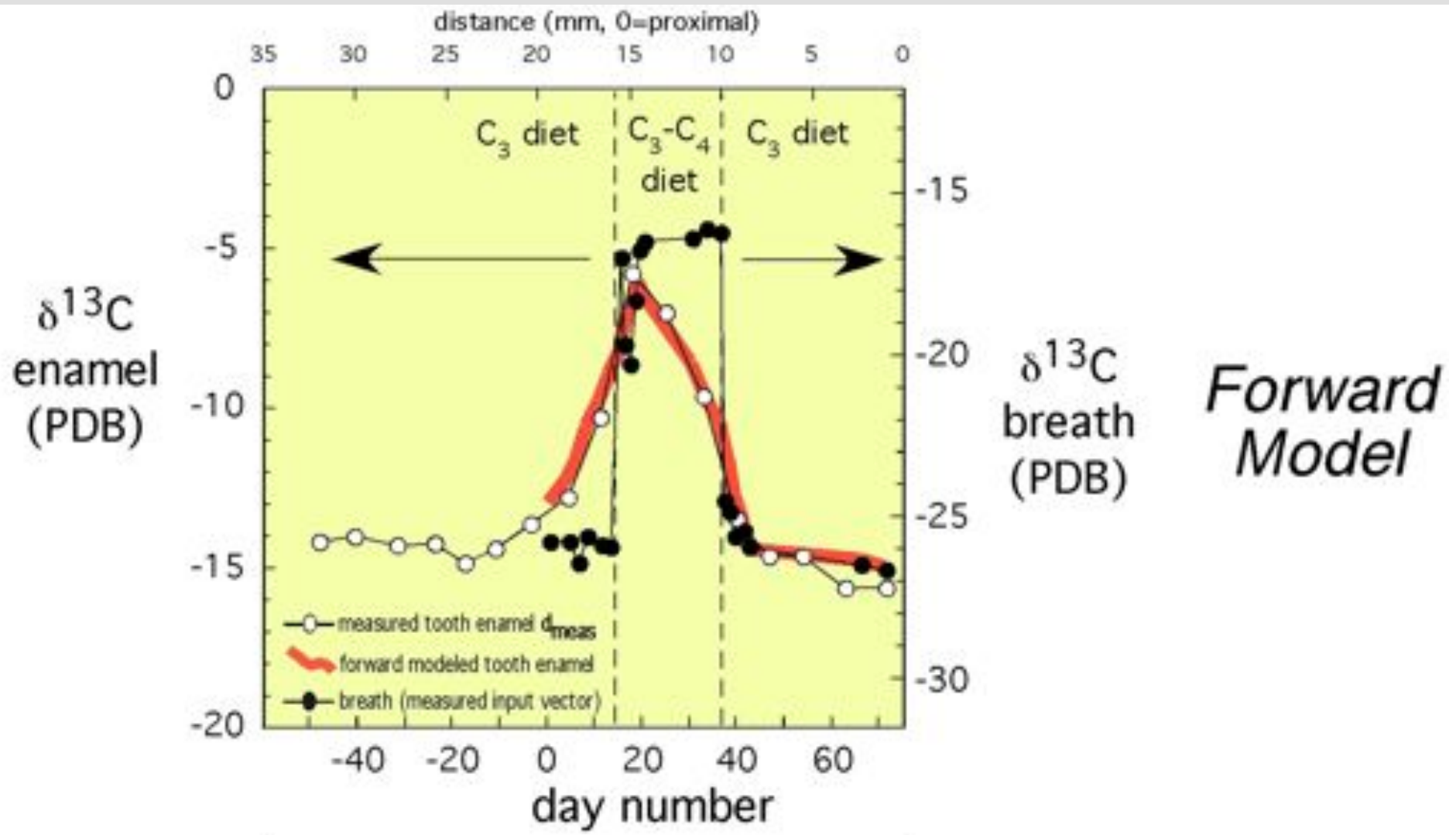
Micro-CT can be used to determine maturation parameters in developing tooth enamel

Corroborated by *in situ* density measurements

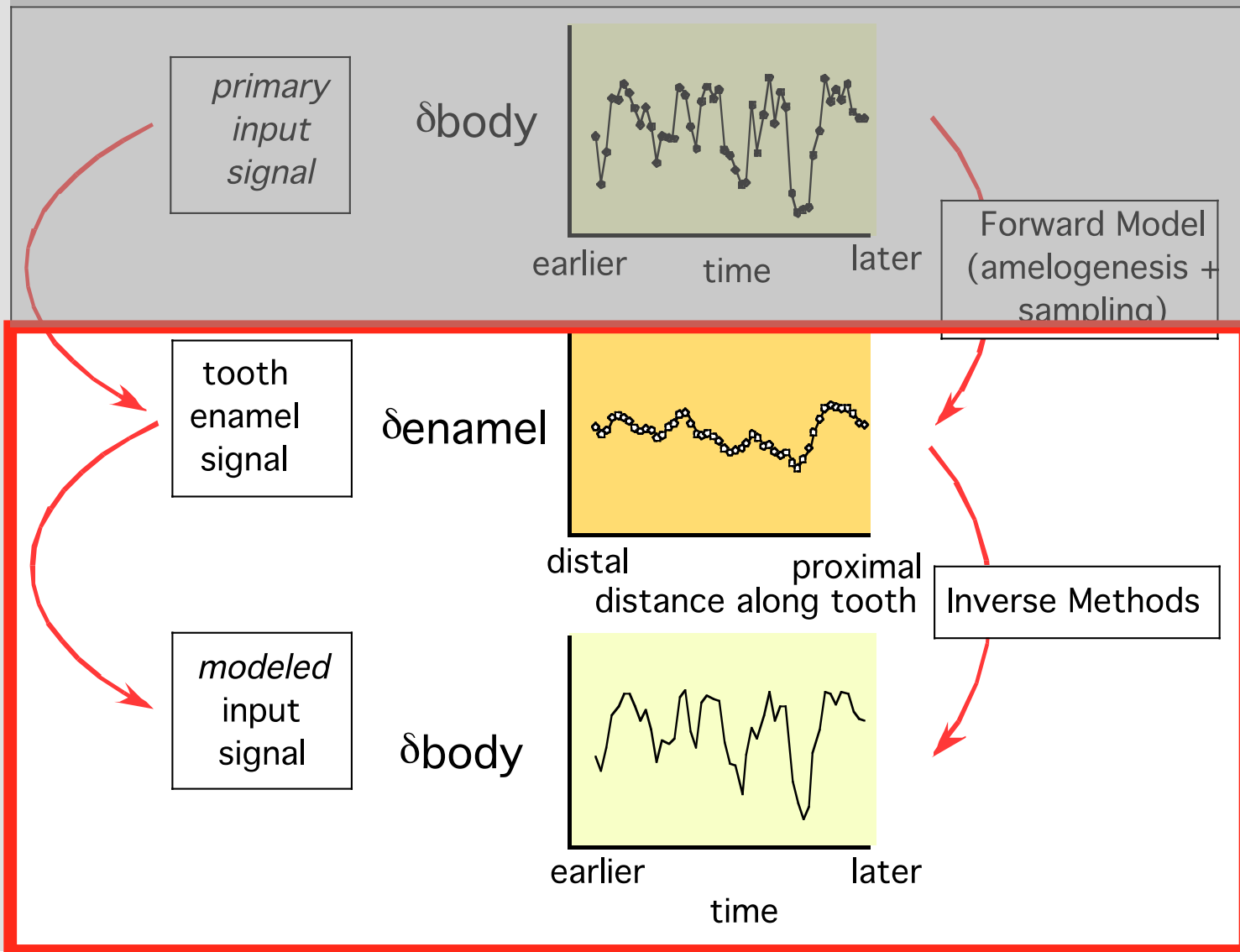
-Passey and Cerling, unpublished



Controlled diet change for rabbit. Forward model for teeth based on breath data and maturation parameters. Passey et al (2005).



Real input vs. modeled output



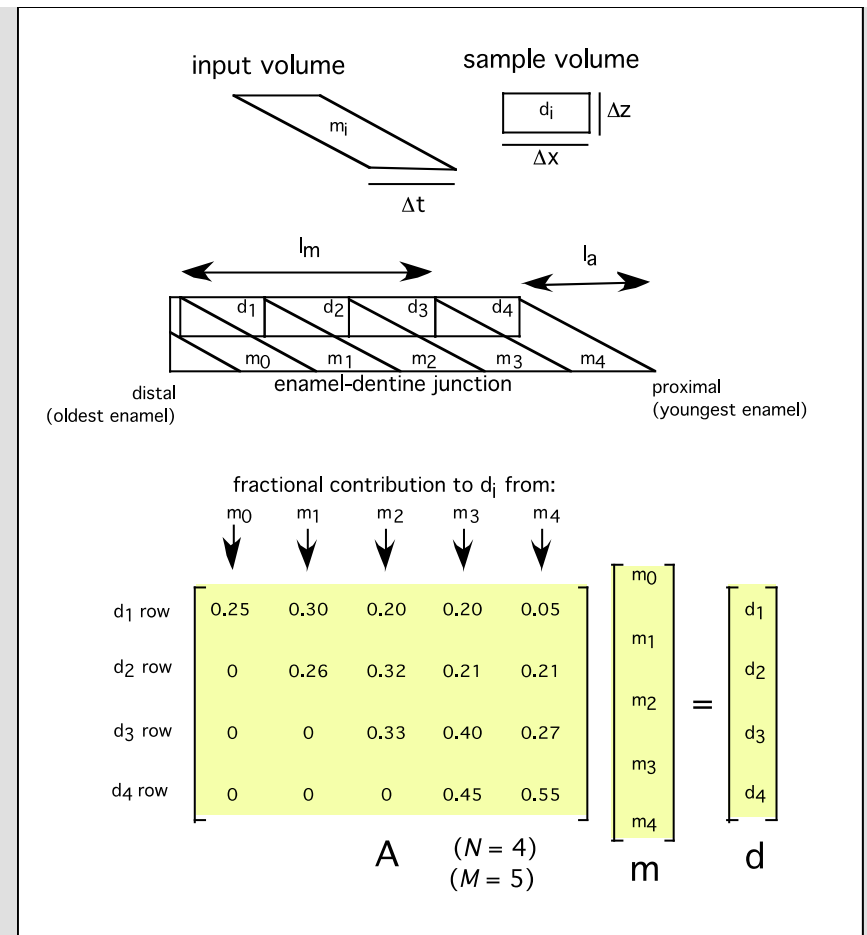
Inversion solution: (Meinke's "moving camera")

Set up input as matrix:

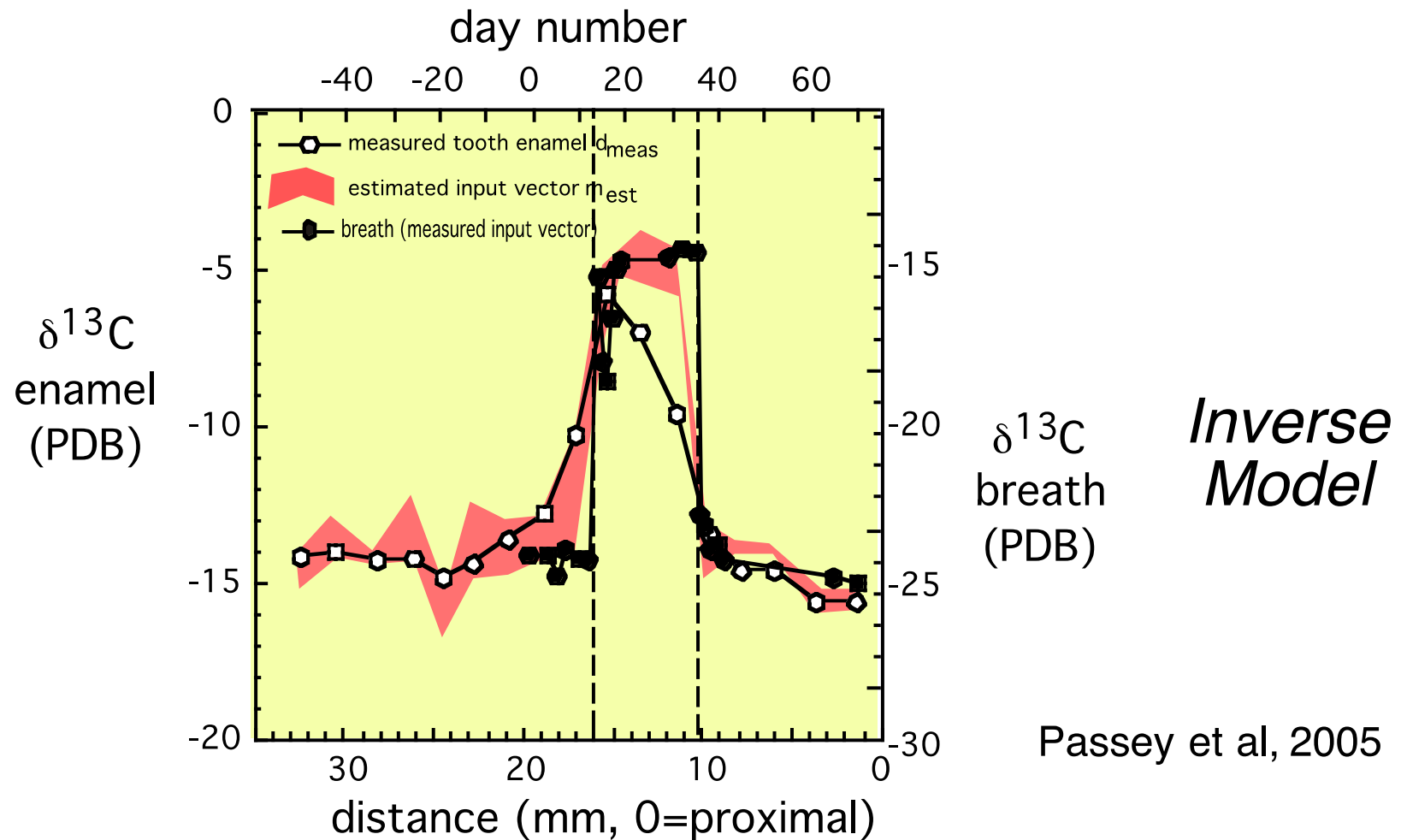
$$\mathbf{A}\mathbf{m} = \mathbf{d}$$

The inverse solution to solve for the input is:

$$\mathbf{m}_{\text{est}} = \langle \mathbf{m} \rangle + \mathbf{A}^T [\mathbf{A}\mathbf{A}^T + \varepsilon^2 \mathbf{I}]^{-1} [\mathbf{d} - \mathbf{A}\langle \mathbf{m} \rangle]$$

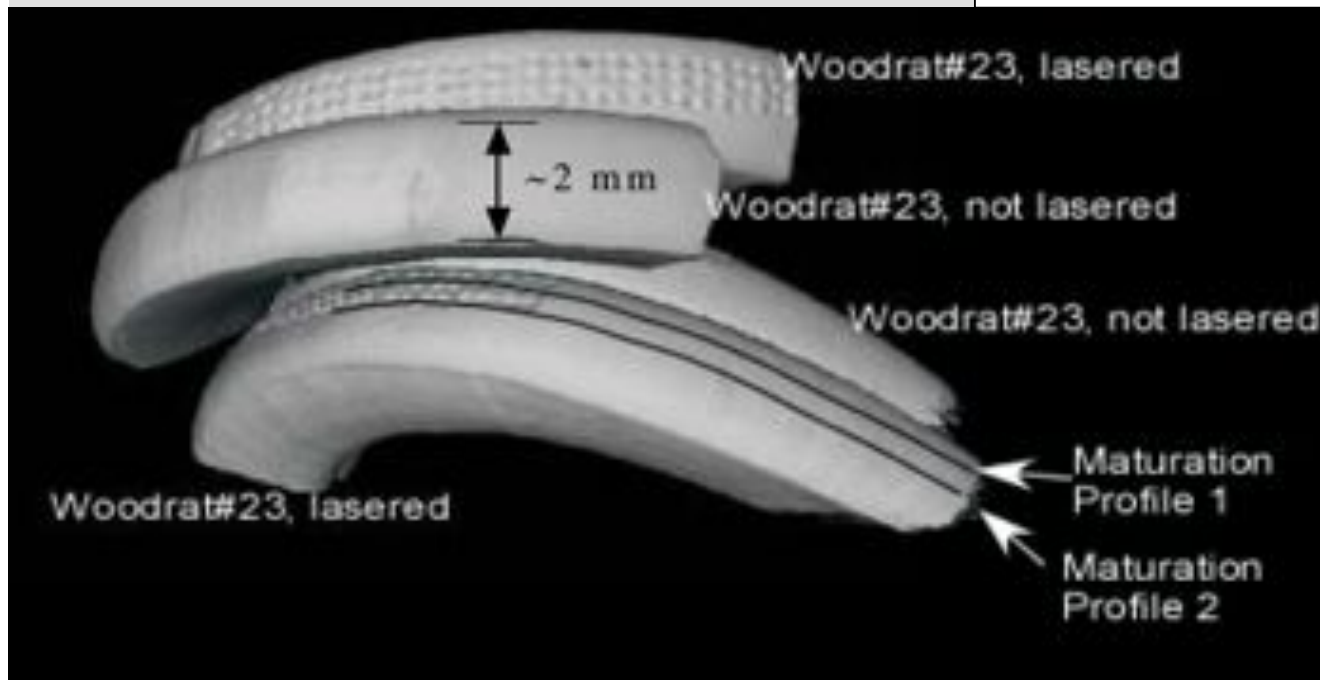
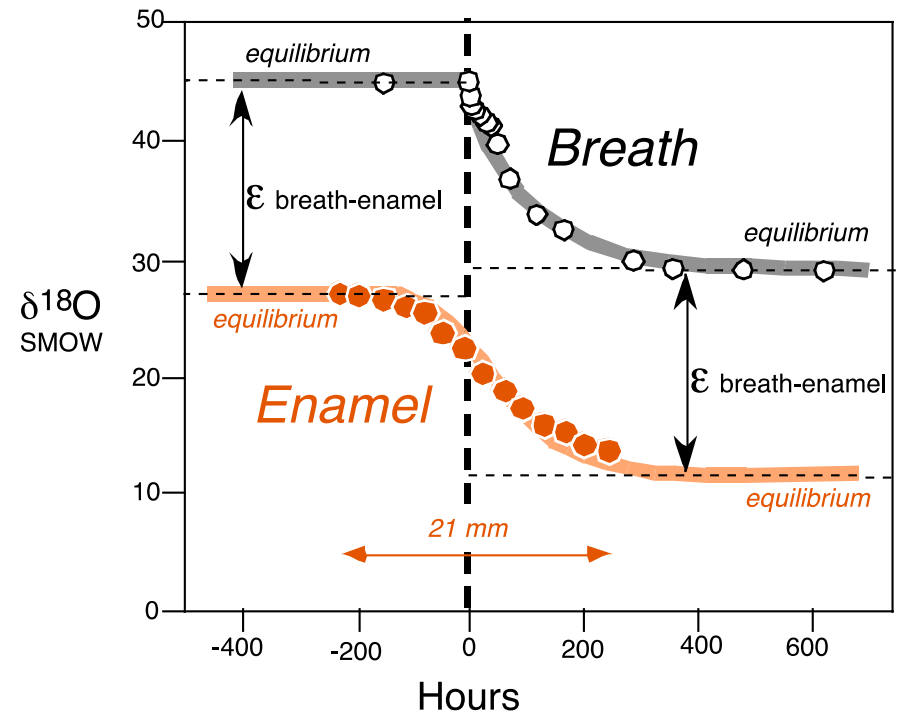


Inversion method recovers original input



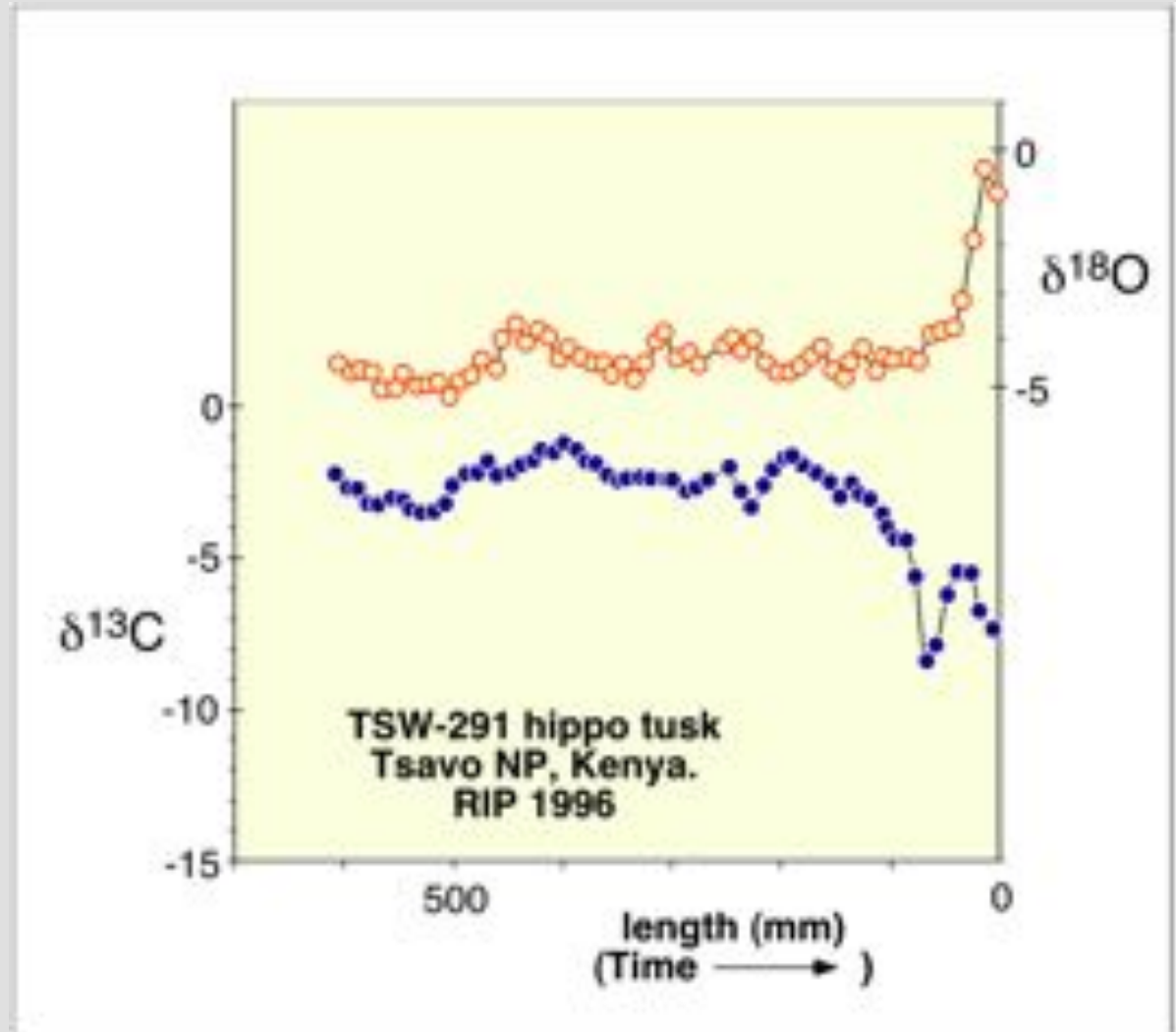
Laser ablation: micro-sampling

- Podlesak et al., 2007



Hippo tusk: Tsavo NP, Kenya

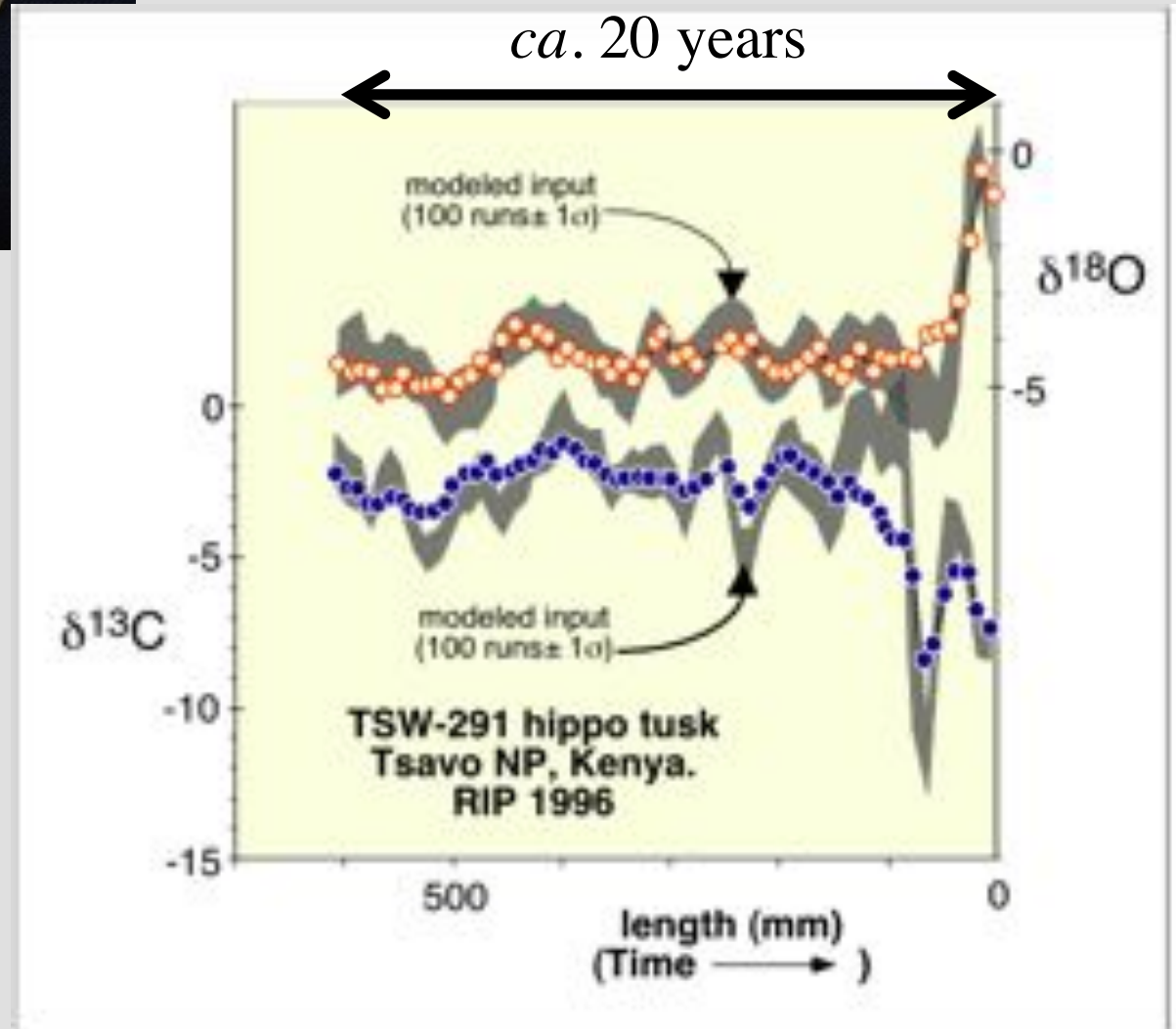
- 610 mm tusk
- Known facts: died during drought
- $\delta^{13}\text{C}$ shows gradual decline in diet quality, $\delta^{18}\text{O}$ shows gradual rise
- Reconstruction:
 - Severe diet stress
 - Severe water imbalance



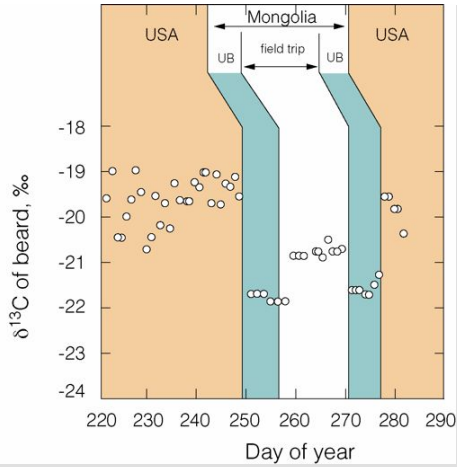
Diet reconstruction



- 100 inversions: $\pm 1\sigma$
- $l_m = 45$ to 65 mm
- $l_a = 8$ to 12 mm
- $x \pm 1$ mm; $z \pm 0.2$ mm
- $\delta^{13}\text{C}$: $\pm 0.1\text{‰}$.



You are what you eat (+ a few ‰):
you cannot escape your history



Modern: detailed history (to a single day)

- diet
- migration
- climate change
- land-use change

